

From exotic hadrons to light nuclei

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Graz Center of Physics (GCP)



NAWI Graz:

Cooperation between TU Graz & Uni Graz

- 36 institutes, ~6000 students: Bioscience, Chemistry, Earth, space & environmental science, Mathematics, Physics
- Common bachelor & master programs (Physics: ~500 physics, ~200 teacher students)

Graz Center of Physics (GCP)

will house TU Graz & Uni Graz Physics departments



- On Uni Graz Campus, next to current physics building
- 380 M€ investment, biggest university construction project in Styria in several decades
- 25.000 m² lab, office & lecture hall space for 600 staff members & 1700 students; lecture halls also ideal for big conferences
- Construction starting now, to be completed by 2030
- Theoretical Particle Physics: one of ~7 research groups

Motivation

· Understanding exotic hadrons







P P P



Glueballs

Hybrid mesons

Tetraquarks

Pentaquarks

• Light dibaryons Dyson, Xuong 1964



Adlarson et al., PRL 106 (2011), PRL 112 (2014), Bashkanov, Brodsky, Clement, PLB 727 (2013), Gal, Garcilazo, PRL 111(2013), . . .

• Strange dibaryons NPLQCD, HALQCD, USQCD, PACS-CS, ...



Illa et al., PRD 103 (2021)

Nucleons in nuclei?
 Short-range correlations, EMC effect?
 CLAS: Duer et al. Nature 560 (2018). Schmidt et al. Nature 578 (2020)

Theory tools



Functional methods

• Hadronic **bound-state equations** (Bethe-Salpeter & Faddeev eqs)



- "QFT analogue of Schrödinger eq."
 - → hadron masses & "wave functions"
 - \rightarrow spectroscopy calculations

 Ingredients: QCD's n-point functions, Satisfy quantum eqs. of motion (DSEs)



- → Dynamical mass generation, gluon mass gap, confinement, ...
- Structure calculations: form factors, PDFs, GPDs, TMDs, two-photon processes, ...





Baryons



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• Quark-diquark (two-body) equation

GE, Fischer, Sanchis-Alepuz, PRD 94 (2016)

Oettel et al., PRC 58 (1998), GE et al., Ann. Phys. 323 (2008), Cloet et al., FBS 46 (2009), Segovia et al., PRL 115 (2015)



Three-guark and guark-diguark results very similar

Diquark clustering in baryons? Barabanov et al., Prog. Part. Nucl. Phys. 116 (2021)





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• Quark-diquark (two-body) equation Oettel et al., PRC 58 (1998), GE et al., Ann. Phys. 323 (2008),...



• Three-quark and quark-diquark results very similar GE, Fischer, Sanchis-Alepuz, PRD 94 (2016)

 $\frac{1}{2}^{+}$ $\frac{1}{2}^{-}$ $\frac{3}{2}^{+}$ $\frac{3}{2}$ $\frac{3}{2}^{+}$ $\frac{3}{2}$ $\frac{1}{2}^{+}$ $\frac{1}{2}^{-}$ M [GeV] 2.0 ∆(1940) N(1895) N(1900) N(1875) ∆(1920) ∆(1900) N(1880) ∆(1910) 1.8 N(1710) N(1700) N(1720) N(1650) ∆(1700) <u></u>Δ(1620) 16 N(1535) N(1520) _ ∆(1600) 1.4 qqq q-dq -**I** ∆(1232) 1.2 PDG ** PDG *** PDG **** 1.0 - N(940)

Heavy baryons Torcato, Arriaga, GE, Peña, FBS 64 (2023)



Towards ab-initio

• Goal: go towards ab-initio calculations by calculating higher n-point functions



...,

Williams, Fischer, Heupel, PRD 93 (2016), Cyrolet al., PRD 97 (2018), Oliveira, Silva, Skullerud, Sternbeck, PRD 99 (2019), Aguilar et al., EPI C 80 (2020), Huber, PRD 101 (2020), Qin, Roberts, Chin. Phys. Lett. 38 (2021), GF, Pavlovski, Silva, PRD 104 (2021),



• Glueball spectrum agrees with lattice QCD Huber, Fischer, Sanchis-Alepuz, EPJ C 80 (2020), EPJ C 81 (2021)



Coupled Yang-Mills DSEs

Huber, PRD 101 (2020), GE, Pawlowski, Silva, PRD 104 (2021)



Exotic mesons



- Several tetraquark candidates in **charmonium spectrum**: X(3872), X(3915), Zc(3900),
- Z states cannot be cc since they carry charge
- Recent additions: all-charm X(6900), open-charm T_{cc}^+ , ...
- Oldest tetraquark candidates: light scalar mesons

Reviews:

Chen, Chen, Liu, Zhu, Phys. Rept. 639 (2016), 1601.02092 Lebed, Mitchell, Swanson PPNP 93 (2017), 1610.04528 Esposito, Pilloni, Polosa, Phys. Rept 668 (2017), 1611.07920 Guo, Hanhart, Meißner et al., Rev. Mod. Phys. 90 (2018), 1705.00141 Ali, Lange, Stone, PPNP 97 (2017), 1706.00610 Olsen, Skwarnicki, Zieminska, Rev. Mod. Phys. 90 (2019), 1708.04012 Liu, Chen, Chen, Liu, Zhu, PPNP 107 (2019), 1903.11976 Brambilla, Eidelman, Hanhart et al., Phys. Rept. 873 (2020)

Light exotic mesons



Light exotic mesons





 Diquark-antidiquark? Explains mass ordering & decay widths Jaffe 1977, Close, Tornqvist 2002, Maiani, Polosa, Riquer 2004







- Meson molecules?
 Weinstein, Isgur 1982, 1990; Close, Isgur, Kumano 1993
- Non-qq nature supported by various approaches Pelaez, Phys. Rept. 658 (2016)



		dim <i>K</i>	memory
$K \psi_i = \lambda_i \psi_i$	Mesons	10 ³	20 MB
	Baryons	10 ⁸	10 ⁷ GB
	Tetraquarks	10 ¹³	10 ¹⁸ GB



• Group momentum variables into multiplets of **permutation group S4:** can switch off groups of variables without destroying symmetries GE, Fischer, Heupel, PRD 92 (2015)

 $f_i(\mathcal{S}_0, \nabla, \mathbf{O})$

• Light scalar mesons $(\sigma, \kappa, a_0, f_0)$ as **four-quark states**: GE, Fischer, Heupel, PLB 753 (2016) M [GeV]+ perm. 15 1.0 $\doteq a_0/f_0$ BSE dynamically generates meson poles in BS amplitude: diquark pole $f_i(\mathcal{S}_0, \nabla, \langle h \rangle, \bigcirc) \rightarrow 1500 \text{ MeV}$ $f_i(\mathcal{S}_0, \nabla, \triangle, \bigcirc) \rightarrow 1500 \text{ MeV}$ 0.5 $f_i(\mathcal{S}_0, \nabla, \mathbf{A}, \mathbf{O}) \rightarrow 1200 \text{ MeV}$ meso $f_i(\mathcal{S}_0, \nabla, \triangle, \odot) \rightarrow 350 \text{ MeV }!$ Dol 0.0 "Light scalar mesons" look like meson molecules. 8 10 diquark-antidiquark components almost negligible. $m_a [MeV]$ Lightness is inherited from pseudoscalar Goldstone bosons!

Two-body formulation: **meson-meson / diquark-antidiquark**, follows from four-quark eq. (analogue of quark-diquark for baryons) Heupel, GE, Fischer, PLB 718 (2012)



- Interaction by quark exchange
- System 'wants' to be meson-meson-like (no diagonal dq-dq term)
- Similar results as in 4-quark approach: m_σ ~ 400 MeV, etc.

Two-body formulation: **meson-meson / diquark-antidiquark**, follows from four-quark eq. (analogue of quark-diquark for baryons) Heupel, GE, Fischer, PLB 718 (2012)



Include **mixing with q** $\overline{\mathbf{q}}$: $\pi\pi$ still dominant

Santowsky, GE, Fischer, Wallbott, Williams, PRD 102 (2020)

[MeV]	ground state mass	first excitation
$\pi\pi$	416 ± 26	970 ± 130
$\pi\pi + 0^+0^+$	416 ± 26	970 ± 130
$q\bar{q}$	667 ± 2	1036 ± 8
$\pi \pi + q\bar{q}$	472 ± 22	1080 ± 280
$\pi\pi + 0^+ 0^+ + q\bar{q}$	456 ± 24	1110 ± 110

Four-quark vs. qq dominance

Santowsky, Fischer, PRD 105 (2022)





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Heavy-light **4q states** Wallbott, GE, Fischer, PRD 100 (2019), PRD 102 (2020)



Hidden charm & bottom states

Hoffer, GE, Fischer, PRD 109 (2024) Wave-function components:

- 1⁻⁻, 0⁺⁺, 1⁺⁺ dominated by molecular component
- 1⁺⁻ is mixture, hadrocharmonium is strongest







preliminary



meson molecule



diquark-antidiquark



 J^P



 $I(0^+) = 0(1^+) = 1(1^+)$

$I(J^P)$	1	Physical components					
		1	$\otimes 1$	$\bar{3}\otimes3$	8	⊗8	${\bf 6}\otimes {\bf \bar 6}$
		f_0	f_1	f_2	f_3	f_4	f_5
1(0+)	$cc\bar{q}\bar{q}$	DD	D^*D^*	$A_{cc}A$	DD	D^*D^*	$S_{cc}S$
1(0)	$bb\bar{q}\bar{q}$	BB	B^*B^*	$A_{bb}A$	BB	B^*B^*	$S_{bb}S$
$0(0^{+})$	$bc\bar{q}\bar{q}$	BD	B^*D^*	$A_{\rm bc}A$	BD	B^*D^*	$S_{bc}A$
	$cc\bar{q}\bar{q}$	DD^*	D^*D^*	$A_{cc}S$	DD^*	D^*D^*	$S_{cc}A$
$0(1^+)$	$bb\bar{q}\bar{q}$	BB^*	B^*B^*	$A_{bb}S$	BB^*	B^*B^*	$S_{bb}A$
	$bc\bar{q}\bar{q}$	BD^*	B^*D	$S_{bc}A$	BD^*	B^*D	$A_{bc}S$
$1(1^+)$	$cc\bar{q}\bar{q}$	DD^*	-	$A_{cc}A$	DD^*	-	-
	$bb\bar{q}\bar{q}$	BB^*	-	$A_{bb}A$	BB^*	-	-

Pentaquarks?



• **5-body equation:** in progress GE, Peña, Torres, in preparation



 Meson-baryon equation with hadronic exchanges GE, Lourenco, Peña, Stadler, Torres, in preparation



Nucleons in nuclei?

Transition from quarks & gluons to light nuclei:



Microscopic origins of short-range nuclear force?

- Relativistic structure of deuteron?
- Exotic dibaryons, hypernuclei, short-range correlations, EMC effect ...

Deuteron



Hadron structure



Quark-gluon structure of hadrons and nuclei

- Flavor structure of proton, pion, kaon
- Spin and orbital angular momentum
- 3D imaging of nucleon and nuclei

Encoded in **parton distributions**, defined on the light front





Hadron-to-hadron correlator Vacuum-to-hadron correlator

 $\mathcal{G}(z, P, \Delta) = \langle P_f | \mathsf{T} \Phi(z) \mathcal{O} \Phi(0) | P_i \rangle$

 $\Psi(z,P) = \langle 0 | \mathsf{T} \, \Phi(z) \, \Phi(0) | P \rangle$

	$\mathcal{G}(q, P, \Delta = 0)$	$\mathcal{G}(q,P,\Delta)$	$\Psi(q,P)$
$\int dq^{-}$	TMD	GTMD	LFWF
$\int d^2 {oldsymbol q}_\perp \int dq^-$	PDF	GPD	PDA

Diehl, Phys. Rept. 388 (2003) Belitsky, Radyushkin, Phys. Rept. 418 (2005) Lorcé, Pasquini, Vanderhaeghen, JHEP 05 (2011)

Hadron structure



Hadron-to-hadron correlator



Bethe-Salpeter WF: vacuum-to-hadron correlator



$\mathcal{G}(z, P, \Delta) = \langle P_f 1$	$(P, \Delta) = \langle P_f \uparrow \Phi(z) \mathcal{O} \Phi(0) P_i \rangle$		$\Psi(z,P) = \langle 0 T \Phi(z)$		
	$\mathcal{G}(q,P,\Delta=0)$	$\mathcal{G}(q,P,\Delta)$	$\Psi(q, P)$		
$\int dq^- \int d^2 oldsymbol{q}_\perp \int dq^-$	TMD PDF	GTMD GPD	LFWF PDA		

2 $\operatorname{Im}\sqrt{x'}$ 0 $\frac{2}{\text{Re}\sqrt{x'}}$

New method to compute light-front wave functions via contour deformations

Editors' Suggestion: GE, Ferreira, Stadler, PRD 105 (2022) Diehl, Phys. Rept. 388 (2003) Belitsky, Radyushkin, Phys. Rept. 418 (2005) Lorcé, Pasquini, Vanderhaeghen, JHEP 05 (2011)

TMDs



Outlook

• Hyperons and charmed baryons: Spectroscopy, form factors, structure



• Exotic hadrons: can quantify strength of different internal components



Dibaryons & baryon-baryon interactions

• Hadron structure: PDFs, GPDs, TMDs



Spectroscopy, form factors, PDFs, scattering amplitudes

Thank you!

Backup slides

QCD phase diagram



Search for critical endpoint (CEP) from DSEs & lattice:



Fischer, Prog. Part. Nucl. Phys. 105 (2019)

Location of CEP sensitive to baryons?

GE, Fischer, Welzbacher, PRD 93 (2016)



Baryon structure







Mesons and diquarks closely related through BSE Maris, FBS 32 (2002)



Lowest-lying diquarks are dominant for ground-state octet & decuplet baryons

 pseudoscalar mesons
 ⇔
 scalar diquarks (~0.8 GeV)

 vector mesons
 ⇔
 axialvector diquarks (~1 GeV)

Higher-lying diquarks are subleading, but contribute to excited states & remaining channels

scalar mesons axialvector mesons

- ⇔ pseudoscalar diquarks (~1.2 GeV)
- ⇔ vector diquarks (~1.3 GeV)



In RL, these are too strongly bound; simulate beyond-RL effects by (one) strength parameter c Roberts, Chang, Cloet, Roberts, FBS 51 (2011) GE, Fischer, Sanchis-Alepuz, PRD 94 (2016)

• Quark-diquark (two-body) equation

Oettel et al., PRC 58 (1998), GE et al., Ann. Phys. 323 (2008), Cloet et al., FBS 46 (2009), Segovia et al., PRL 115 (2015), Chen et al., PRD 97 (2018)







Relativistic effects

Orbital angular momentum: clear traces of nonrelativistic quark model, but strong relativistic effects (in some cases even dominant)



Relativistic contributions even up to bottom baryons! Qin, Roberts, Schmidt, PRD 97 (2018)



Towards ab-initio



Family of "decoupling" solutions, also seen in lattice QCD

Cucchieri, Maas, Mendes, PRD 77 (2008) Boucaud et al., JHEP 06 (2008) Bogolubsky et al., PLB 676 (2009) Fischer, Maas, Pawlowski, Ann. Phys. 324 (2009) Duarte, Oliveira, Silva, PRD 94 (2016) Aquilar et al., EPJ C 80 (2020)

Endpoint is "scaling" solution, confinement manifest

Lerche, Smekal, PRD 65 (2002) Fischer, Alkofer, PLB 536 (2002) Alkofer, Fischer, Llanes-Estrada, MPLA 23 (2008)

All solutions show aluon mass gap

$$\lim_{r \to \infty} \int \frac{d^3 Q}{(2\pi)^3} \frac{Z(\boldsymbol{Q}^2)}{\boldsymbol{Q}^2} e^{i \boldsymbol{x} \cdot \boldsymbol{Q}} \propto e^{-m_{\text{gap}} r}$$

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Truncation error

- Set $Z_{3g} \rightarrow c Z_{3g}$... quantifies deviation from STI (without truncation: c = 1), same effect from "over-renormalizing" 3-gluon vertex
- YM system only converges up to $\,c_{
 m max} < 1\,$
- · Anomalous dimensions reproduced for

$$\begin{array}{c|c} 1 & c \sim 0.4 \\ \hline 2 & c \sim 0.9 \\ \hline 3 & c \sim 0.96 \end{array} \end{array} \Rightarrow \begin{array}{c} \Rightarrow & \text{identifies "physical point"} \\ \text{for each truncation} \\ \hline & \text{GE Pawlowski, Silva, PRD 104 (2021)} \end{array}$$



Resonances

Most hadrons are resonances and decay
 ⇔ poles in complex momentum plane



BSE kernel must include decay channels:
 ρ meson becomes resonance

Williams, PLB 798 (2019), Miramontes, Sanchis-Alepuz, EPJA 55 (2019), Santowsky, GE, Fischer, Wallbott, PRD 102 (2020), Miramontes, Sanchis-Alepuz, Alkofer, PRD 103 (2021)



 Contour deformations as tool to go beyond thresholds GE, Duarte, Peña, Stadler, PRD 100 (2019)



Mesons

 Pion is Goldstone boson: m_π² ~ m_q



• Light meson spectrum beyond rainbow-ladder





GE, Sanchis-Alepuz, Williams, Alkofer, Fischer, PPNP 91 (2016)

- Bottomonium spectrum
 Fischer, Kubrak, Williams, EPJ A 51 (2015)
- · Pion transition form factor



GE, Fischer, Weil, Williams, PLB 774 (2017)

Strange baryons



GE, Fischer, FBS 60 (2019), Fischer, GE, PoS Hadron 2017

Strange baryons



New states from Bonn-Gatchina Sarantsev et al., 1907.13387 [nucl-ex]

GE, Fischer, FBS 60 (2019), Fischer, GE, PoS Hadron 2017