

Beyond the standard model: particle physics

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ELFT Particle Physics Summer School

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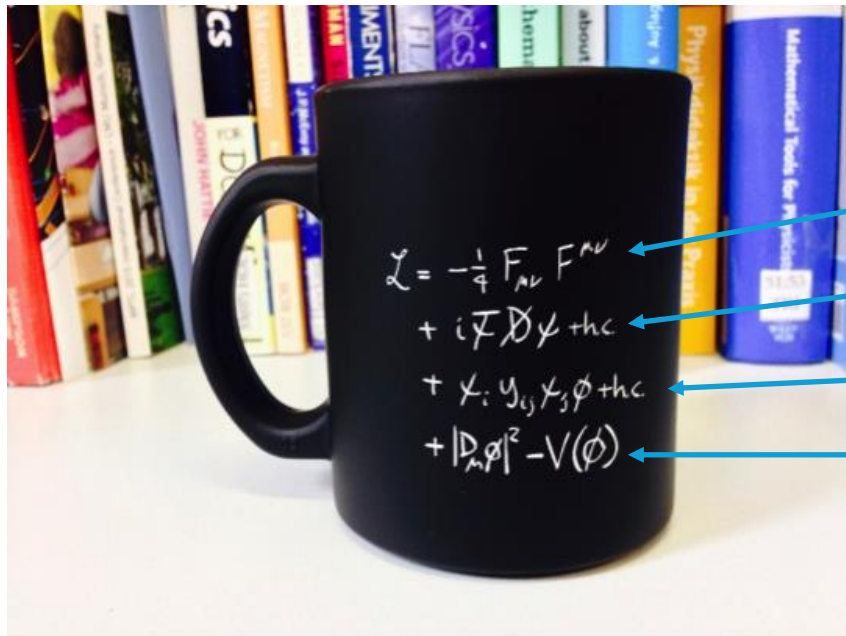
What is the standard model?

Elementary particles + interactions described precisely

THREE GENERATIONS OF MATTER (FERMIONS)

	I	II	III	
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name →	u up	c charm	t top	γ photon
QUARKS	4.8 MeV $-\frac{1}{3}$	104 MeV $-\frac{1}{3}$	4.2 GeV $-\frac{1}{3}$	0
	d down	s strange	b bottom	0
				1
				g gluon
LEPTONS	<2.2 eV 0	<0.17 MeV 0	<15.5 MeV 0	0
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	0
				1
				Z weak force
	0.511 MeV -1	105.7 MeV $-\frac{1}{2}$	1.777 GeV $-\frac{1}{2}$	80.4 GeV +1
	e electron	μ muon	τ tau	W weak force

BOSONS (FORCES)



Gauge interactions

Matter fermions

Yukawa interactions

Higgs potential

Tested before LHC (in some cases <0.1% precision!)

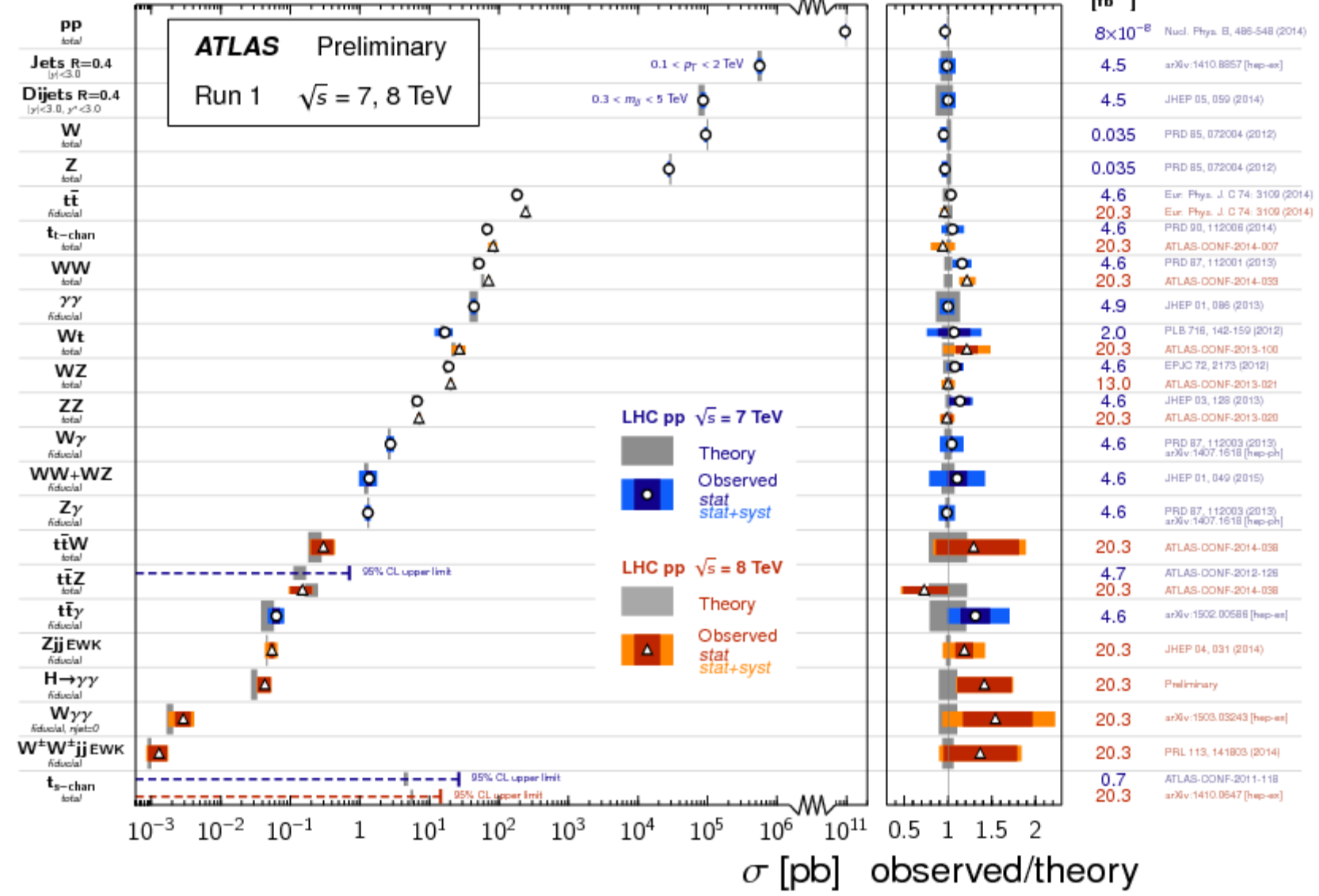
Testing in progress

Standard Model Production Cross Section Measurements

Status: March 2015

$$\int \mathcal{L} dt$$

Reference



What is beyond the standard model?

Cannot be explained in the SM:

- Neutrino masses
- Dark matter & dark energy
- Baryon asymmetry of the universe

New particles exist but hidden:

- Too heavy
- Interact too weakly

Anomalies as hint for new physics:

- 2-3 σ excesses at the LHC over SM expectation in certain processes
- Muon anomalous magnetic moment
- Promising (?) measurements to be verified independently:
 - X17 Atomki anomaly
 - CDF II measurement of the W boson mass

Puzzles (are related to the Higgs boson!):

$$\mathcal{L} = yH\psi\bar{\psi} + \frac{\mu^2}{2} |H|^2 - \frac{\lambda}{4} |H|^4 - V_0 + \dots$$

- Basically every parameter in this Lagrangian
- y : Fermion masses are free parameters, SM cannot explain their origin!
- μ gives rise to the naturalness problem
- λ is too small to make the vacuum stable...
- V_0 : does the Higgs field affect cosmic inflation?
- ...: any new terms in the Higgs potential?

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Let's start with the



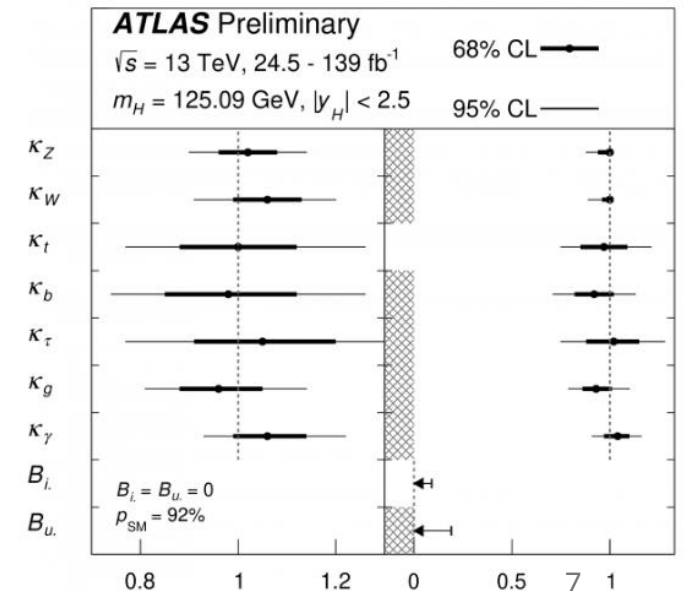
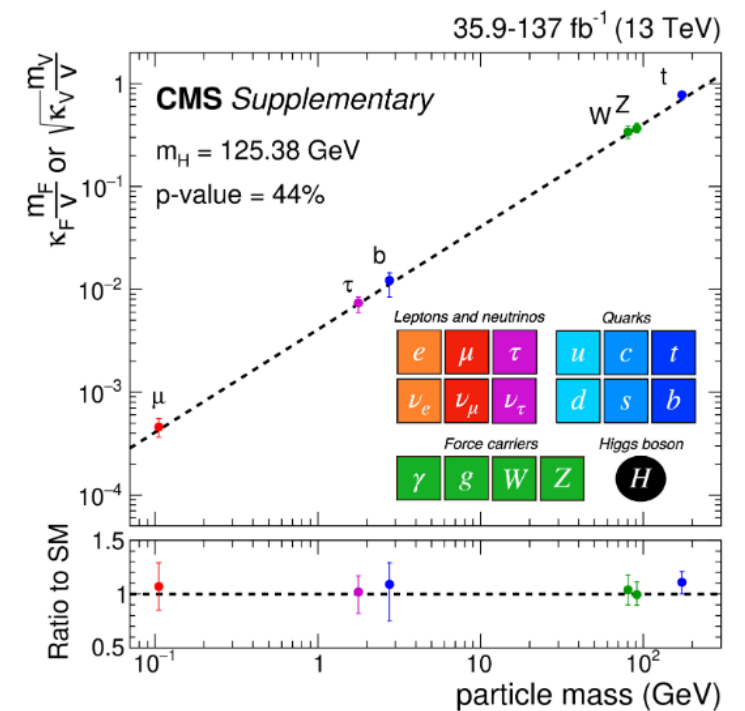
sector!

$$V(\phi) = -\frac{\mu^2}{2} |\phi|^2 + \frac{\lambda}{4} |\phi|^4$$

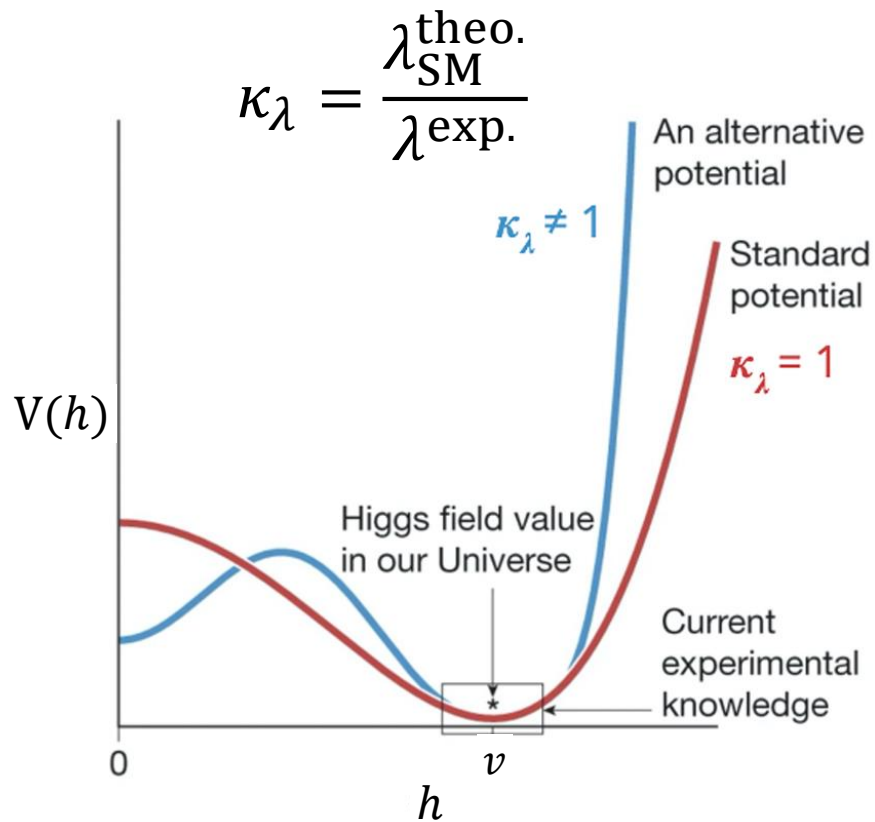
- Due to SSB: $\phi \rightarrow h + v$
- In the SM every mass is $\propto v$
- v and the masses are well measured
- Proportionality factor measured as well
- κ can signal deviation from SM

As for the Higgs boson:

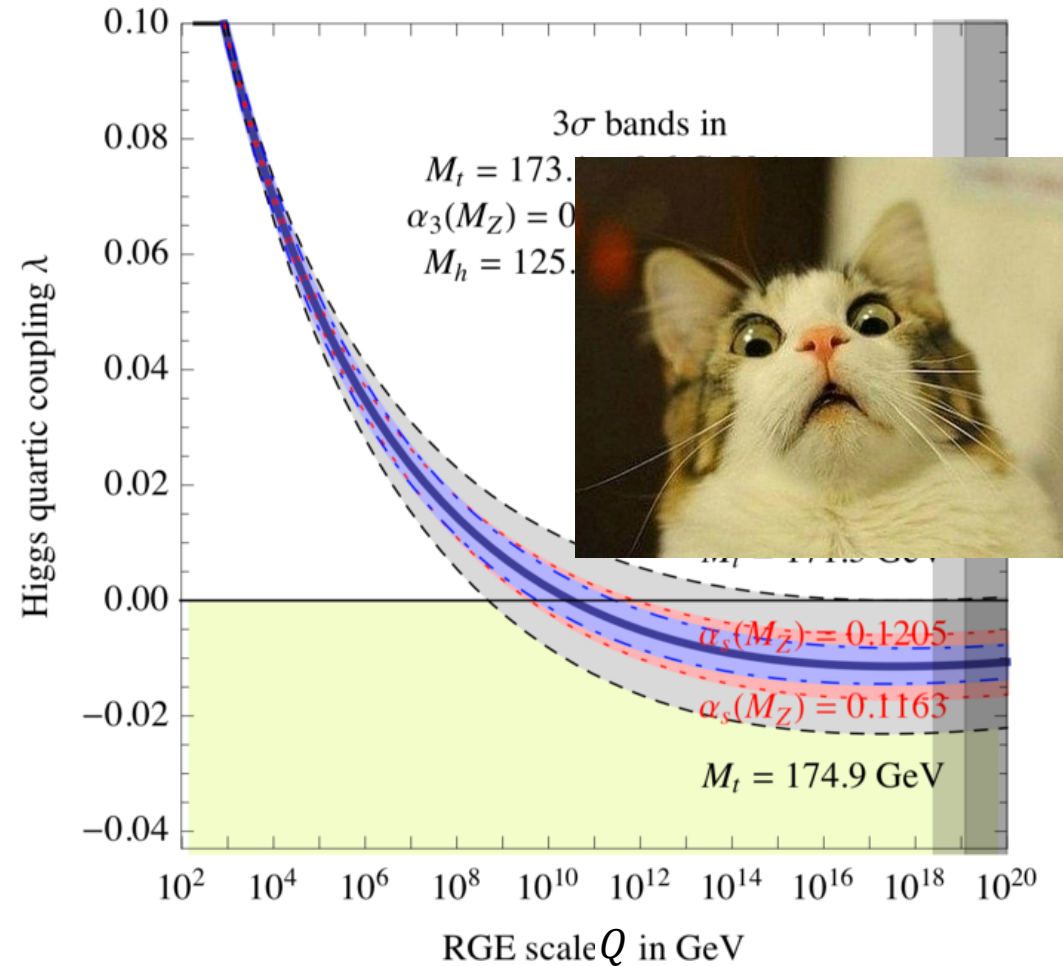
- From first derivative: $0 = -\mu^2 + \lambda v^2$
- From second derivative: $m_h^2 = -\mu^2 + 3\lambda v^2 = 2\lambda v^2$
- λ is predicted, not measured (yet)!



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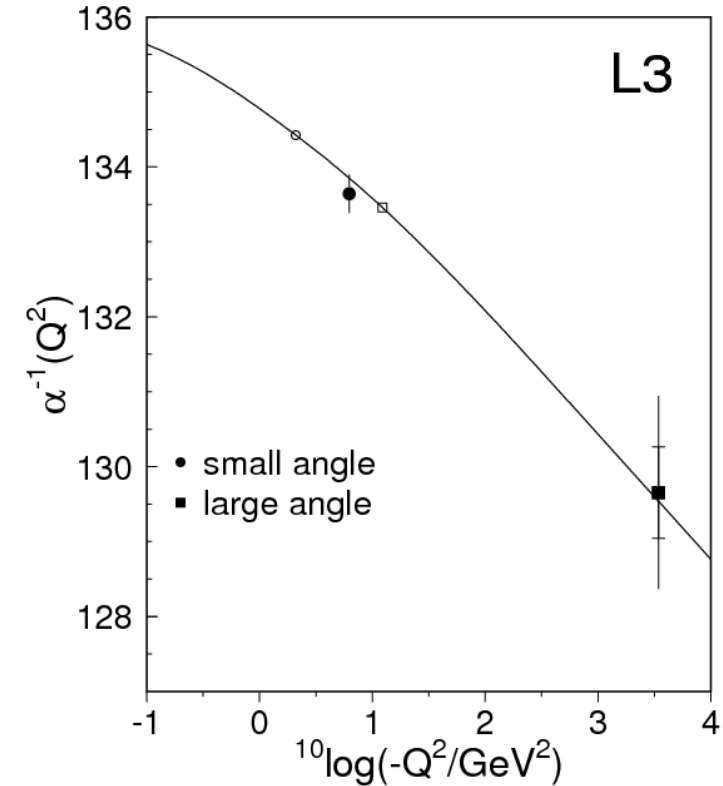
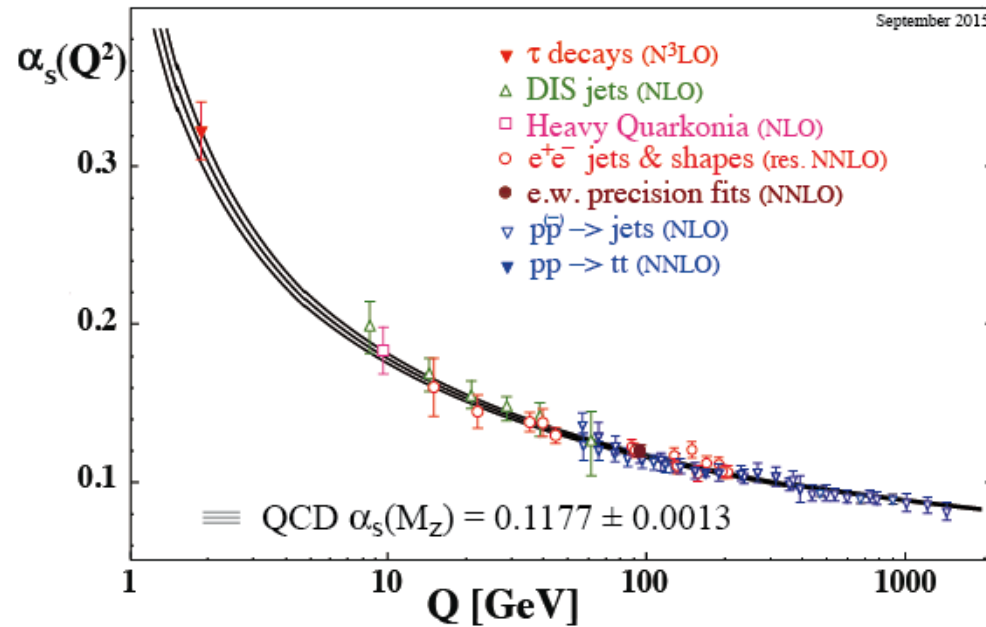


λ affects the shape of the potential...



...and depends on the energy scale

Scale dependence: $Q \frac{\partial g}{\partial Q} = \beta_g$ (RGE)



- If a collider has \sqrt{s} C.M. energy \rightarrow appropriate interaction strength is $g(Q = \sqrt{s})$
- Random processes due to quantum fluctuations can have much larger energies than colliders...

$$\beta_\lambda = \frac{1}{(4\pi)^2} \left(\underbrace{12\lambda^2}_{\text{Higgs boson}} + \frac{3}{8} \left(\underbrace{[g_y^2 + g_L^2]^2}_{\text{Z boson}} + \underbrace{2[g_L^2]^2}_{\text{W}^\pm \text{ bosons}} \right) - \underbrace{6y_t^4}_{\text{top quark}} + \dots \right)$$

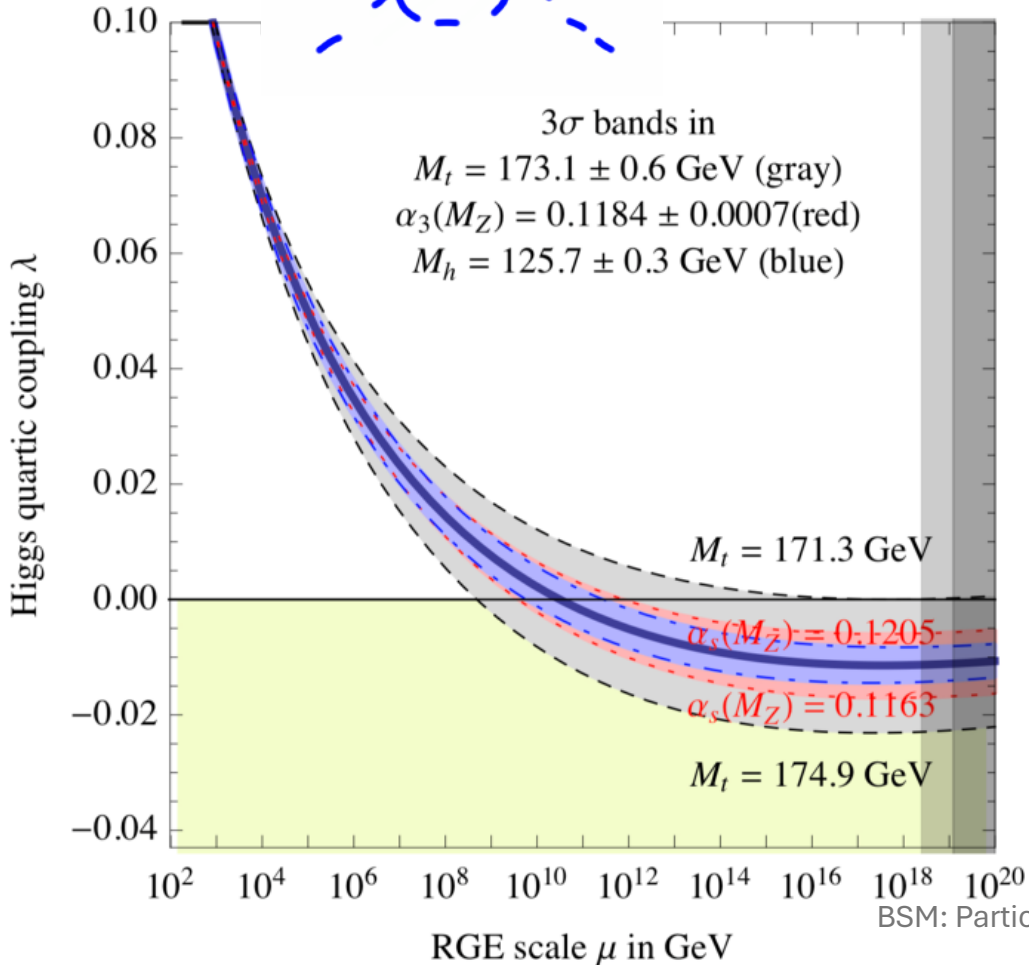


Higgs boson

Z boson

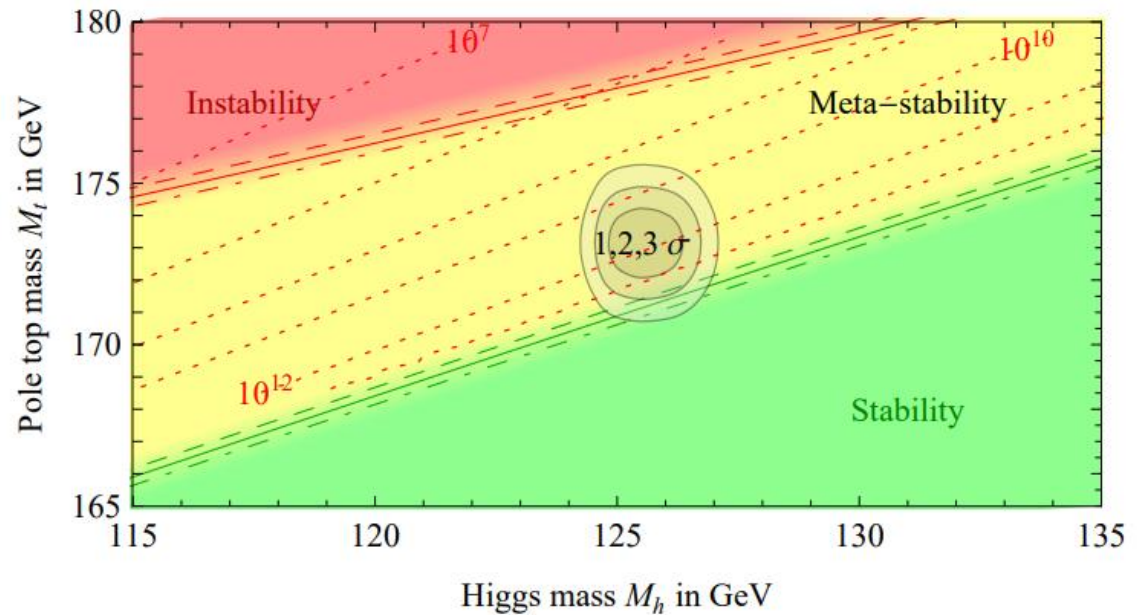
W[±] bosons

top quark



SM vacuum is metastable

Initial conditions are given at the E.W. scale



New physics should stabilize V !

$$V(\phi, \chi) = -\frac{\mu_\phi^2}{2} |\phi|^2 + \frac{\lambda_\phi}{4} |\phi|^4 - \frac{\mu_\chi^2}{2} |\chi|^2 + \frac{\lambda_\chi}{4} |\chi|^4 + \frac{\lambda}{2} |\phi|^2 |\chi|^2 + \dots$$

It is possible to extend the SM potential in many ways:

- **Scalar singlet (SSM)**
- Another doublet (2HDM)
- Many others, e.g.: 3HDM

Here ϕ is the **BEH doublet** field and χ is a **complex scalar singlet**

Extended potential \rightarrow **how to make it stable?**

- $\lambda_\phi > 0$ and $\lambda_\chi > 0$ obviously
- $4\lambda_\phi\lambda_\chi - \lambda^2 > 0$ if $\lambda < 0$

Why these terms in the potential?

- An additional global symmetry constrains it (more on this later)
- No higher orders than **[scalar field]⁴**: otherwise cutoff scale in the model!

What do we want?

- Scan **free parameters** and see if the V can be stable
- What are the free parameters? $\rightarrow \lambda_\phi, \lambda_\chi, \lambda$
- V has 5 params, but v and m_h have to be compatible with exp.
- Don't violate **perturbativity** $< 4\pi$
- The free params are initial conditions for **RG equations** at $Q = \text{EW. Scale}$
- Calculation of β -functions: can be **automatized** up to two loop (**SARAH** Mathematica package)

How to represent our findings?

- After SSB: $\phi \rightarrow h' + v$ and $\chi \rightarrow s' + w$

- The two fields mix to form *mass eigenstates*

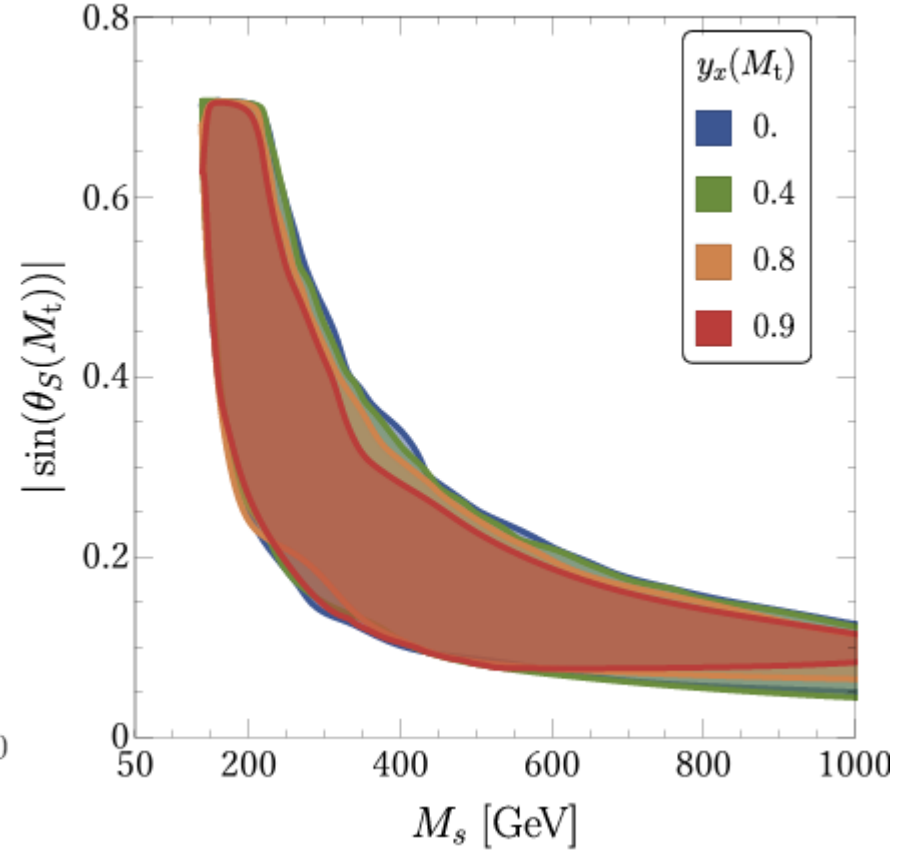
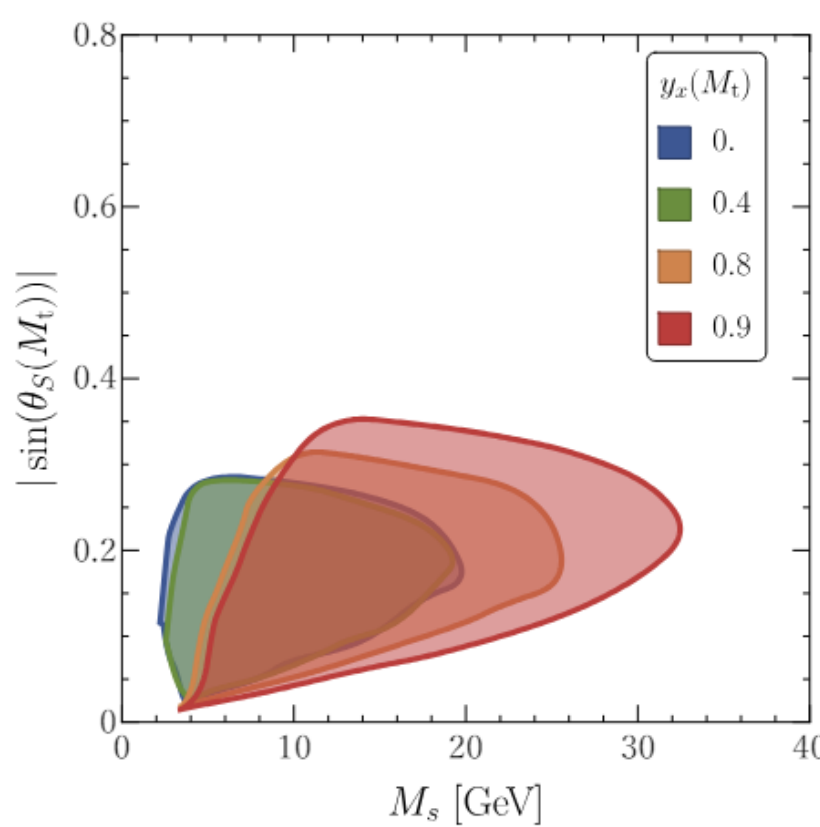
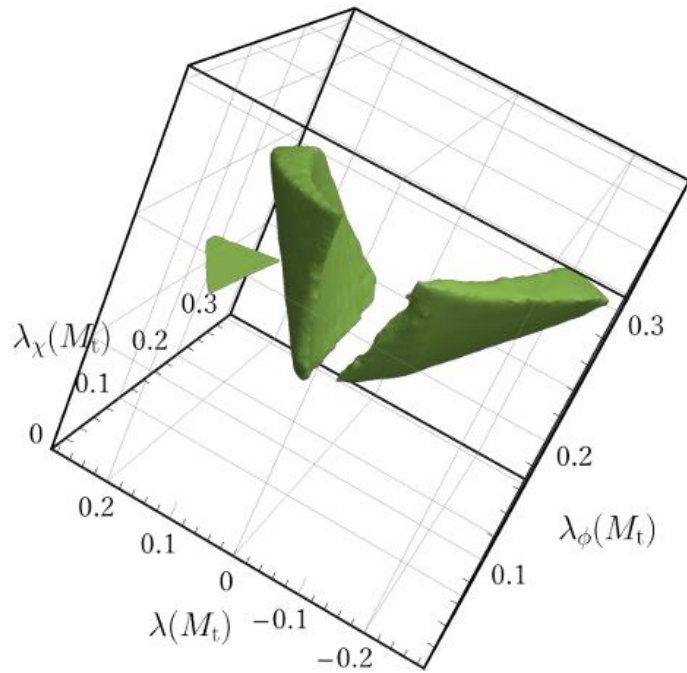
$$\begin{pmatrix} h' \\ s' \end{pmatrix} = \begin{pmatrix} \cos \theta_s & \sin \theta_s \\ -\sin \theta_s & \cos \theta_s \end{pmatrix} \begin{pmatrix} h \\ s \end{pmatrix}$$

- Good to have a basis where the **mass matrices** are **diagonal**:

$$m_{h/s}^2 = \lambda_\phi v^2 + \lambda_\chi w^2 \mp \frac{\lambda_\chi w^2 - \lambda_\phi v^2}{\cos 2\theta_s} \text{ with } \tan 2\theta_s = \frac{\lambda v w}{\lambda_\chi w^2 - \lambda_\phi v^2}$$

- **Experiments** can search for a scalar with m_s and θ_s !

Please ignore the colors

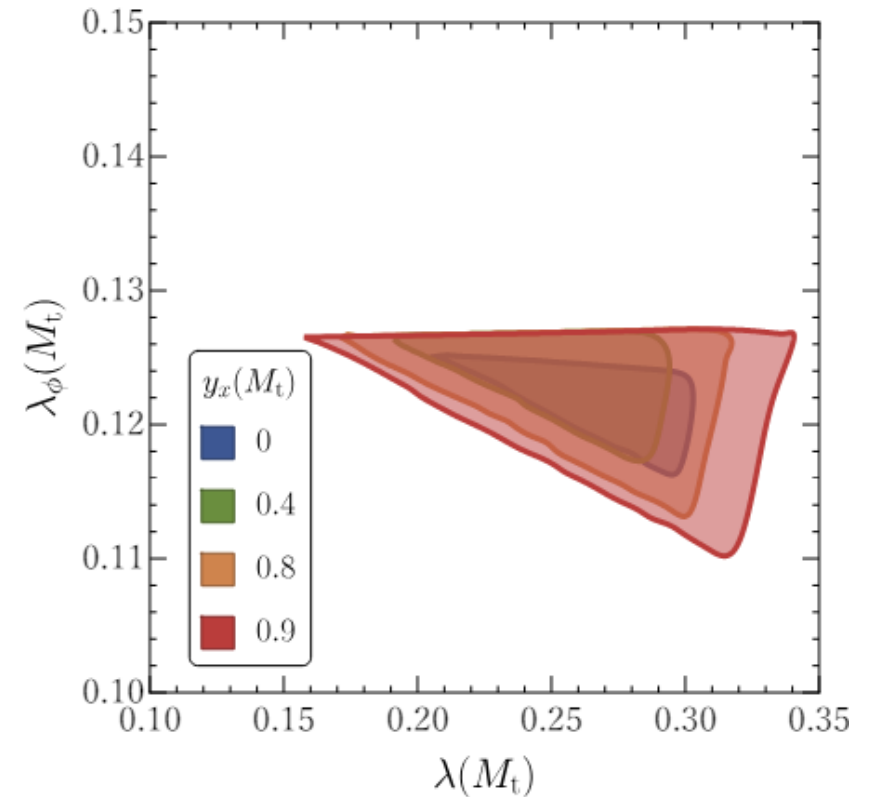


Lambda constraints
are strong!

Vacuum can be stabilized by either a lighter or a
heavier scalar than the Higgs boson!

Are we consistent with everything?

- The decay width of the Higgs boson is very small: $\Gamma_h = 3.2_{-2.2}^{+2.8}$ MeV
- The SM prediction is $\Gamma_h^{\text{SM}} \simeq 4$ MeV
- If the new scalar is lighter than $\frac{m_h}{2} \simeq 62.5$ GeV
- ...then $h \rightarrow s s$ decay is allowed!
- $\Gamma(h \rightarrow ss) \simeq \lambda^2 \frac{v^2}{32 \pi m_h} \simeq \lambda^2 \times (4.8 \text{ GeV})$



$\lambda < 0.03$ for consistent Γ_h but $0.15 < \lambda < 0.30$ for stability

Are we consistent with everything?

- What about electroweak observables?

$$M_W^{\text{PDG22}} = 80.379 \pm 0.012 \text{ GeV} \text{ or } M_W^{\text{CDFII}} = 80.433 \pm 0.009 \text{ GeV}$$

- While the SM prediction: $M_W^{\text{SM}} = 80.353 \pm 0.009 \text{ GeV}$
- M_W computed from the muon decay:

$$\frac{G_F}{\sqrt{2}} = \frac{\pi \alpha}{2 M_W^2 s_W^2} (1 + \Delta r)$$

- **New physics** affects the RHS, mostly $\Delta r \rightarrow \Delta M_W^{\text{BSM}}$

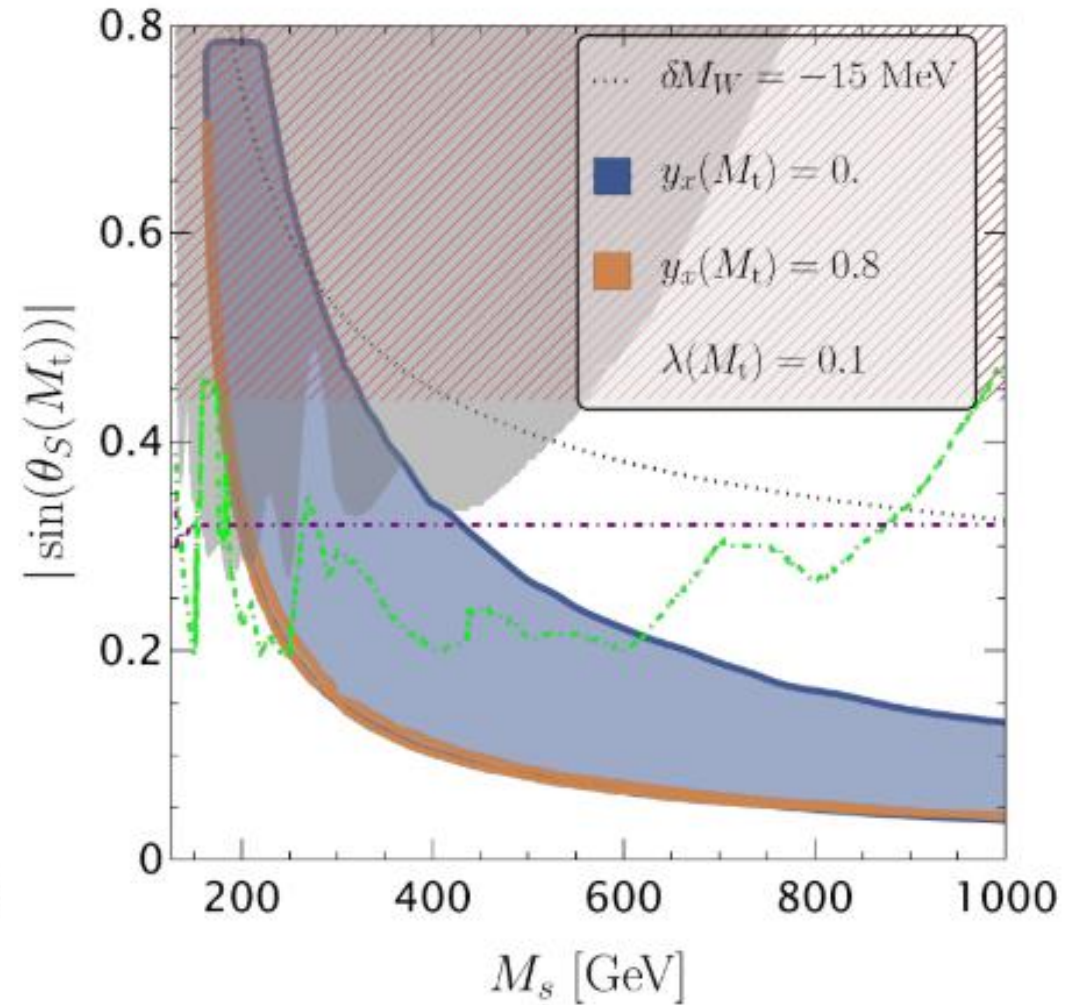
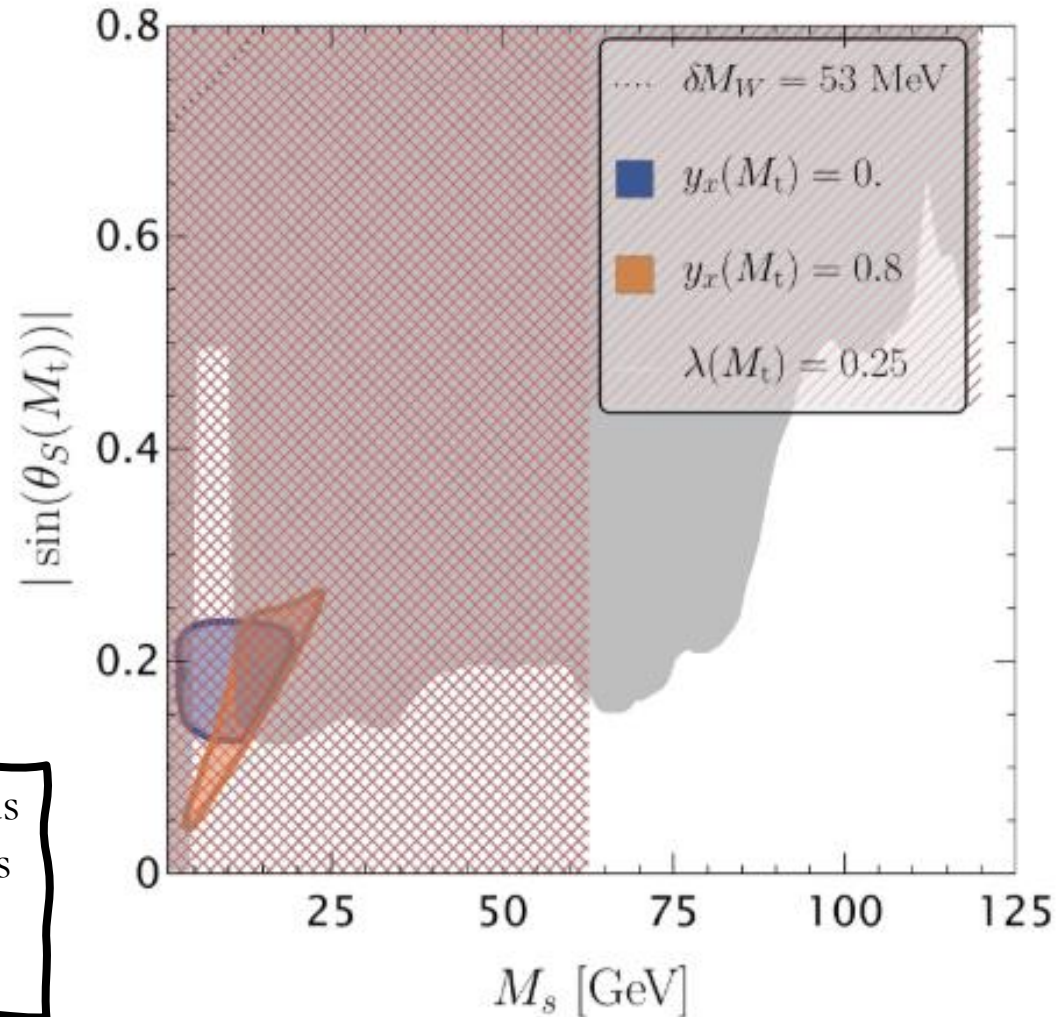
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- While the SM prediction: $M_W^{\text{SM}} = 80.353 \pm 0.009 \text{ GeV}$
- Turns out: $\Delta M_W^{\text{BSM}} > 0$ if $M_S < M_h$ (not so interesting case anymore)
- But $\Delta M_W^{\text{BSM}} < 0$ if $M_S > M_h$: If the CDFII result is verified it kills the scalar singlet extensions!!

But extensive direct searches also exist!



HiggsBounds
HiggsSignals
HiggsTools
software!

What does a new scalar do?

Cannot be explained in the SM:

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Anomalies as hint for new physics:

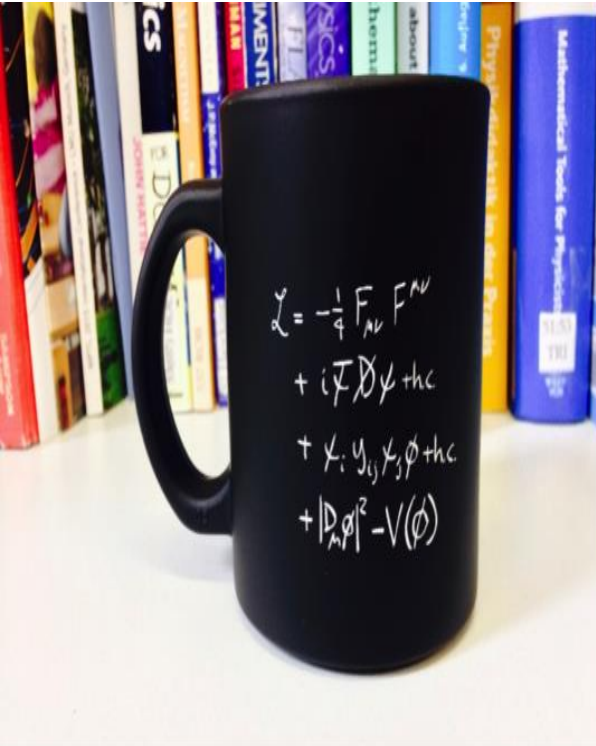
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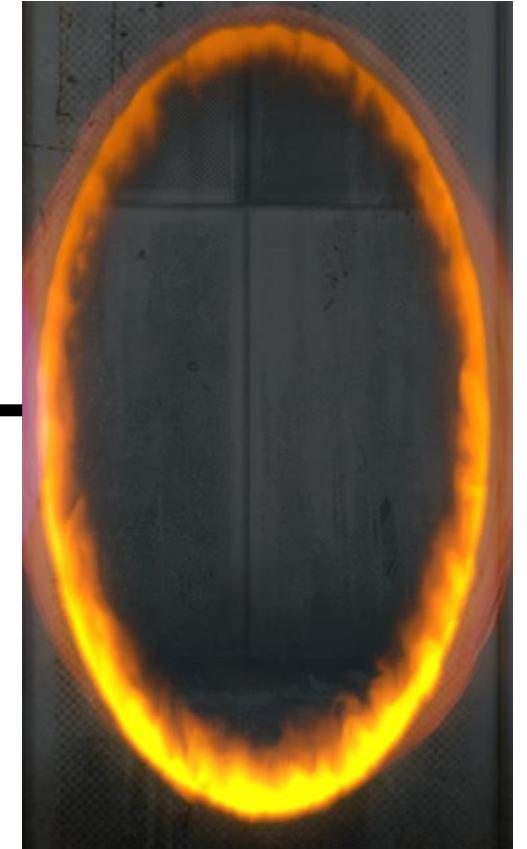
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What else can we have?



Portal to new physics:

- Scalar (0)
- Vector (1)
- Tensor (2)
- Fermions (1/2)



Secluded new physics

For instance: $\lambda |\phi|^2 |\chi|^2$

Neutral gauge bosons: Z' (vector mediators)

Motivation for extra neutral gauge bosons (Z')

- Z' appears after breaking a $U(1)$ gauge group (or higher)
- Fifth fundamental interaction?
- Breaking a larger gauge group with a scalar TeV \rightarrow the unbroken subgroup has $U(1)$ -s (e.g.: GUT, SUSY, string)
- Z' can connect to a secluded sector in the SM
- A discovery would have a lot of consequences: **extended scalar $[\chi]$** (make Z' massive) and **extended fermion sectors $[3 \times \nu_R]$** (cancel gauge anomalies)

Minimal extension of the SM

- SM gauge group + $U(1)_Z$
- Covariant derivative is modified:

$$D_\mu^{U(1)} = -i (y \mathbf{z}) \begin{pmatrix} g_y & -g_z \eta \\ 0 & g_z \end{pmatrix} \begin{pmatrix} B_\mu \\ B'_\mu \end{pmatrix}$$

- $\eta \propto$ kinetic mixing ($F'_{\mu\nu} F^{\mu\nu}$)

- Rotate to mass eigenstates:

$$\begin{pmatrix} B_\mu \\ W_\mu^3 \\ B'_\mu \end{pmatrix} = \begin{pmatrix} c_W & -s_W & 0 \\ s_W & c_W & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_Z & -s_Z \\ 0 & s_Z & c_Z \end{pmatrix} \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix}$$

z charges are defined
at $\eta(\mu_0) = 0$

Z charge assignment

field	$SU(3)_c$	$SU(2)_L$	y	z
Q_L	3	2	$\frac{1}{6}$	$z_q = \frac{1}{3}(z_\phi - z_N)$
U_R	3	1	$\frac{2}{3}$	$z_u = \frac{1}{3}(4z_\phi - z_N)$
D_R	3	1	$-\frac{1}{3}$	$z_d = -\frac{1}{3}(2z_\phi + z_N)$
ℓ_L	1	2	$-\frac{1}{2}$	$z_\ell = z_N - z_\phi$
N_R	1	1	0	z_N
e_R	1	1	-1	$z_e = z_N - 2z_\phi$
ϕ	1	2	$\frac{1}{2}$	z_ϕ
χ	1	1	0	$z_\chi = -1$

- Cancel anomalies
+ Yukawa mass terms
= Fix all, but two Z charges
- χ : new singlet scalar
- N : right handed (sterile) neutrinos
- Choose z_N and z_ϕ to be free

Z charge remarks

- 2 free Z charges (due to anomaly cancellation + Yukawa masses + normalization)
- $Z_N \sim$ neutrino mass generation mechanism: tree level Majorana mass term is allowed if $Z_\chi + 2Z_N = 0$ ($\sim \chi \bar{\nu}_R \nu_R^c$)
- Z_ϕ appears only in the combination: $Z_\phi - \frac{\eta}{2} \rightarrow$ use this one

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- In the branching ratios of Z' **the combination** appears:

$$\mathbf{Z} = \frac{z_\phi - \eta/2}{z_N} \text{ e.g.: } \text{Br}(Z' \rightarrow \text{inv.}) = \frac{(3+n_N)}{(3+n_N)+2(1-2c_W^2 \mathbf{Z})^2} \text{ for } M_{Z'} < m_\mu$$

- B-L model: $\mathbf{Z} = \mathbf{0}$

Other free parameters:

- $M_{Z'}$ (or rather $\xi = M_{Z'}/M_Z$ to treat diff. mass scales)
- Either the mixing angle s_Z or the new gauge coupling g_Z :

$$-s_Z c_Z \frac{(1-\xi^2)}{\rho} = \frac{2}{\sqrt{g_Y^2 + g_L^2}} g_Z \left(z_\phi - \frac{\eta}{2} \right)$$

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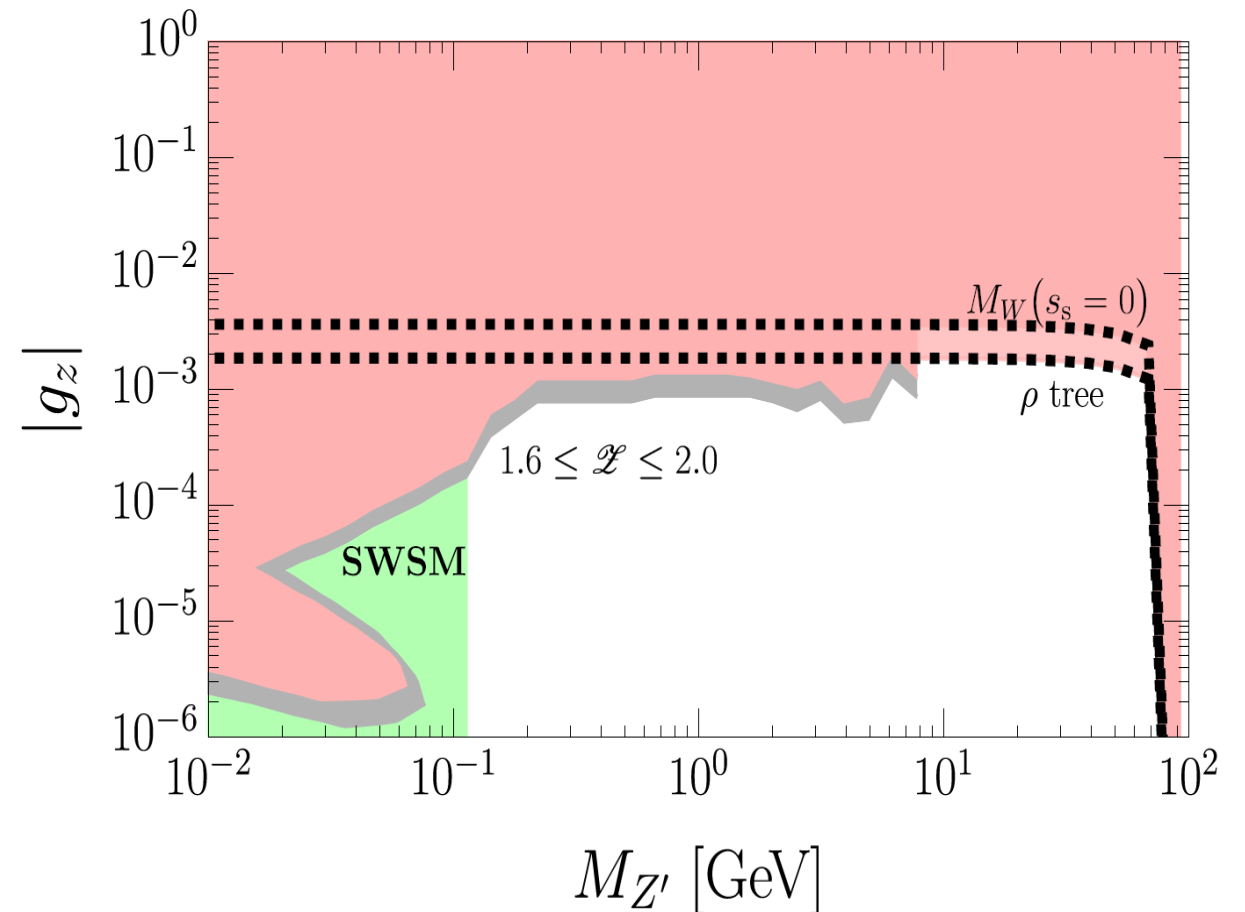
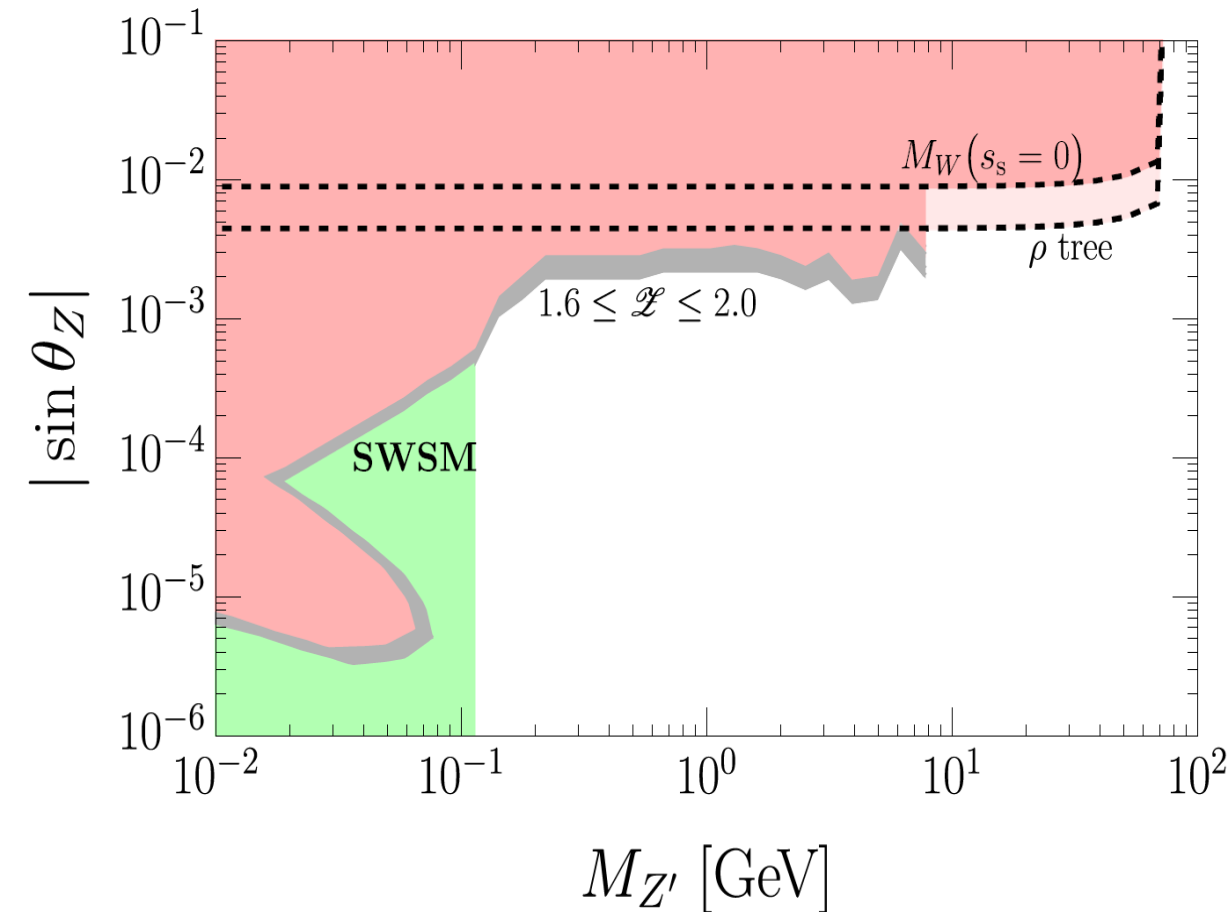
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This is BSM only!

- From global fits one has: $\rho = 1.00038 \pm 0.00020$
- The tree level model prediction is:

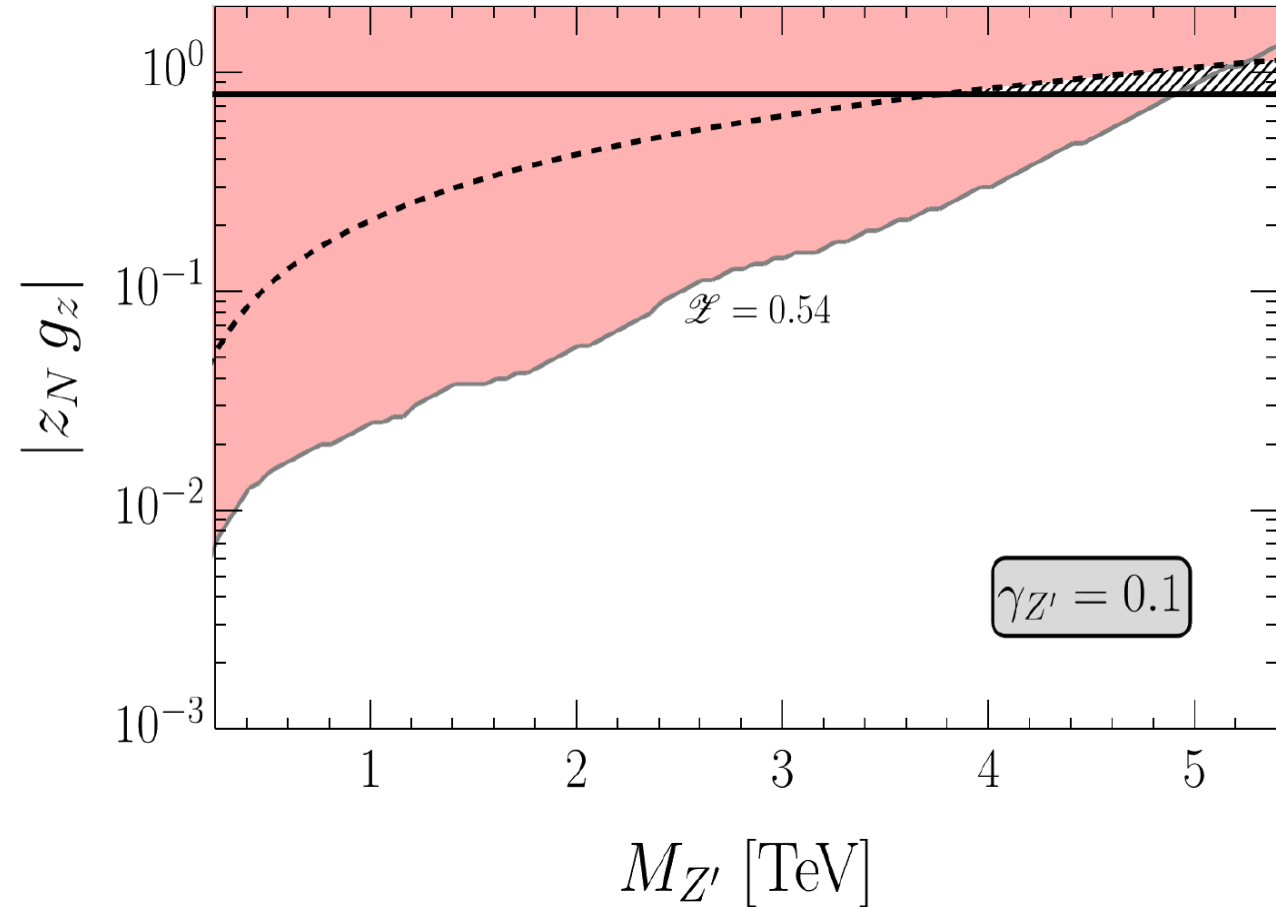
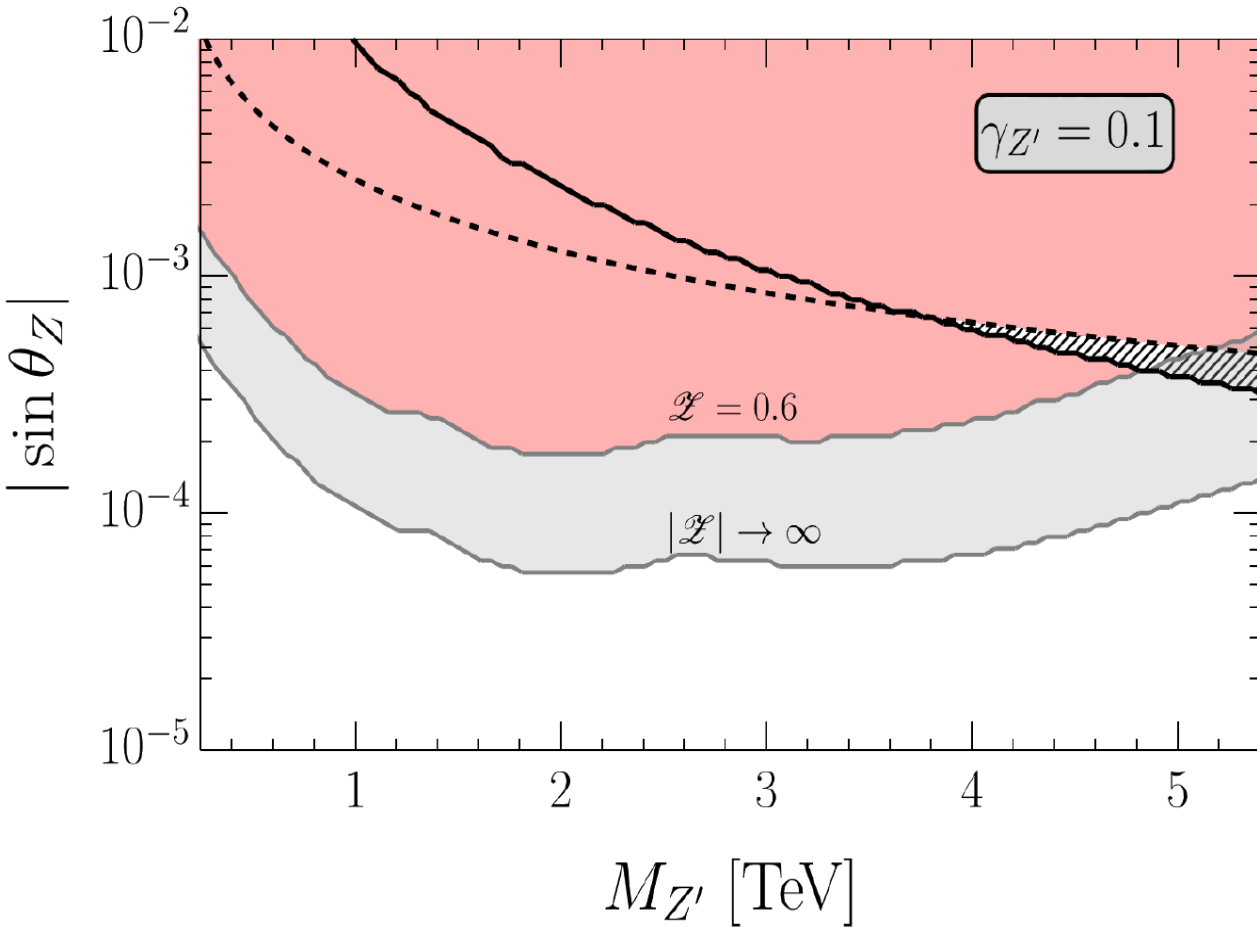
$$\rho = \frac{M_W^2}{M_Z^2 c_W^2} = 1 + (\xi^2 - 1) s_Z^2$$

Light Z' : the superweak model



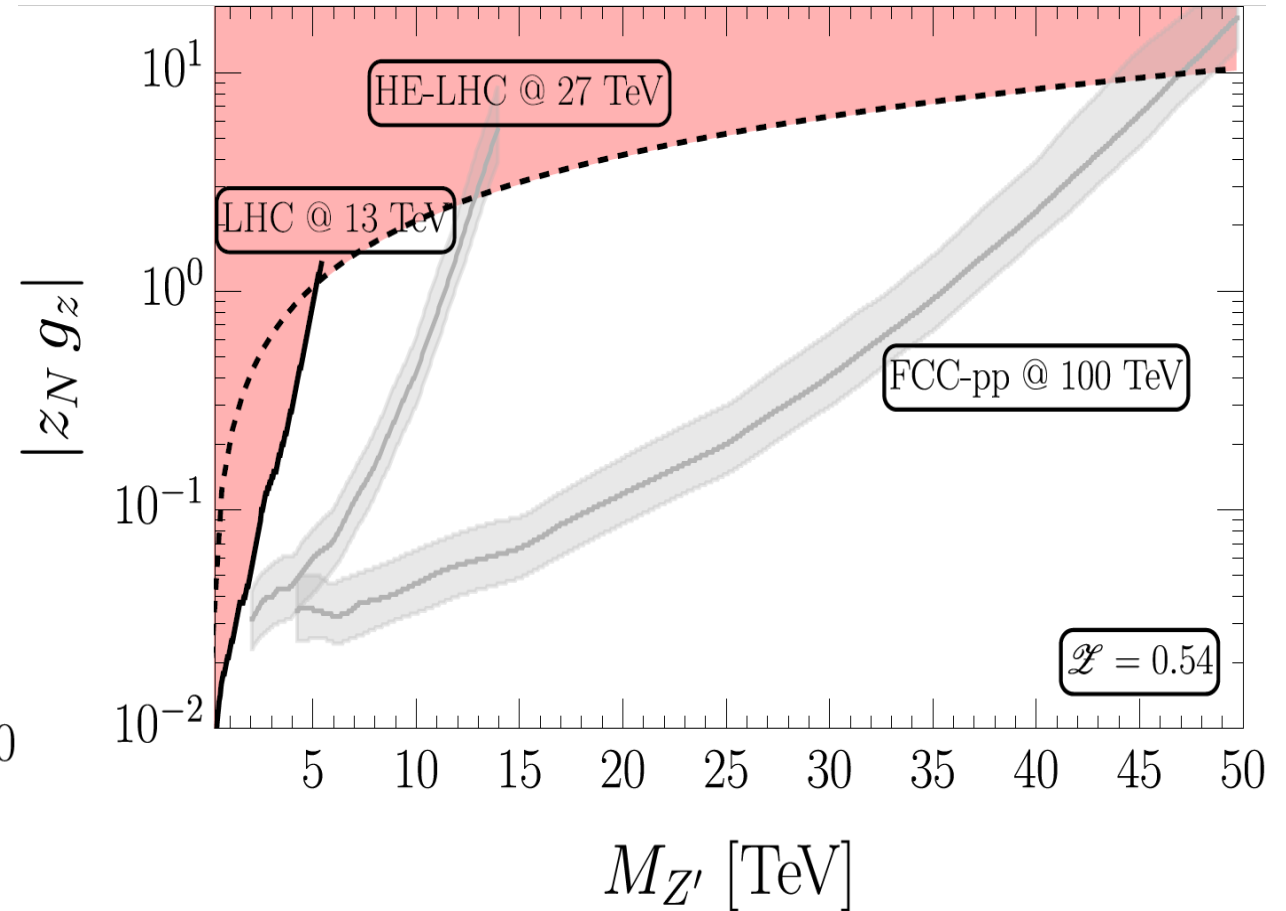
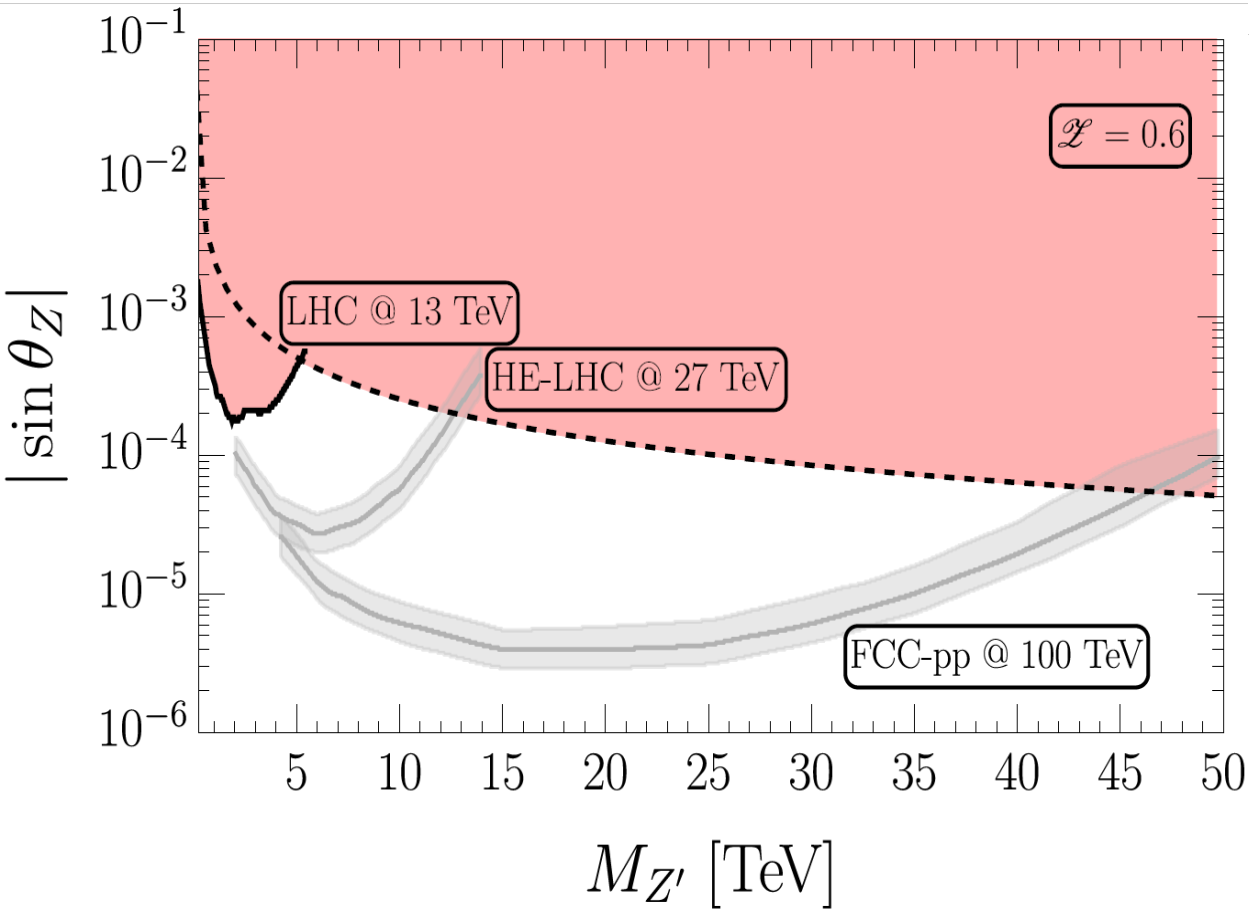
Uncertainty due to sterile neutrinos + running of η : thickness of gray line

Heavy Z' : almost model independent!



There is a **Z** value corresponding to a *loosest* bound!

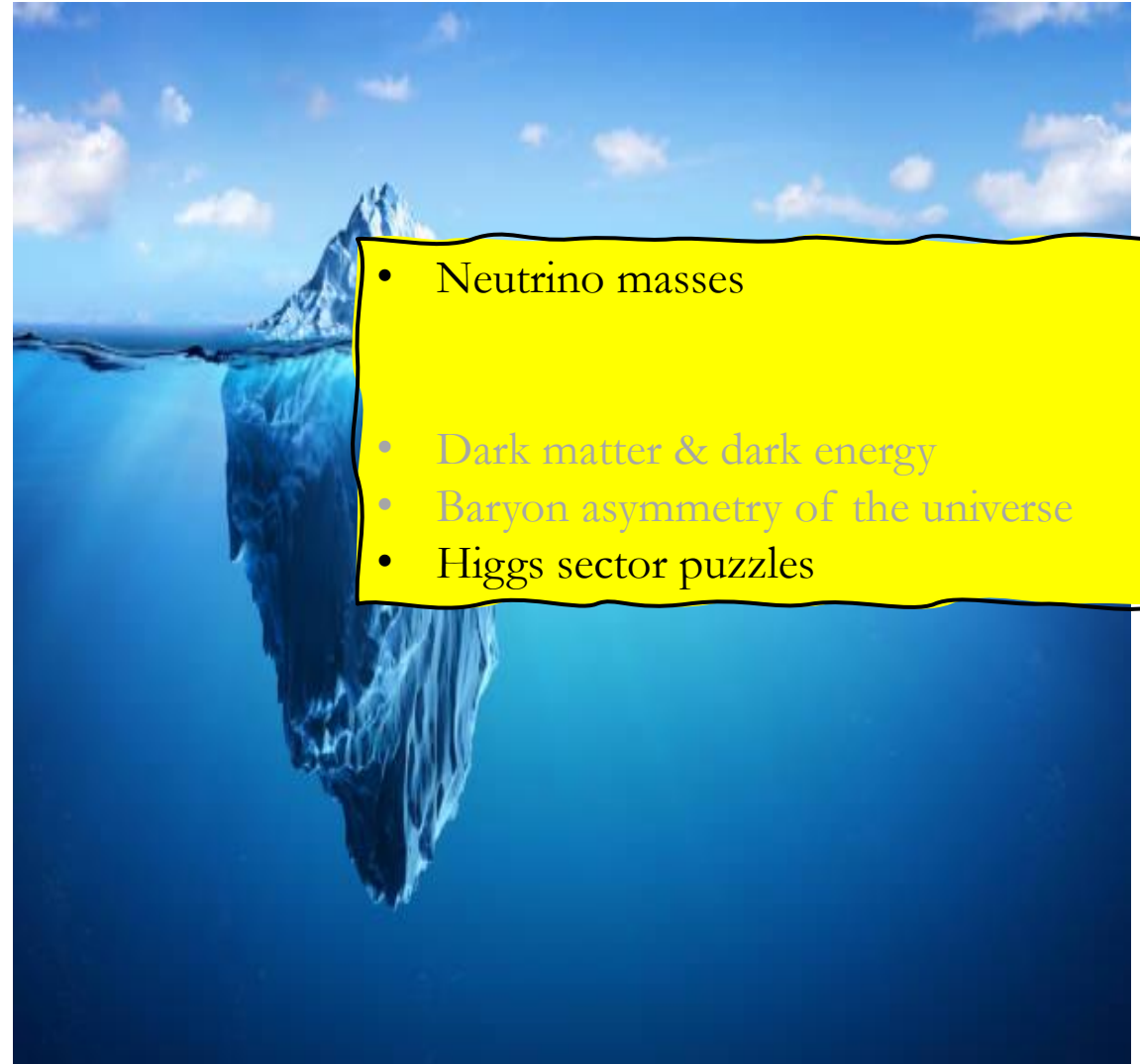
Projections for future colliders



...using detector simulations for the HE-LHC and FCC-hh

Outlook

- BSM is a rich topic
- Particle physics explanation for most of the unexplained phenomena
- But the clues are hiding well
- Explore the possible new particles and their consequences to know what to expect



- Neutrino masses
- Dark matter & dark energy
- Baryon asymmetry of the universe
- Higgs sector puzzles