

Suppressing photon detection errors in nondeterministic state preparation

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Quantum advantage using photons

The Quantum Information Group of USTC in Hefei (led by Jian-Wei Pan) demonstrated an advantage over classical computation in 2020, using the Gaussian Boson Sampling (GBS) scheme¹.

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However, GBS only uses linear optical quantum gates \implies GBS is **non-universal!**

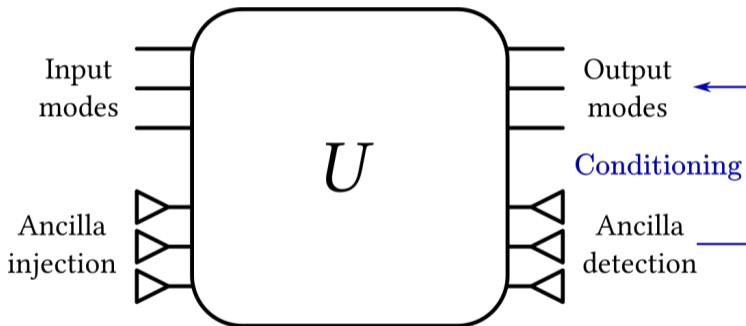
Difficult to implement non-linear (e.g., Kerr) gates in a photonic circuit \implies We try to **avoid non-linear gates**.

Idea: include ancilla detections and postselection!

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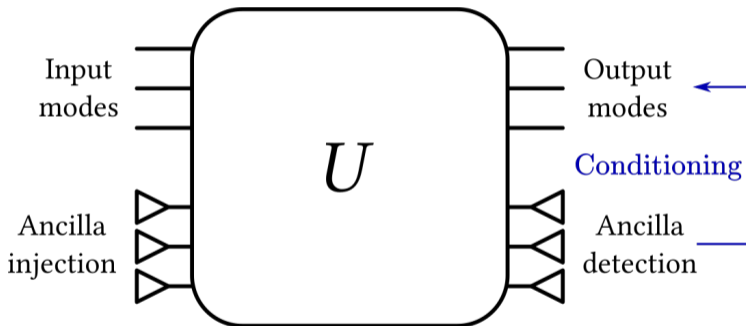
Non-deterministic gates

Postselection is conditioning the output on the measurement result of ancilla modes.



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In our case, we use **particle number resolving detectors** (PNRDs).

Example: Nonlinear phaseshift (NS) gate

Goal: Implement the following gate²:

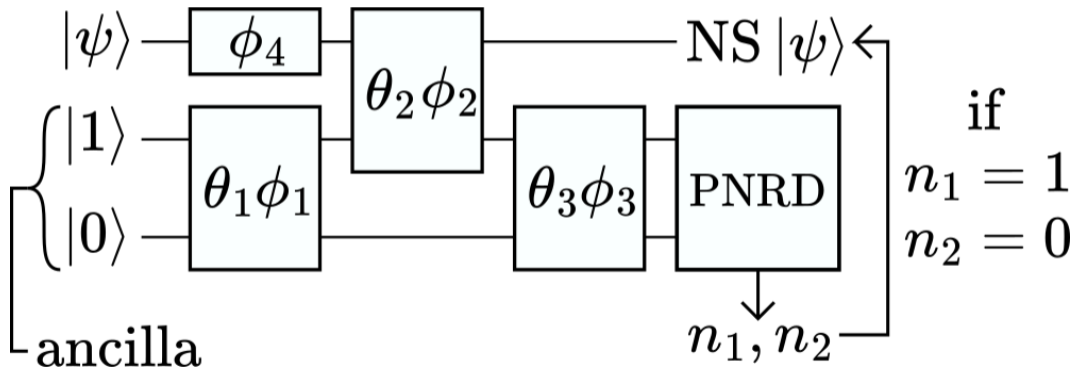
$$\text{NS} : \alpha_0 |0\rangle + \alpha_1 |1\rangle + \alpha_2 |2\rangle \mapsto \alpha_0 |0\rangle + \alpha_1 |1\rangle - \alpha_2 |2\rangle. \quad (1)$$

²E. Knill, R. Laflamme, G. J. Milburn, *A scheme for efficient quantum computation with linear optics*, Nature (2001)

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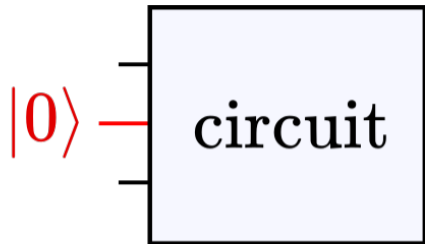
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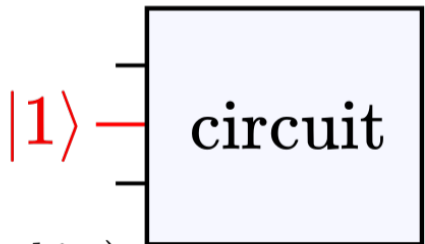
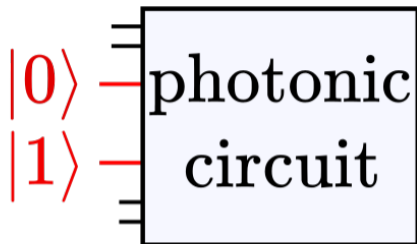


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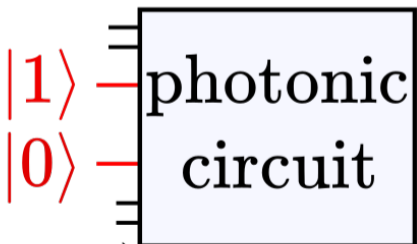
Dual-rail encoding



\equiv



\equiv



(qubits)

(photons)

Conditional sign flip gate

Goal: Implement the following transformation³:

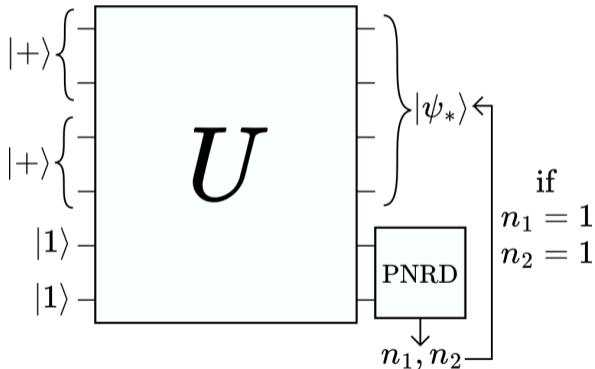
$$\text{CZ} : |++\rangle_{\text{qubit}} \mapsto |\psi_*\rangle = \frac{1}{2} (|0, 0\rangle + |1, 0\rangle + |0, 1\rangle - |1, 1\rangle)_{\text{qubit}} \quad (2)$$

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We can implement this by using a specific interferometer denoted by U !

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KLM protocol

The **KLM protocol** combines postselection and dual-rail encoding (+ gate teleportation).

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Problem: PNRDs are **biased** in practice \implies incorrect state may be postselected after faulty postselection!

Detector efficiency matrix

The imperfections in the PNRD can be characterized by the **detector efficiency matrix**:

$$P_{m,n} := \mathbb{P}_{\text{readout}}(m|n). \quad (3)$$

⁴V. Resta et al., *Gigahertz Detection Rates and Dynamic Photon-Number Resolution with Superconducting Nanowire Arrays*. Nano Lett. (2023)

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An example⁴:

$$P = \begin{pmatrix} 1.0 & 0.1050 & 0.0110 & 0.0012 & 0.001 \\ 0.0 & 0.8950 & 0.2452 & 0.0513 & 0.0097 \\ 0.0 & 0.0 & 0.7438 & 0.3770 & 0.1304 \\ 0.0 & 0.0 & 0.0 & 0.5706 & 0.4585 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.4013 \end{pmatrix}. \quad (4)$$

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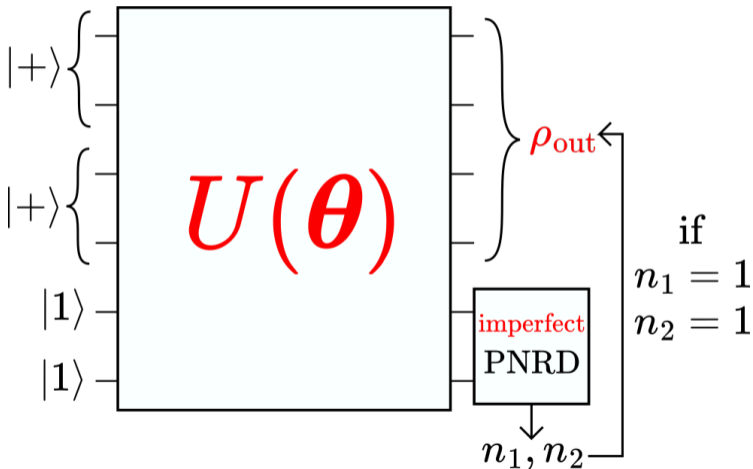
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This will introduce an error in the nondeterministic gates!

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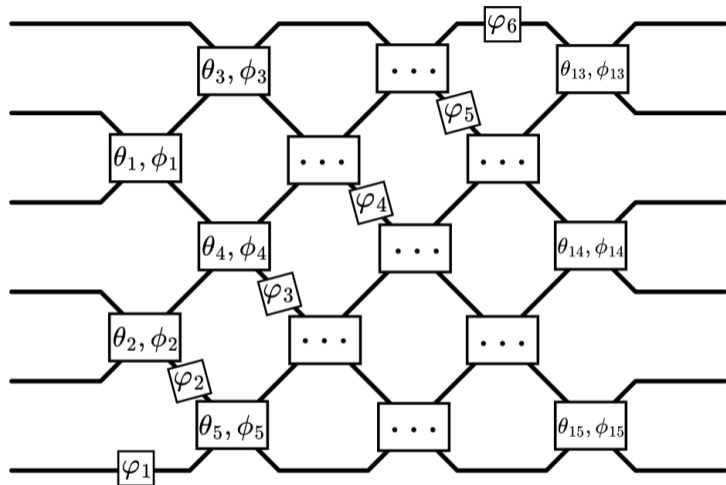
Idea: adjust interferometer!

Changing the θ angles in the interferometer can increase the output state fidelity or the success probability of nondeterministic gates with imperfect PNRDs!



Parametrizing the interferometer⁵

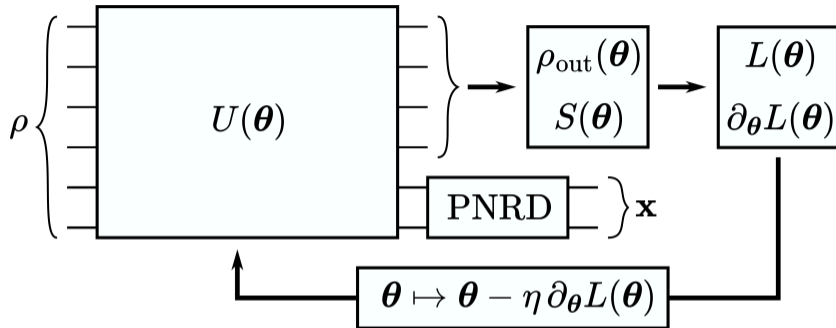
$$U(\boldsymbol{\theta}) \equiv$$



$$(\boldsymbol{\theta} = \{\theta_i, \phi_i, \varphi_i\}_i)$$

⁵W. R. Clements et al., *An Optimal Design for Universal Multiport Interferometers*, Optica (2016), [arXiv:1603.08788](https://arxiv.org/abs/1603.08788)

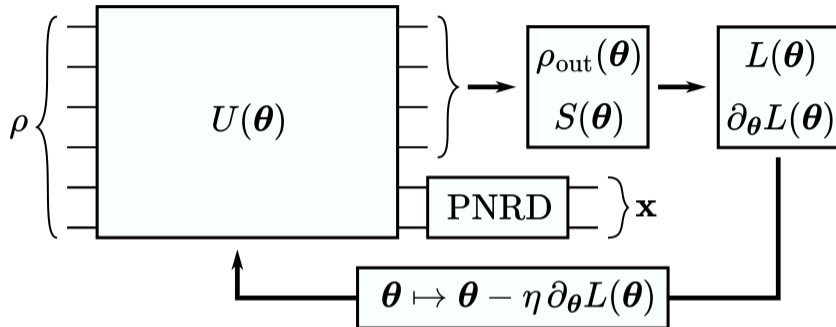
Gradient-based optimization



$$\rho_{\text{out}}(\theta) := \frac{1}{S(\theta)} \sum_{\mathbf{n}} \mathbb{P}(\mathbf{x}|\mathbf{n}) \text{tr}_2 \left\{ U(\theta) \rho U^{\dagger}(\theta) (I \otimes |\mathbf{n}\rangle \langle \mathbf{n}|) \right\} \quad \text{(Final state)}$$

$$S(\theta) := \sum_{\mathbf{n}} \mathbb{P}(\mathbf{x}|\mathbf{n}) \text{tr} \left\{ U(\theta) \rho U^{\dagger}(\theta) (I \otimes |\mathbf{n}\rangle \langle \mathbf{n}|) \right\} \quad \text{(Success rate)}$$

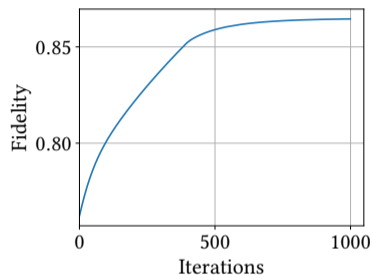
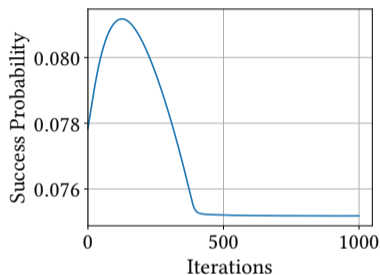
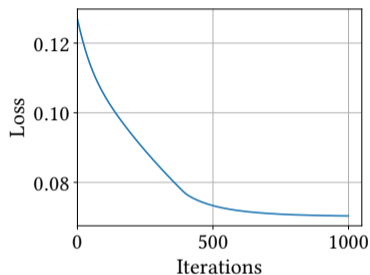
Gradient-based optimization



$$L(\theta) := 1 - \sqrt{\langle \psi^* | \rho_{\text{out}}(\theta) | \psi^* \rangle} + \alpha \text{softplus}_{\beta}(S^* - S(\theta)) \quad (S^* = \text{Target success rate})$$

$$\text{softplus}_{\beta}(x) := \frac{1}{\beta} \log(\exp(\beta x) + 1) \quad (5)$$

Optimization of conditional phase shift gate with imperfect PNRDs⁷

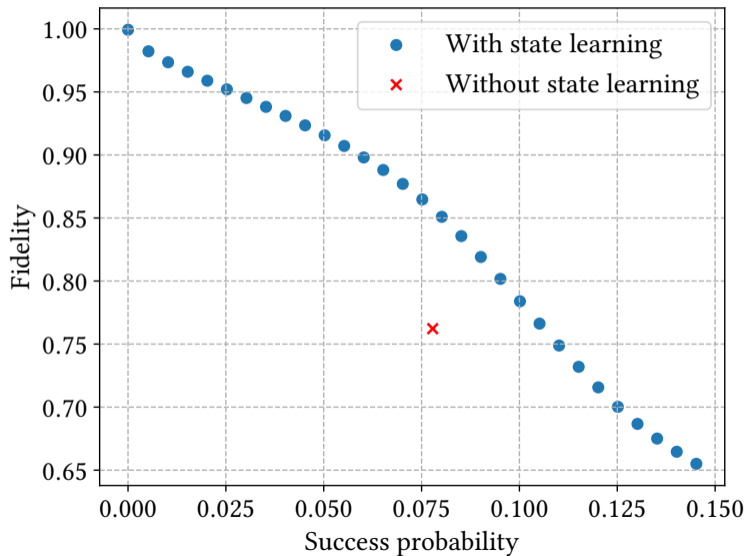


The simulations were executed using Piquasso⁶.

⁶ZK et al., *Piquasso: A Photonic Quantum Computer Simulation Software Platform*, [arXiv:2403.04006](https://arxiv.org/abs/2403.04006) (2024)

⁷In this example, with target success rate $S^* = 0.075$, code available at <https://github.com/Budapest-Quantum-Computing-Group/supressing-loqc-pd-errors>

Tradeoff between fidelity and success rate



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