



# Jet propagation within a Linearized Boltzmann Transport Model

LuoTan

*Central China Normal University  
Institute of Particle Physics*



*In collaboration with Yayun He, Xin-Nian Wang and Yan Zhu*

$$p_1 \cdot \partial f_1(p_1) = - \int dp_2 dp_3 dp_4 (f_1 f_2 - f_3 f_4) |M_{12 \rightarrow 34}|^2$$

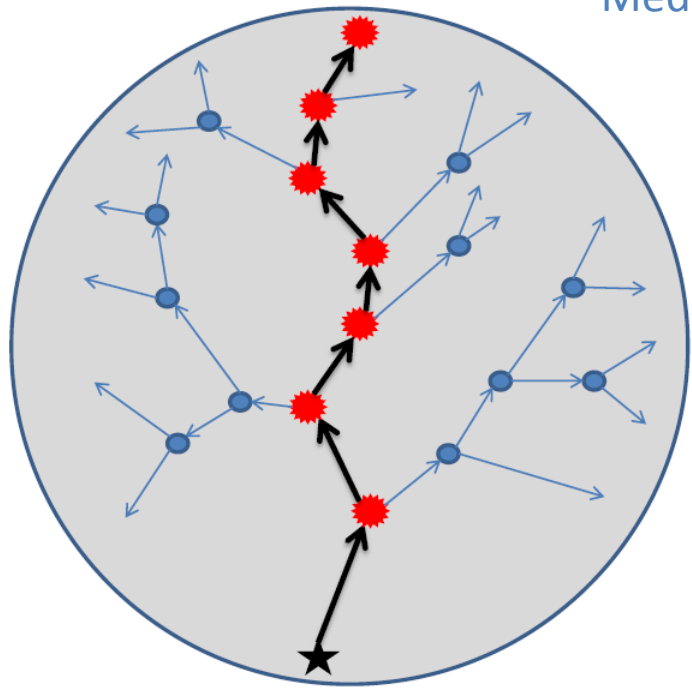
$$\times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4)$$

$$dp_i \equiv \frac{d^3 p_i}{2E_i (2\pi)^3}, |M_{12 \rightarrow 34}|^2 = Cg^2 (s^2 + u^2) / (t + \underline{\mu}^2)^2$$

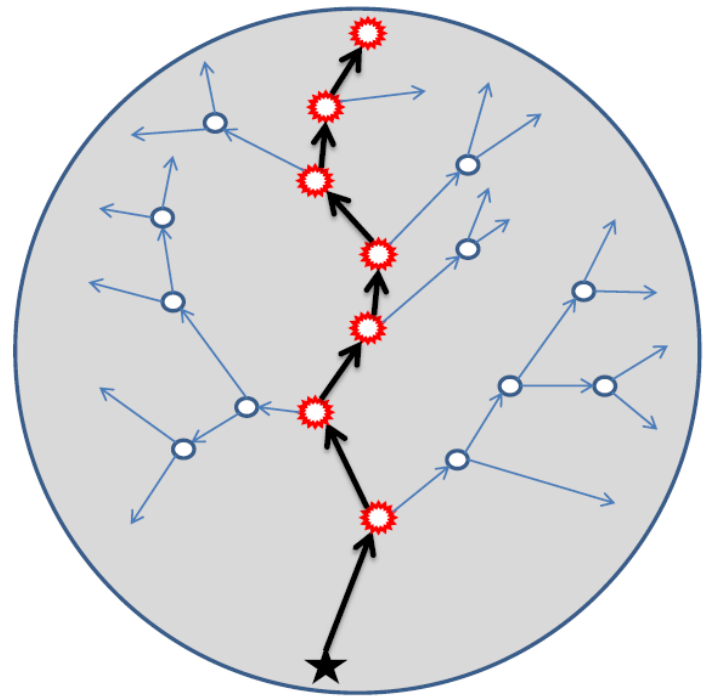
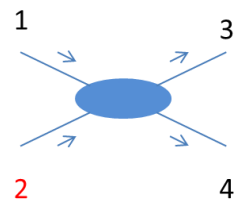
$$f_i = 1 / (e_i^{p_i \cdot u / T} \pm 1) (i = 2, 4), f_i = (2\pi)^3 \delta^3(\vec{p} - \vec{p}_i) \delta^3(\vec{x} - \vec{x}_i) (i = 1, 3)$$

-  Leading parton-----thermal parton scattering
-  recoiled parton-----thermal parton scattering

Medium Excitation



Negative particle  
the particle hole



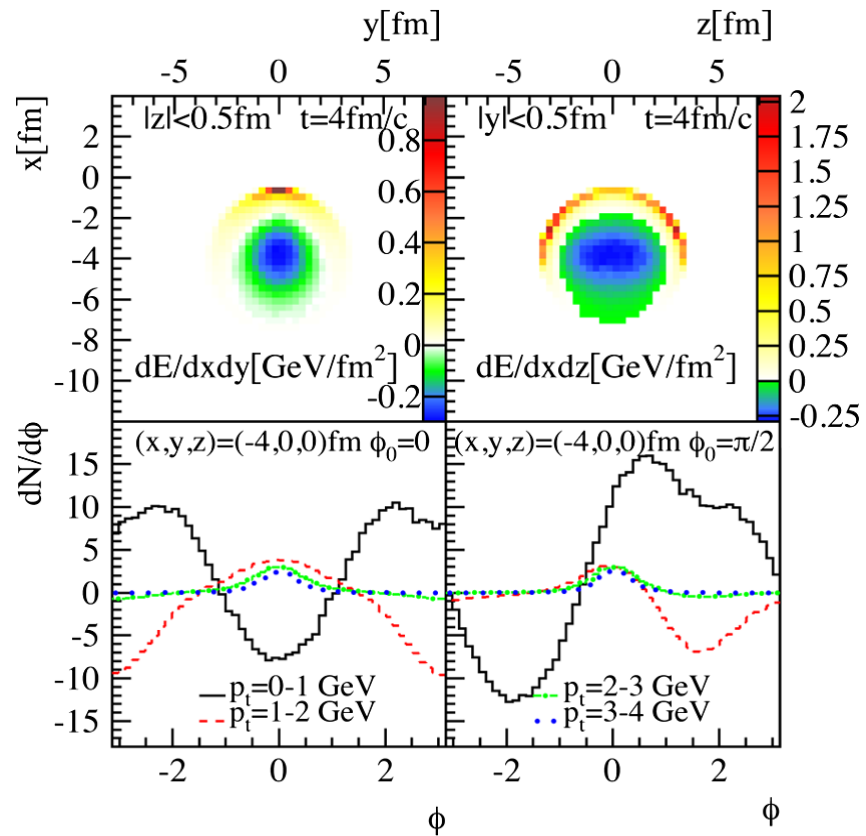
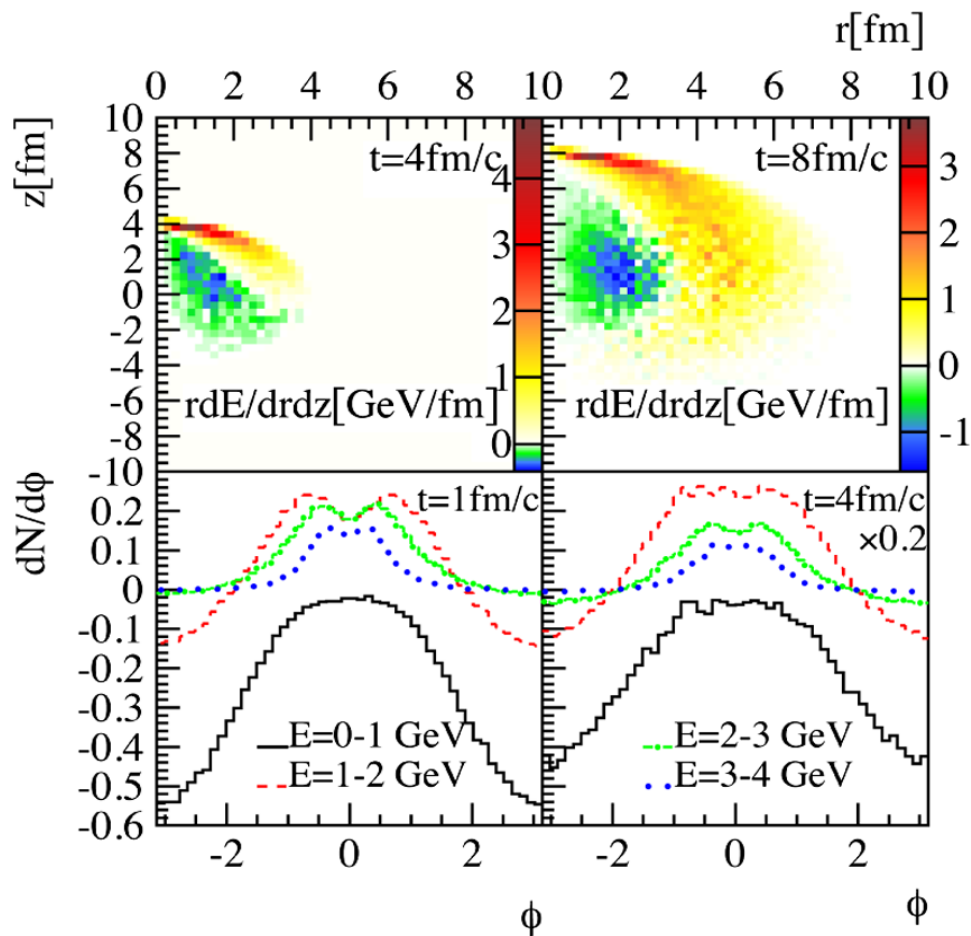
Linearized Boltzmann jet transport neglect scatterings between recoiled medium partons. It's a good approximation when the jet induced medium excitation  $\delta f \ll f$ .

Deflection of different phase space. One has to subtract the 4-momentum of negative particle when combine it to jet.

# Jet induced Mach Cone in HIC

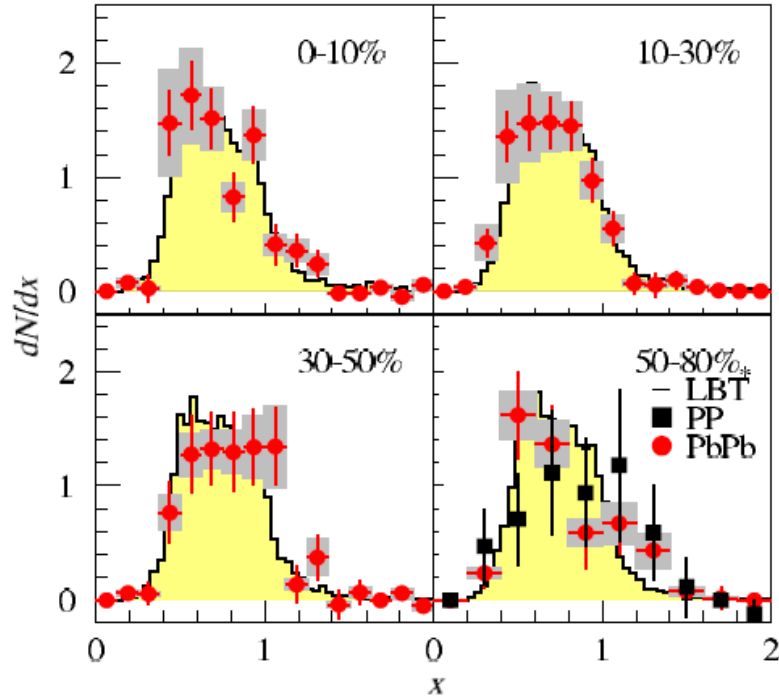
I. No conic distribution of the final partons in an uniform medium.

II. Double-peak correlation of the final partons in 3+1D medium .



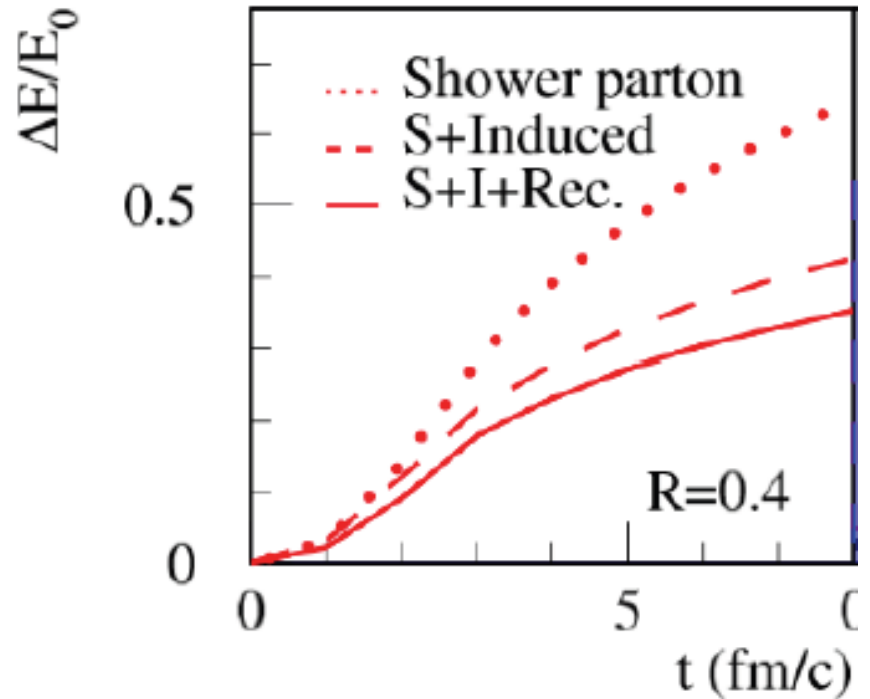
Hanlin Li, Fuming Liu, Guo-liang Ma, Xin-Nian Wang, Yan Zhu

**Phys. Rev. Lett. 106, 012301**



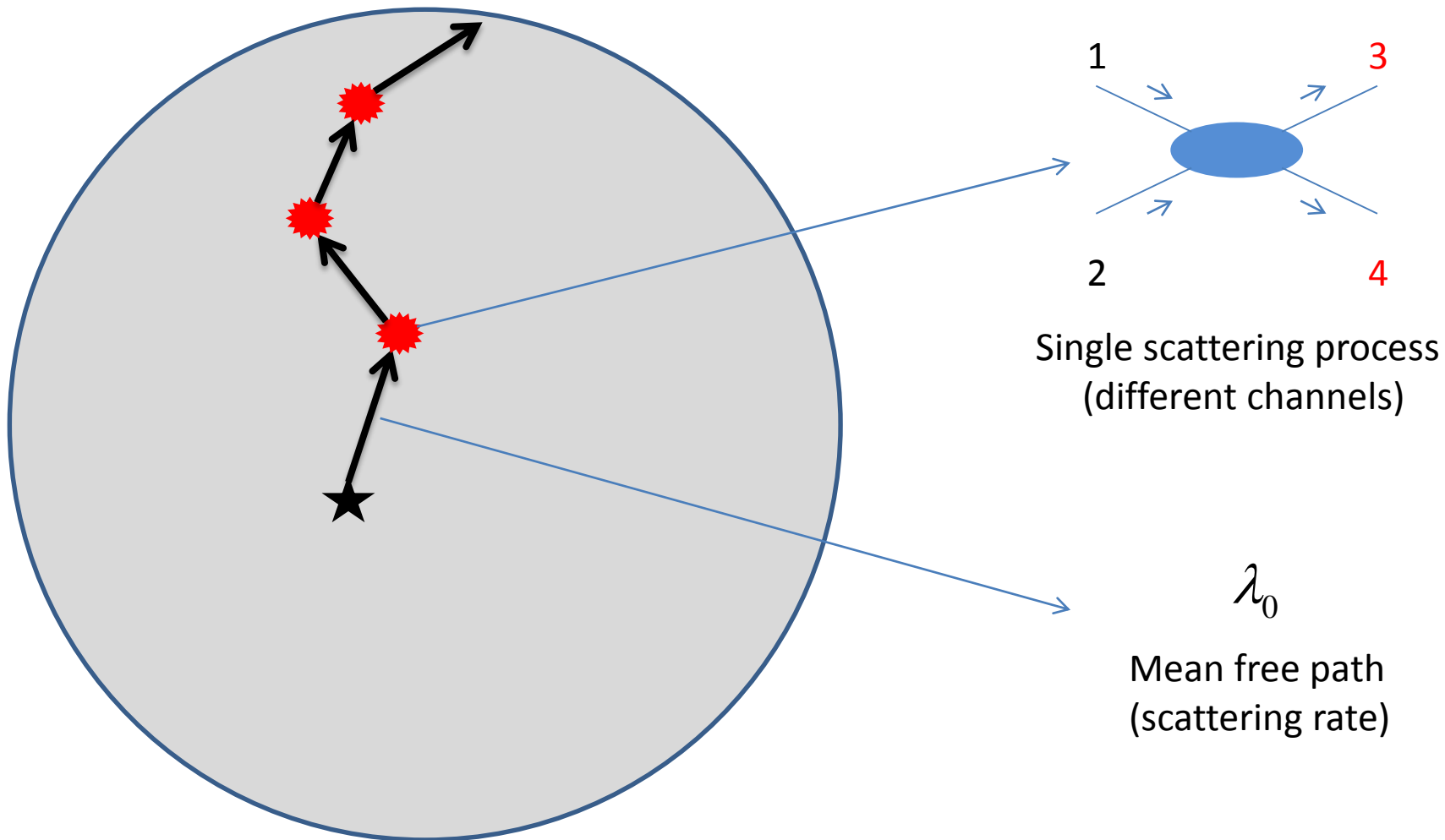
*Radiation process is included*

**Jet energy loss**



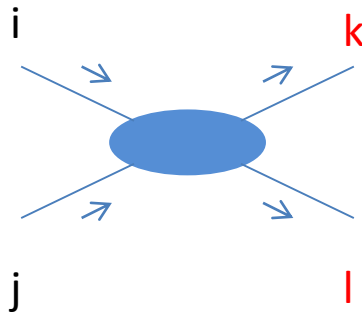
Simulation results for gamma-jet correlation describe the experiment data successfully.

# The Monte-Carlo Simulation : a hard parton traversing an uniform medium



a static, homogeneous and infinite QGP

## Single scattering



$$i, j = g, u, d, s, \bar{u}, \bar{d}, \bar{s}$$

Jussi Auvinen, Kari J. Eskola, Thorsten Renk

Phys.Rev. C82 024906

- Scattering rate for a process  $ij \rightarrow kl$  in the local rest frame of the fluid

$$\Gamma_{ij \rightarrow kl} = \frac{1}{2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \int \frac{d^3 p_3}{(2\pi)^3 2E_3} \int \frac{d^3 p_4}{(2\pi)^3 2E_4} \times f_j(p_2 \cdot u, T) \\ \times |M|_{ij \rightarrow kl}^2(s, t, u) \times S_2(s, t, u) \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4)$$

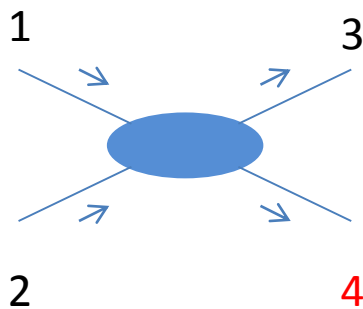
- The regularization

$$S_2(s, t, u) = \theta(s \geq 2\mu_D^2) \theta(-s + \mu_D^2 \leq t \leq -\mu_D^2) \quad \mu_D^2 = \left(\frac{3}{2}\right) 4\pi\alpha_s T^2$$

- The mean free path

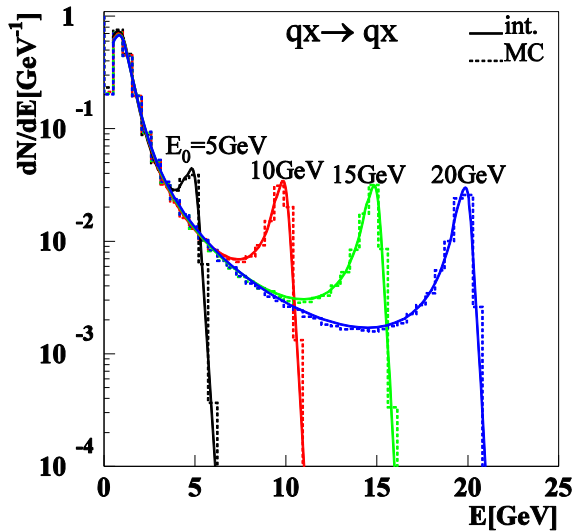
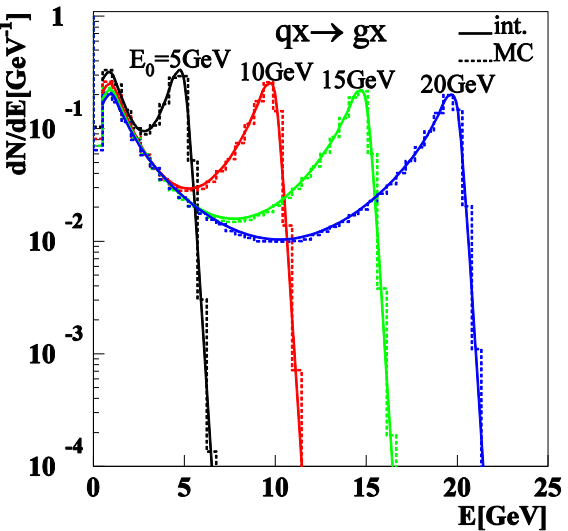
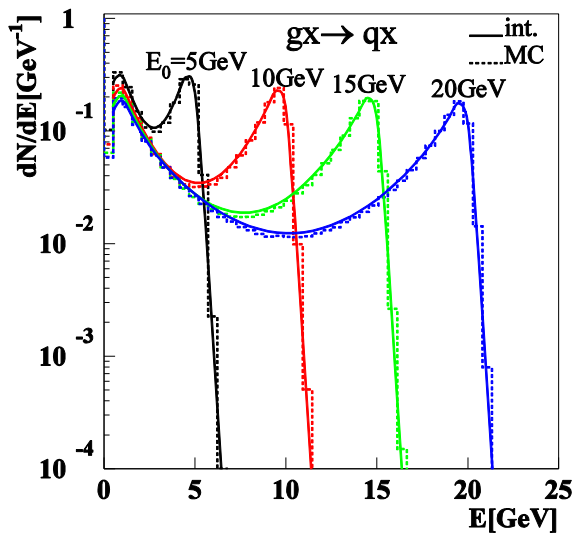
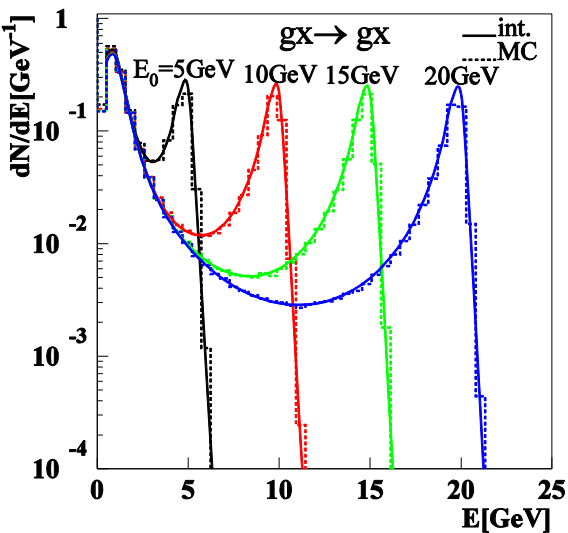
$$\Gamma_i = \sum_{j, (kl)} \Gamma_{ij \rightarrow kl} = 1 / \lambda_0 \quad P(\Delta t) = 1 - e^{-\Gamma_i \Delta t} \quad P(ij \rightarrow kl) = \frac{\Gamma_{ij \rightarrow kl}}{\Gamma_i}$$

# Single scattering



the selection of the jet parton

T=0.2GeV



$$gg \rightarrow gg$$

$$gg \rightarrow q\bar{q}$$

$$gq \rightarrow gq + g\bar{q} \rightarrow g\bar{q}$$

$$q_i g \rightarrow q_i g$$

$$q_i q_j \rightarrow q_i q_j$$

$$q_i q_i \rightarrow q_i q_i$$

$$q_i q_i \rightarrow q_j q_j$$

$$q_i q_i \rightarrow q_i q_i$$

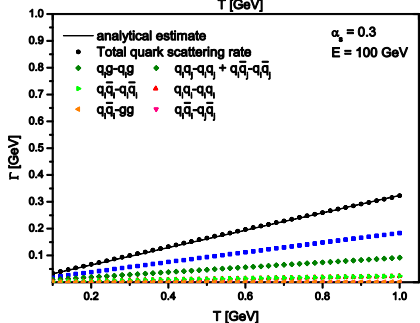
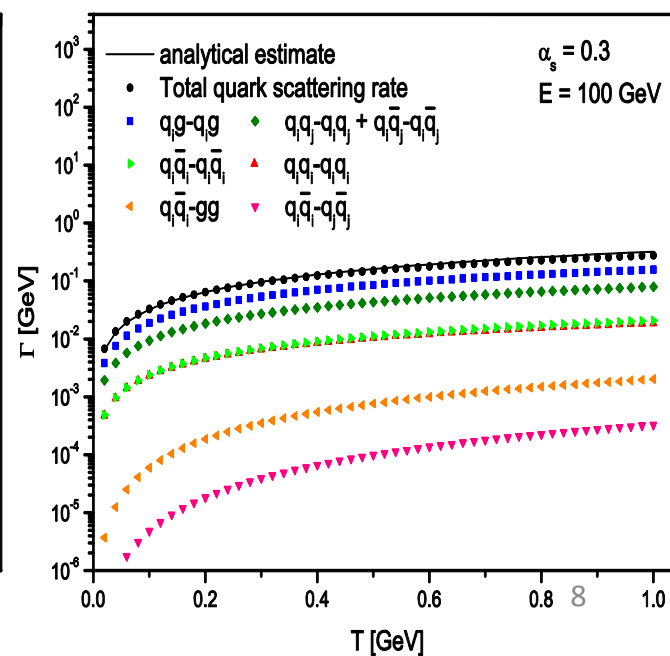
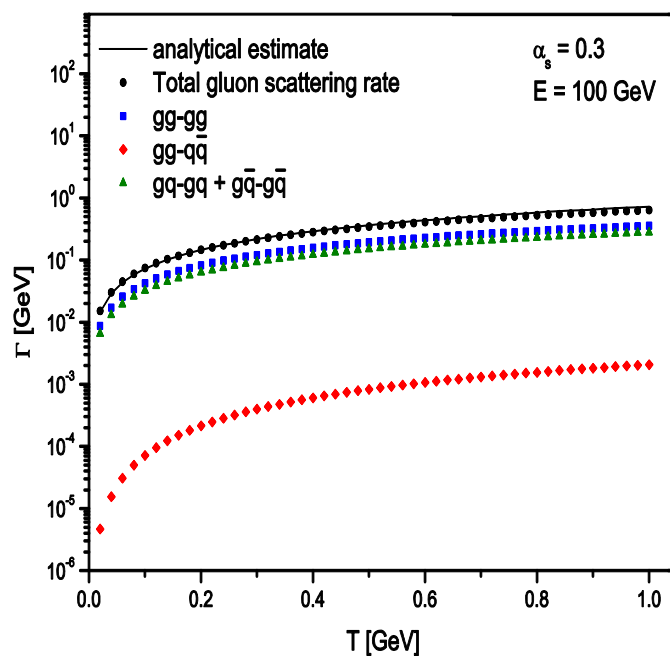
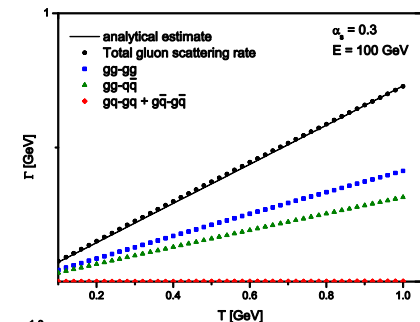
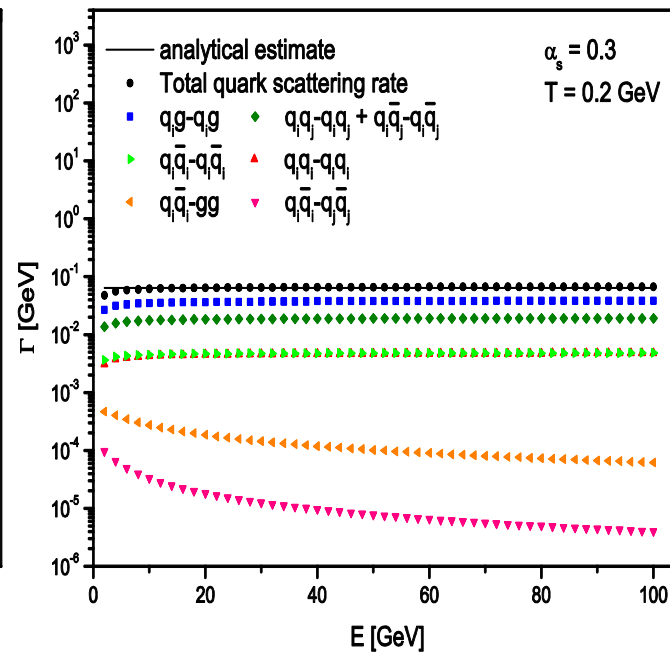
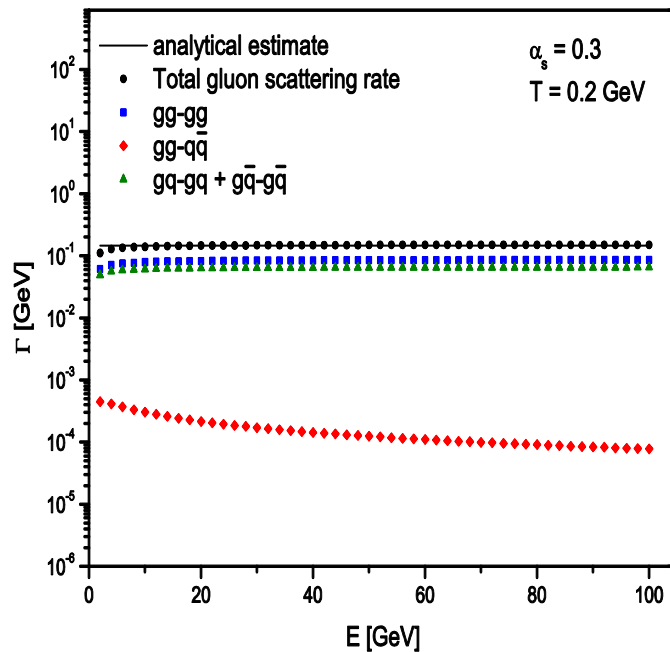
$$q_i q_i \rightarrow gg$$

# Scattering rate

Contribution of different processes on scattering rate as functions of energy and temperature

gluon

quark





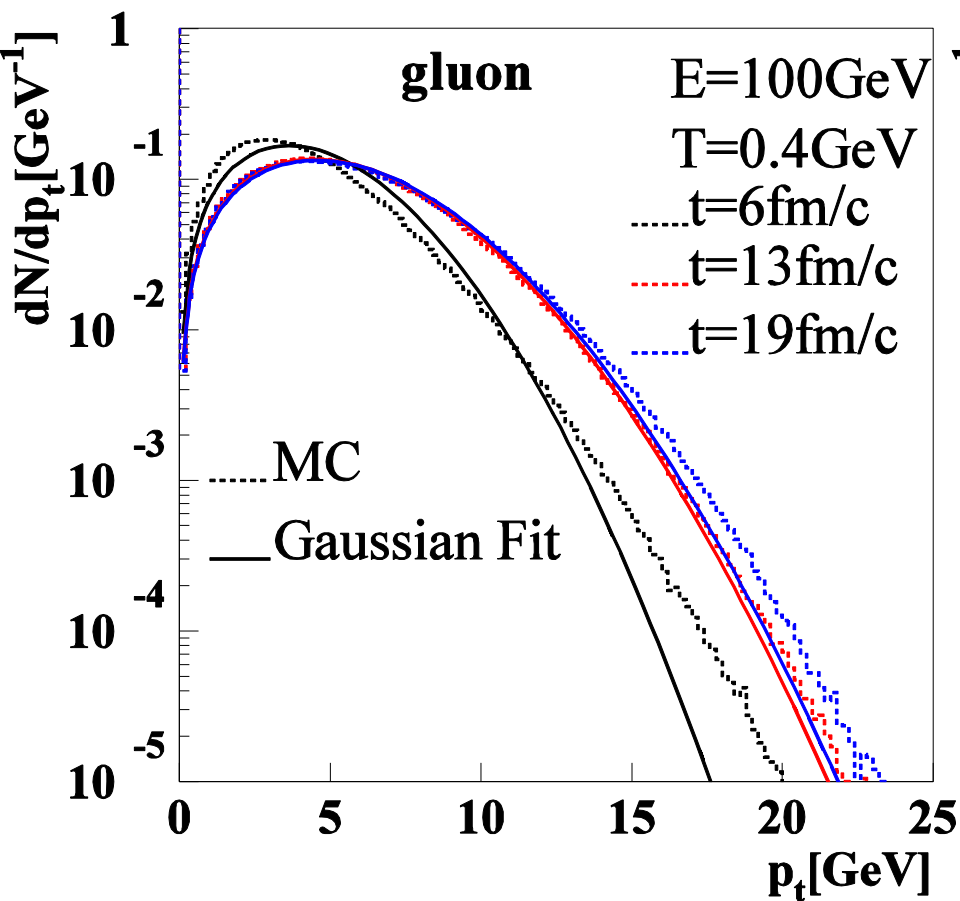
## Multiple scattering

F. D'Eramo, M. Lekaveckas, Hong Liu and K. Rajagopal  
arXiv:1211.1922

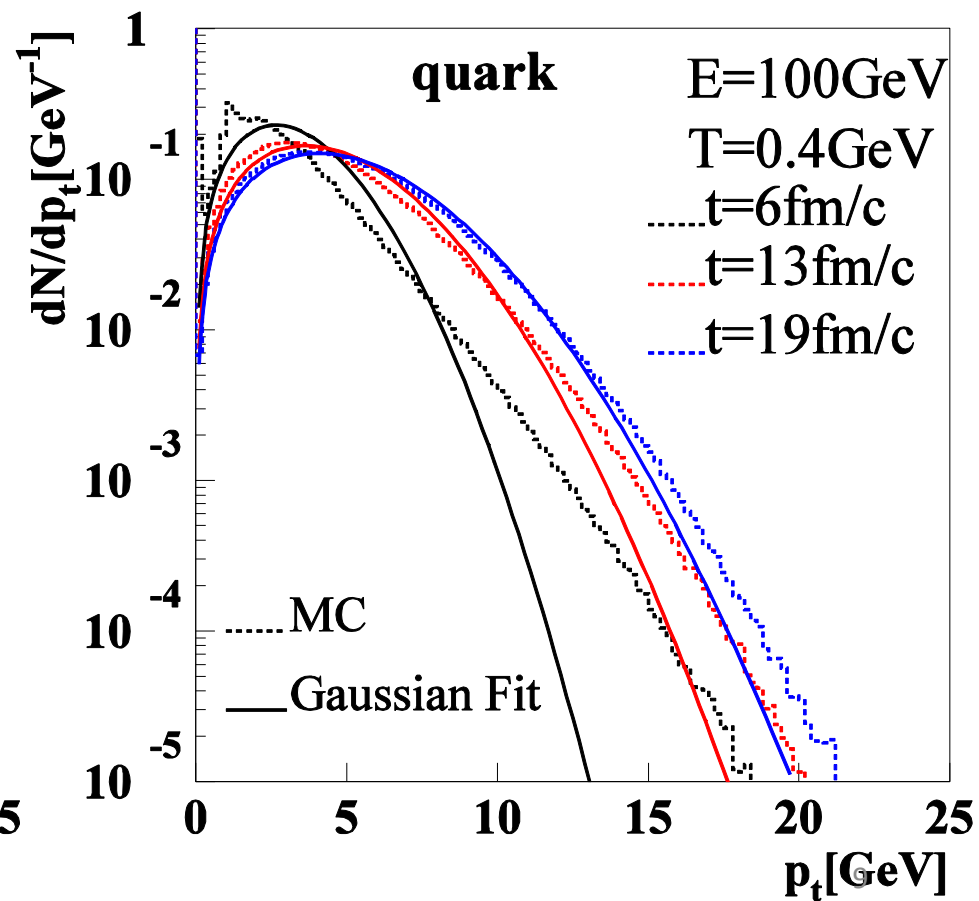
$dn/dp_t$  as a function of time

Gaussian fit 
$$\frac{dn}{dp_t} = \frac{2p_t}{\langle p_t^2 \rangle} e^{-\frac{p_t^2}{\langle p_t^2 \rangle}}$$

Pt broadening

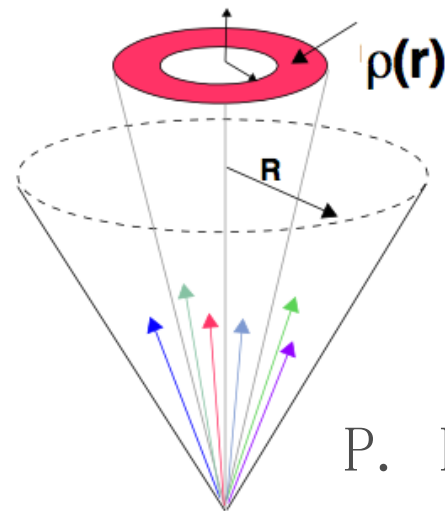


The  $\langle p_t^2 \rangle$  comes from the MC simulation



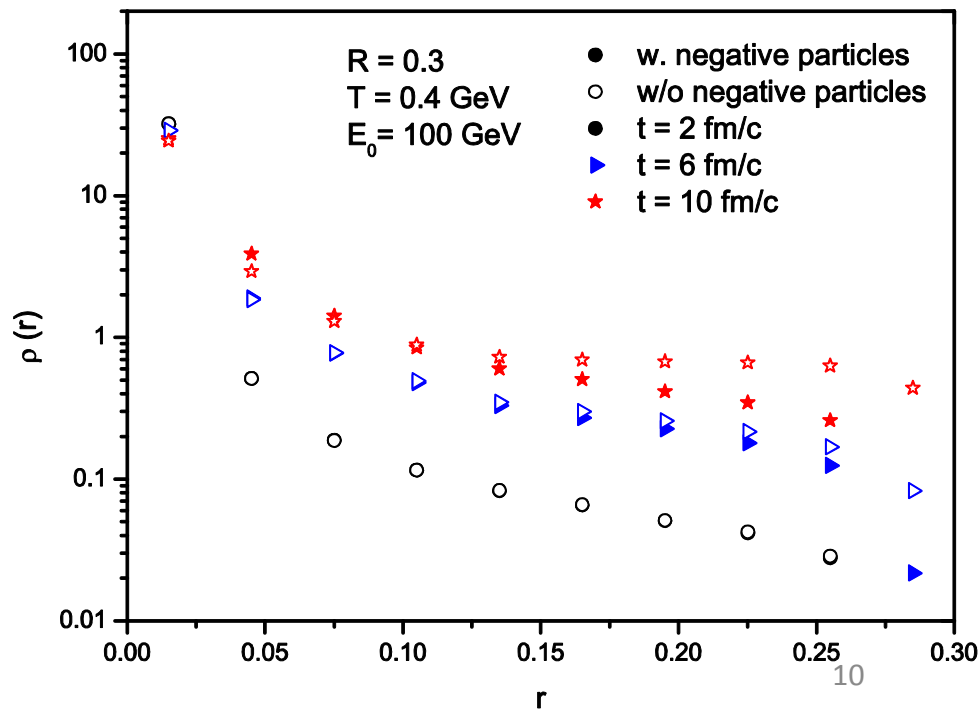
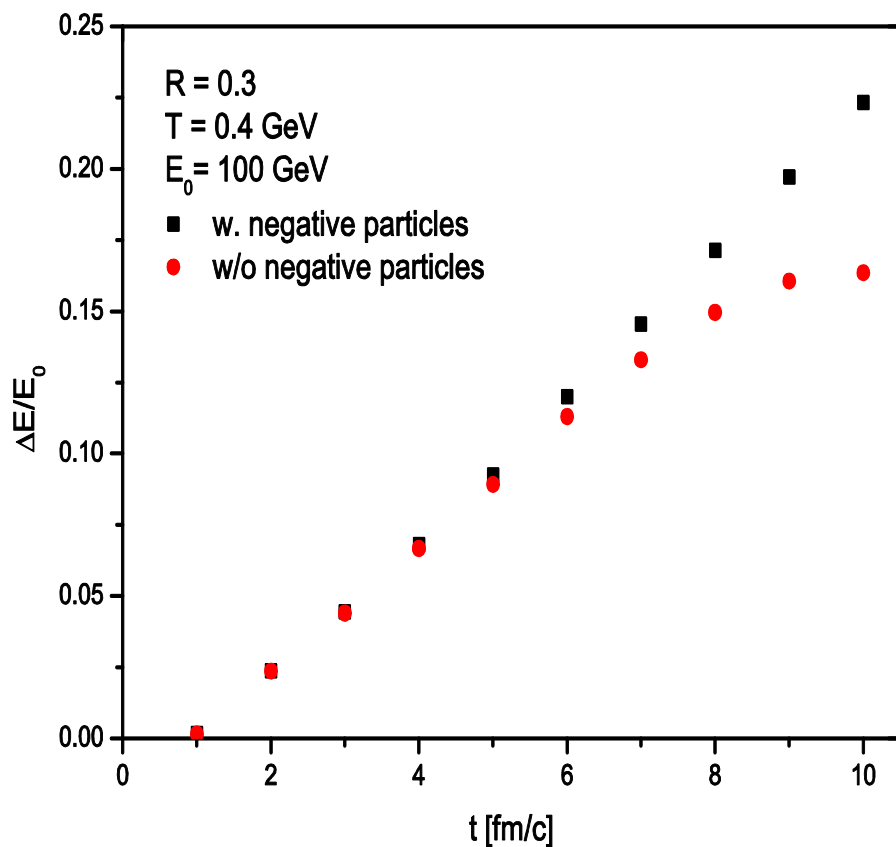
## Reconstructed jet

$$\rho(r) = \frac{1}{\Delta r} \frac{1}{N_{jet}} \sum_{jets} \frac{p_t(r - \frac{\Delta r}{2}, r + \frac{\Delta r}{2})}{p_t(0, R)}$$



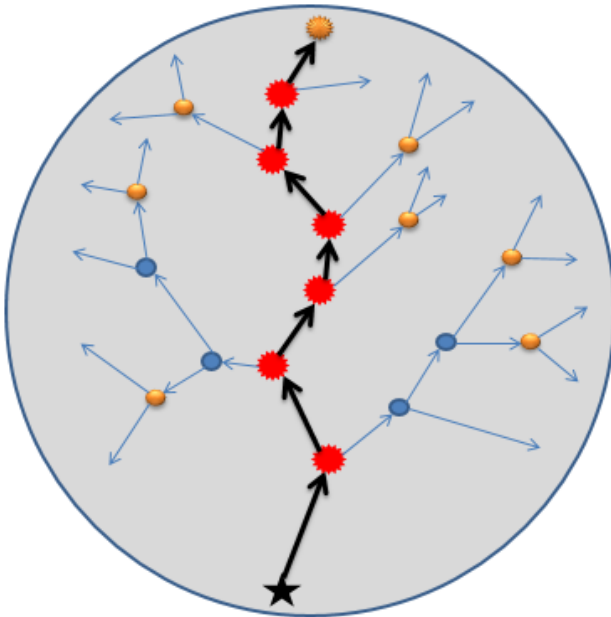
## Energy loss

## transverse profile



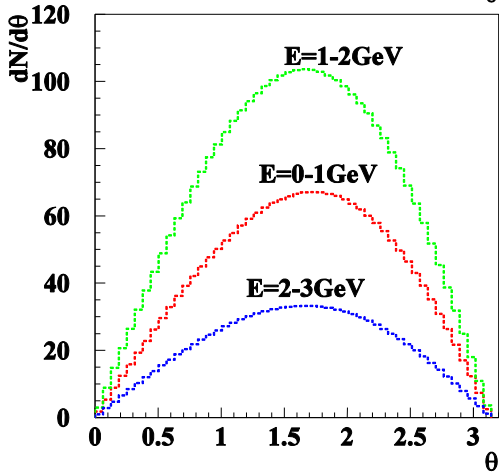
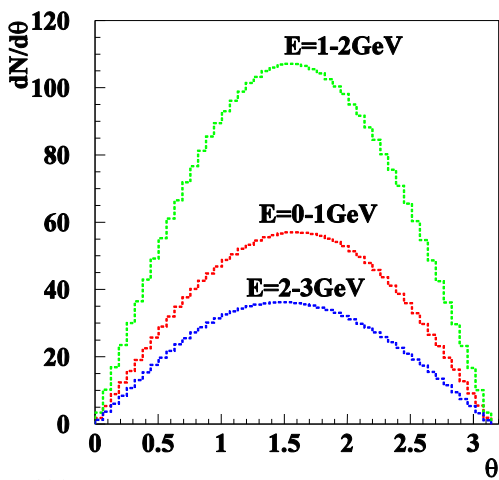
# Summary

- We present a computation of elastic energy loss of the leading parton traversing the uniform medium.
- The FASTJET program is used to reconstruct jets, the leading jet structure is distorted by the interaction with thermal partons.
- Graphics Processing Unit(GPU) parallel computing.

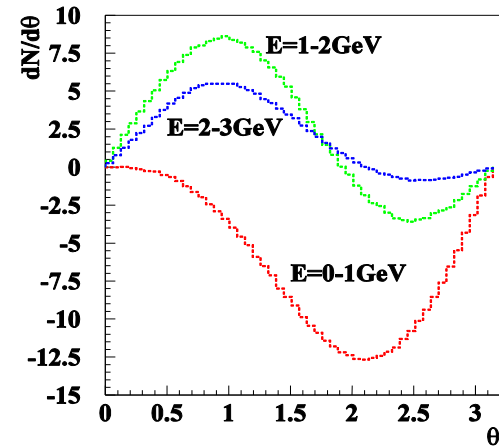


In a typical event

20000particles At  $t=8\text{fm}$

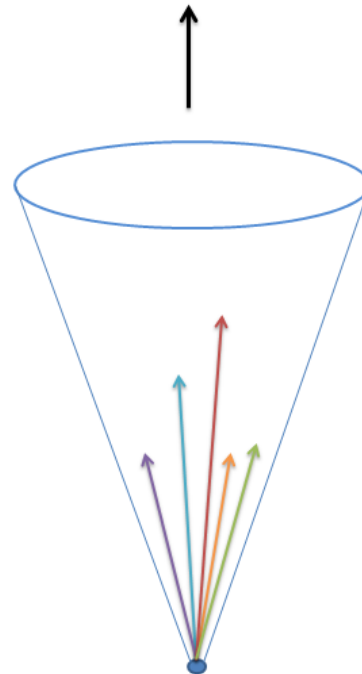


negative



combine

w/o negative



w. negative

