

Superfluid magneto-elastic oscillations of magnetars

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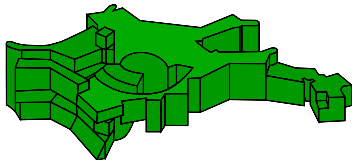
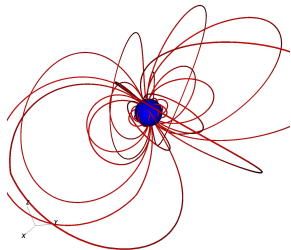
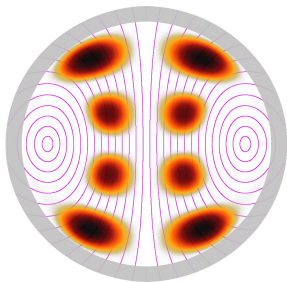
MNRAS, 443, 2014

PRL, 111, 2013

MNRAS, 430, 2013

MNRAS, 421, 2012

MNRAS, 410, 2011



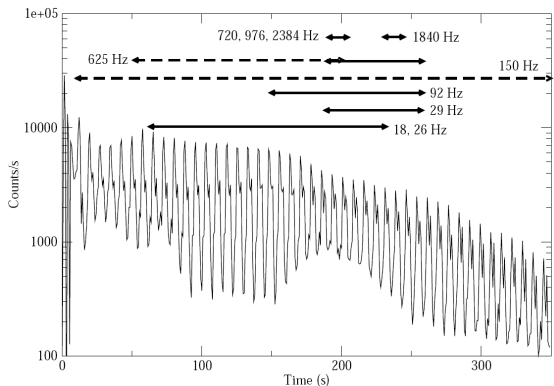
QPOs in giant flares of magnetars

Giant flares

- SGR 0526-66 (1978),
SGR 1900+14(1998),
SGR 1806-20 (2004)
- Strong modulation \Rightarrow
rotation period (5...10s)
- Additional quasi periodic
oscillations (QPOs)

(Israel et al. 2005, Strohmayer &
Watts 2006, El-Mezeini & Ibrahim
2010, Hambaryan et al. 2011)

- QPOs in normal bursts:
93, 127 and 260Hz
(Huppenkothen et al. 2014)



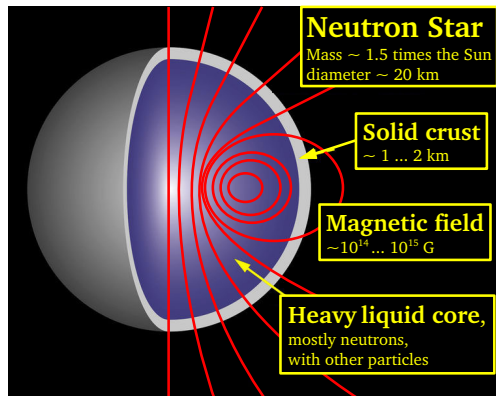
Strohmayer & Watts 2006

Confirmed QPO frequencies

SGR 1806-20: 18, 26, 30, 92, 150
625, 1840 Hz

SGR 1900+14: 28, 53, 84, 155 Hz

Where do the QPOs come from? Are they Starquakes?



Possible origin of the observed frequencies

- Discrete Shear modes (crust)?
- Alfvén oscillations at the turning points of a continuum (core+crust)?

Coupled Crust-Core oscillations

(Glampedakis et al. '06; Levin '07; Van Hoven & Levin '11 & '12;
Colaiuda et al. '10 & '11 & '12; Gabler et al. '11 & '12)

Torsional shear modes

Samuelsson & Andersson 2007

Observed frequency in Hz		Shear mode	
SGR 1806-20	SGR 1900+14	n	l
18		???	???
26		???	???
30	28	0	2
	53	0	4
92	84	0	6
150		0	10
	155	0	11
625		1	
1840		3	

(Schomaker & Thorne 1983, Piro 2005, Samuelsson & Andersson 2007)

- No magnetic field

- Free slip / zero traction at crust core interface

- Relativistic estimates for f :

$$\Rightarrow n = 0:$$

$$f^2 \sim \frac{(l-1)(l+2)}{RR_c}$$

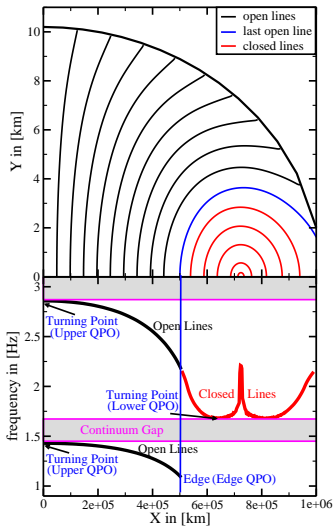
R_c - radius of crust

$$\Rightarrow n > 1:$$

$$f \sim \frac{n}{\Delta}$$

Δ - crust thickness

The Alfvén continuum



- Each field line has proper eigenfrequency (purely poloidal magnetic field + torsional oscillations)
- Field lines are coupled through:
 - (i) surface boundary conditions
 - (ii) the crust
 - (iii) numerics
- Long-lived QPOs exist at the turning-points or edges of the continuum
- Gaps between successive Alfvén overtones
- $f_1 : f_2 : f_3 : \dots = 1 : 2 : 3 : \dots$

(Levin '06 & '07, Sotani et al.'07, Cerdá-Durán et al. '09)

MCoCoA - 2D GRMHD simulations

MCoCoA

- Ideal MHD code in dynamical space-time (Godunov type schemes + flux CT)
- Spherical polar coordinates in axisymmetry (2D)
- Zero temperature, tabulated EOS
- Including elastic crust
- Spherically symmetric background
- Small-amplitude oscillations
- Cowling approximation
- In linear regime and axisymmetry poloidal and toroidal perturbations decouple

⇒ only consider torsional oscillations

Results - magneto-elastic oscillations inside the magnetar

$$B^2 \ll \mu_S \quad B \sim 10^{13} \text{ G} \quad B \sim 10^{15} \text{ G} \quad B^2 \gg \mu_S$$



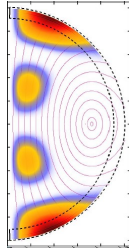
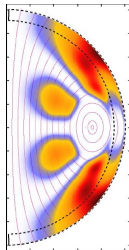
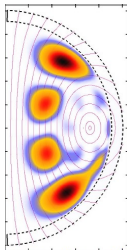
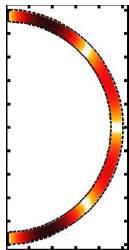
**predominantly
shear modes**

**shear modes
strongly
damped**

**magneto-elastic QPOs
confined
to core**

**reach
surface**

**predominantly
Alfvén QPOs**



Identifying observed frequencies

- Frequency ratio of low frequency magneto-elastic oscillations (**antisymmetric**, **symmetric**) is roughly

$$1 : 2 : 3 : 4 : 5 : \dots$$

- **Different magnetic field configurations** give more than one fundamental

SGR 1806-20: (18), **26**, **30**, **92**, **150**, 625, 1840 Hz

SGR 1900+14: **28**, **53**, **84**, **155** Hz

or **28**, **53**, **84**, **155** Hz

Superfluid neutron star core - one-fluid approximation

Effective one fluid model (decoupling n from p):

$$\rho \rightarrow \rho_p \sim 0.05\rho$$

$$v_A^2 = \frac{B^2}{\rho} \rightarrow \frac{B^2}{\rho_p}$$

Fundamental oscillations

Exist as before but with:

$$f_{\text{sf}} \sim \frac{1}{t_A} \sim \frac{v_A}{R} \sim \frac{B}{R\sqrt{\rho_p}} \sim \frac{B}{R\sqrt{0.05\rho}} \sim 5 \times f_n$$

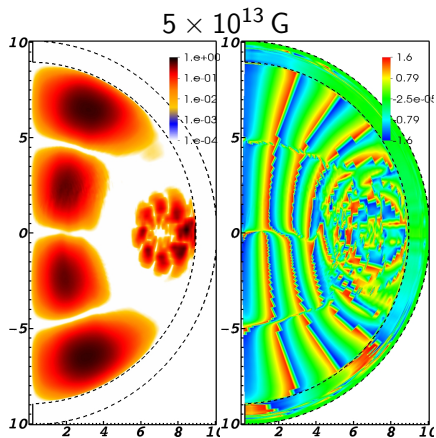
To match observed QPOs:

$$2 \times 10^{14} \lesssim B \lesssim 10^{15} \text{ G}$$

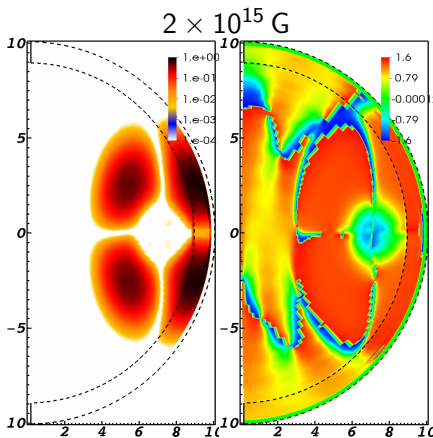
Andersson et al. '09, Glampedakis et al. '11, vanHoven & Levin '11 & 12,
Passamonti & Lander '13

Constant Phase Oscillations

- Alfvén dominated oscillations confined to the core
- Continuous phase change



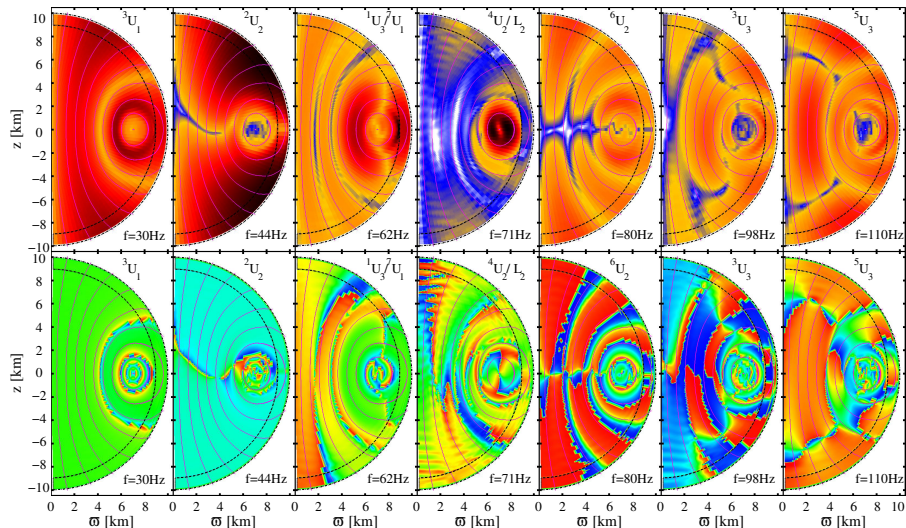
- Magneto-elastic oscillations penetrating the crust
- Constant phase



Lowest frequency oscillations lU_n at $B = 2 \times 10^{15}$ G

• l maxima in θ direction

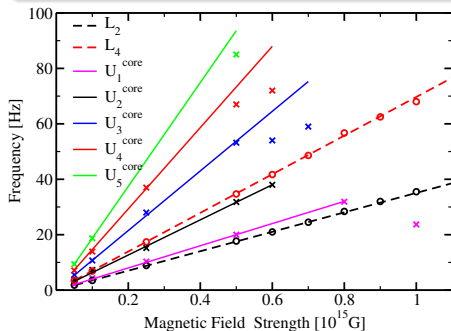
• n maxima in r direction



Scaling of the frequencies with B

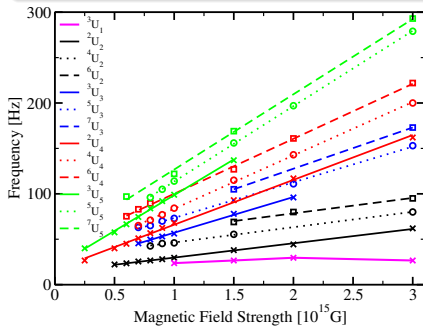
Alfvén oscillations (in the core)

- Continuous phase
- Scale linearly with B
- $f \rightarrow 0$ for $B \rightarrow 0$
- Exist for $B \rightarrow 0$



Magneto-elastic oscillations

- Constant phase
- Scale linearly with B
- $f \rightarrow f_0$ for $B \rightarrow 0$
- Disappear $B \lesssim \text{few} \times 10^{14}$ G



Scaling of the frequencies with $\varepsilon_* X_c$ at $B = 5 \times 10^{14}$ G

Fitting function: f [Hz] = $d_0 \times (\varepsilon_* X_c)^d$

Alfvén oscillations (in the core)

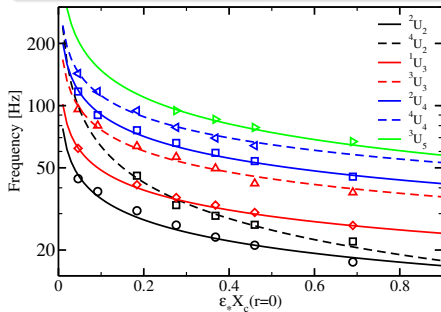
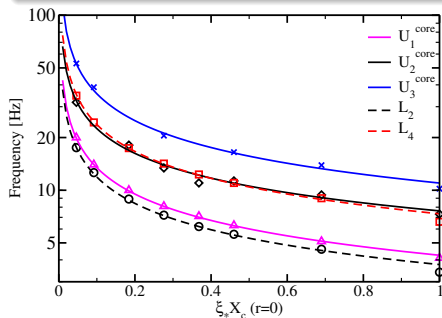
$$d \sim -0.5$$

$$f \sim \frac{v_A}{R} \sim \frac{B}{R\sqrt{\varepsilon_* X_c \rho}}$$

Magneto-elastic oscillations

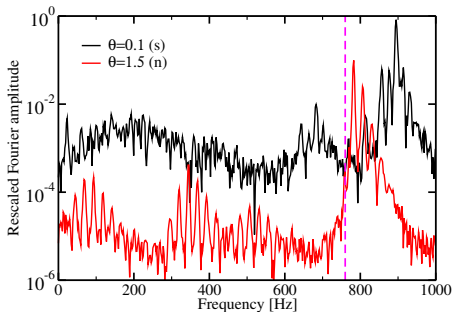
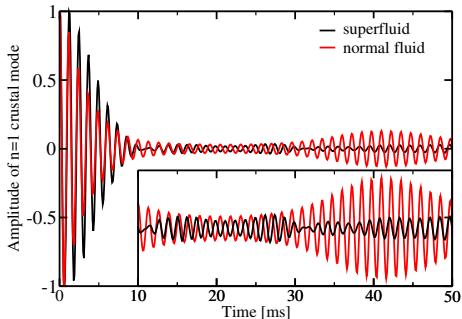
$$d \sim -0.33$$

crust is important



High frequency QPOs

- Rapid initial damping
- Long-lived QPOs at $f \sim f_{\text{crust}}^{n=1}$



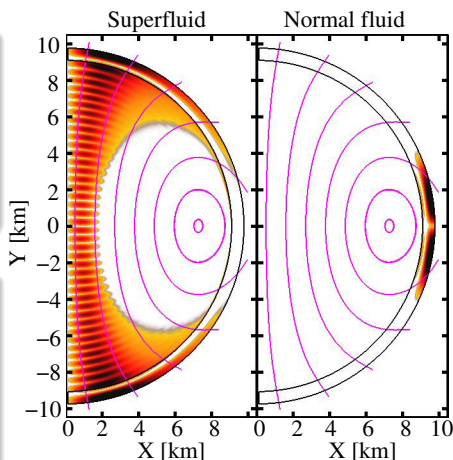
Superfluid neutron star core - High frequency QPOs

Normal fluid

- $n = 1$ radial shear mode structure
- Localized close to equatorial plane
- $\hat{B} \perp \hat{r} \Rightarrow$ predominantly shear mode only in crust

Superfluid

- $n = 1$ radial shear mode structure
- Close to pole
- Resonance with Alfvén overtone of core



Identifying observed frequencies

- Frequency ratio of low frequency magneto-elastic oscillations (**antisymmetric**, **symmetric**) is roughly

$$1 : 2 : 3 : 4 : 5 : \dots$$

- **Different magnetic field configurations** give more than one fundamental
- More **constant phase oscillations**, because different / dependence
- High frequency QPO as resonance of higher Alfvén overtone in core with $n > 0$ crustal mode if **core is superfluid**

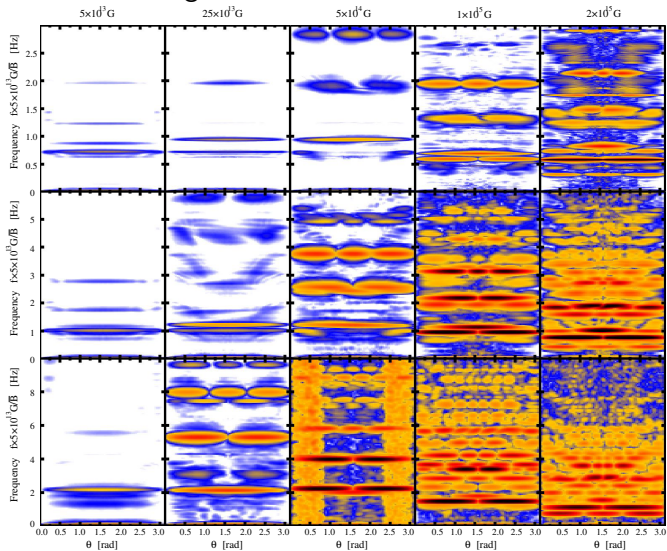
SGR 1806-20: (18), 26, 30, 92, 150, 625, 1840 Hz

SGR 1900+14: 28, 53, 84, 155 Hz

or 28, 53, 84, 155 Hz

Magneto-elastic oscillations break out of crust ($B \sim 10^{15}$ G)

Magnitude of the FFT at different B



$$\varepsilon_{\star} X_c =$$

$$\varepsilon_{\star} X_c = 8 \varepsilon_c^2 X_c^0$$

$$8 \times \varepsilon_{\star}^0 X_c^0$$

$$\varepsilon_{\star} X_c = 4 \varepsilon_c^2 X_c^0$$

$$4 \times \varepsilon_{\star}^0 X_c^0$$

$$\varepsilon_{\star} X_c = \varepsilon_c^2 X_c^0$$

$$\varepsilon_{\star}^0 X_c^0$$

Conclusions

- Antisymmetric (v_φ) fundamental magneto-elastic oscillations can explain low frequency QPOs
- Inclusion of superfluid effects:
 - ⇒ Low and high frequency QPOs
 - ⇒ B estimates in agreement with spin down observations
 - ⇒ Constant phase oscillations (no crustal modes in gaps!)
- Break out of oscillations sensitive to magnetic field strength and superfluid properties

QPOs of SGRs are probably superfluid magneto-elastic oscillations

Caveats:

- Different field configurations give same QPO frequency for different field strength
- Degeneracy between EOS and magnetic field configuration/strength