

ACTIVITY IN NEUTRON STARS

A. Melatos (Melbourne)

1. Rotational glitches
2. Superfluid turbulence
3. Magnetic crust-core decoupling

GPE SIMS

**EXCLUDE
MAGNETARS**

I. “ACTIVE INGREDIENTS”

Slow, erratic phenomena in radio pulsars:
glitches, nulling, orthogonal mode switching

DRIVER

- Heat flux... but NS **stably stratified** thermally
- EM **spin down** → crust-core shear

field decay
in magnetars

INTERMITTENCY ↔ STORAGE

- Pinned superfluid
- Closed magnetic flux tubes

Hall effect
in magnetars

CASCADE TO SHORT SCALES

- Local random pinning → global **inhomogeneity**
- Shear viscosity → turbulent **eddies**
- Magnetorotational and Tayler instabilities

STELLAR COMPONENTS

- Rigid **crust** → EM braking
- Inviscid n condensate → **superfluid**
- Viscous $p^+ + e^- +$ uncondensed n
 - **mutual friction** with n condensate
 - locks (?) magnetically to crust
- Array (?) of quantized **vortices** with $\kappa = \hbar/2m_n$
 - “wave function” $\Psi_s \propto e^{i\theta(x)}$ implies $\mathbf{v}_s \propto \nabla\theta$
 - **pinned** to nuclear lattice ($E_{\text{pin}} \sim \text{MeV}$)

Where is angular momentum stored?

(A) Inner crust SF ($I_{res} \approx 10^{-2}I_0$) plus “crust” ($I_c \approx I_0$),
i.e. lattice + p^+ + e^- + core n locked magnetically

1. Constant crust-SF lag over long term: $\langle \dot{\Omega}_{res} \rangle = \langle \dot{\Omega}_c \rangle$
2. SF glitches (no creep): $\langle \dot{\Omega}_{res} \rangle = \langle \Delta\Omega_{res,g} \rangle / \langle \Delta t_g \rangle$
3. AM conserved in glitch: $I_{res}\Delta\Omega_{res,g} = -I_c\Delta\Omega_{c,g}$

(Link et al. 99)

$$\frac{\langle \Delta\Omega_{c,g} \rangle}{\langle \Delta t_g \rangle} = -\frac{I_{res}}{I_c} \langle \dot{\Omega}_c \rangle$$

**few % from
radio timing**

(B) Inner crust & core SF (e.g. ${}^3\text{P}_2$) ($I_{res} \approx I_0$) plus “crust” ($I_c \approx 10^{-2}I_0$) comprising lattice + p^+ + e^-

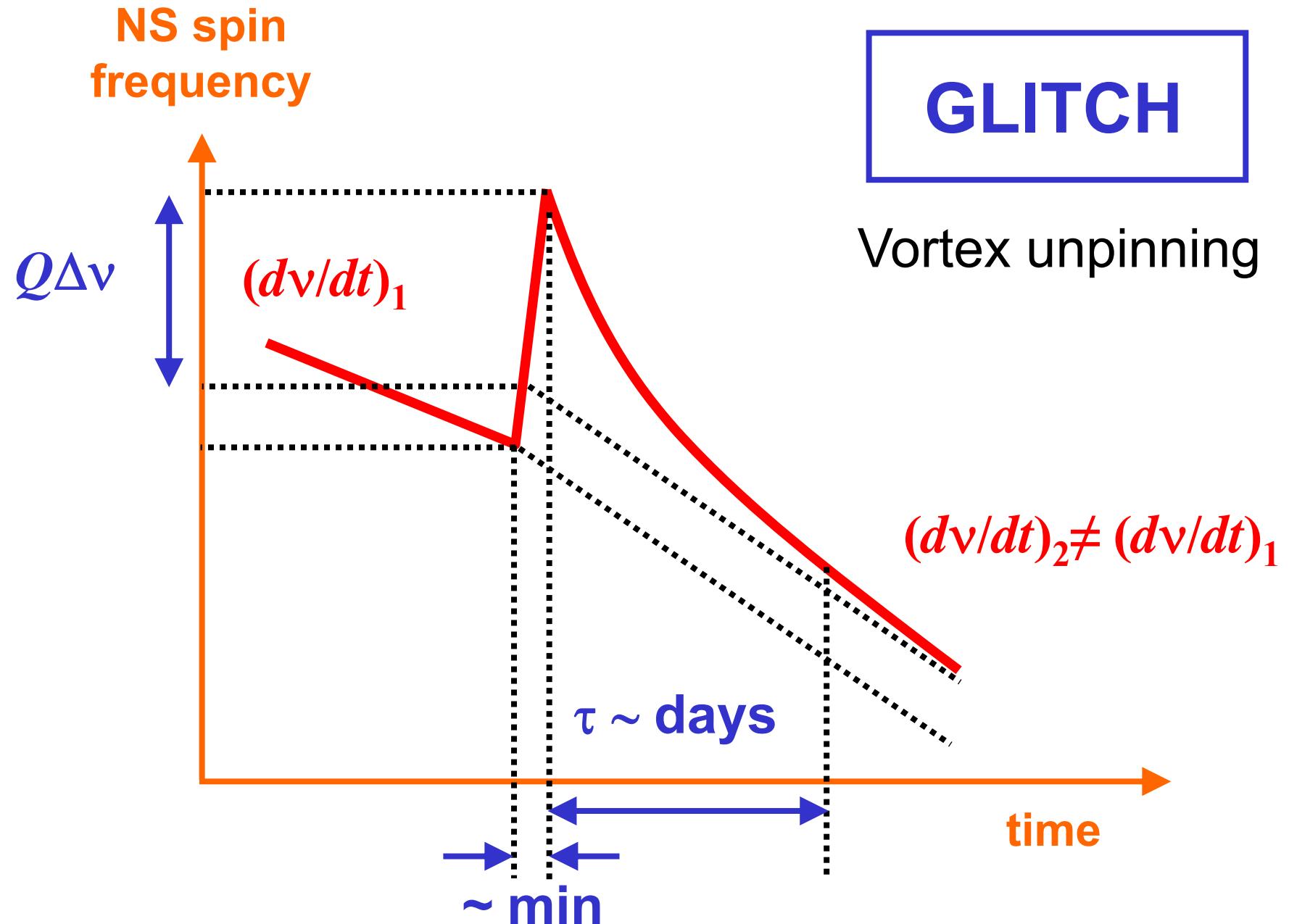
- **Bragg entrainment** reduces SF mobility relative to lattice (Chamel 12; Andersson et al. 12; Newton et al. 15)
- “Crust not enough”, $I_{res} > 0.1I_0$
- Consistent if creep dominates

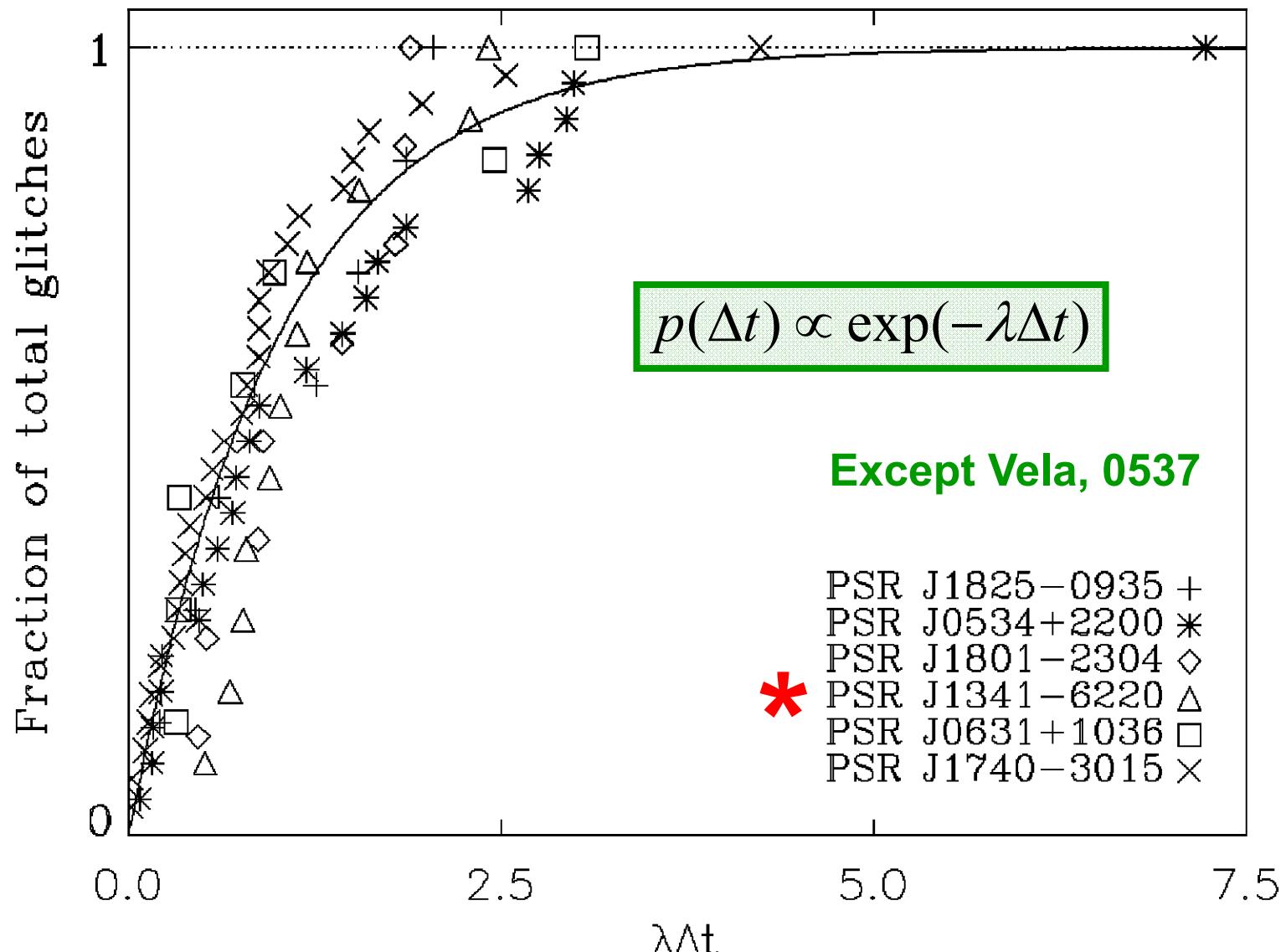
Superfluid **vortex**-superconductor **fluxoid** coupling

- **Strong...** if not tangled... (Ruderman et al. 98; Link 12)
- **Weak...** e.g. snow plow (Pizzochero 11; Haskell et al. 12), type I superconductor (Jones 06)

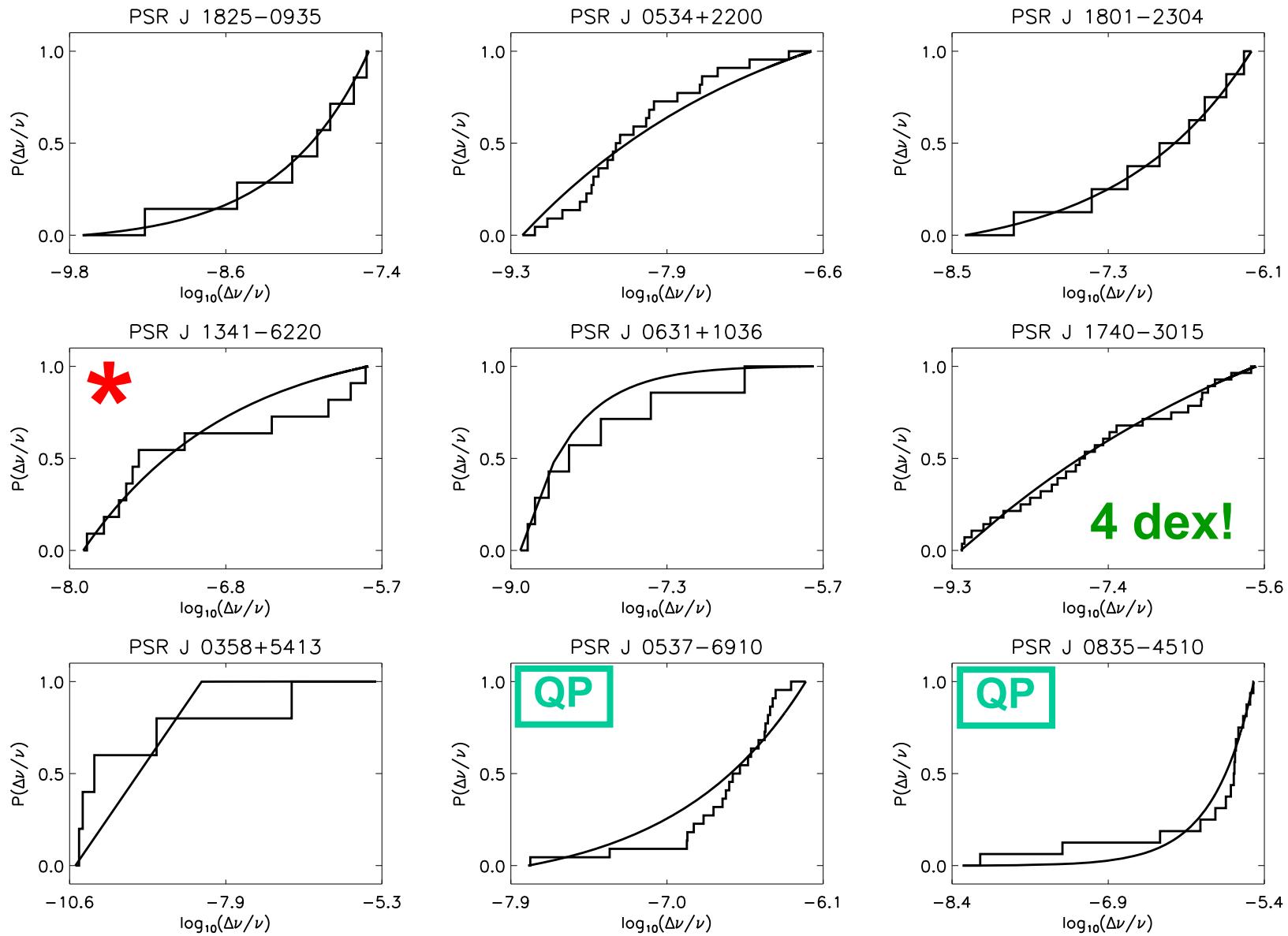
II. GLITCHES

Gross-Pitaevskii simulations:
trigger mechanism and long-term statistics



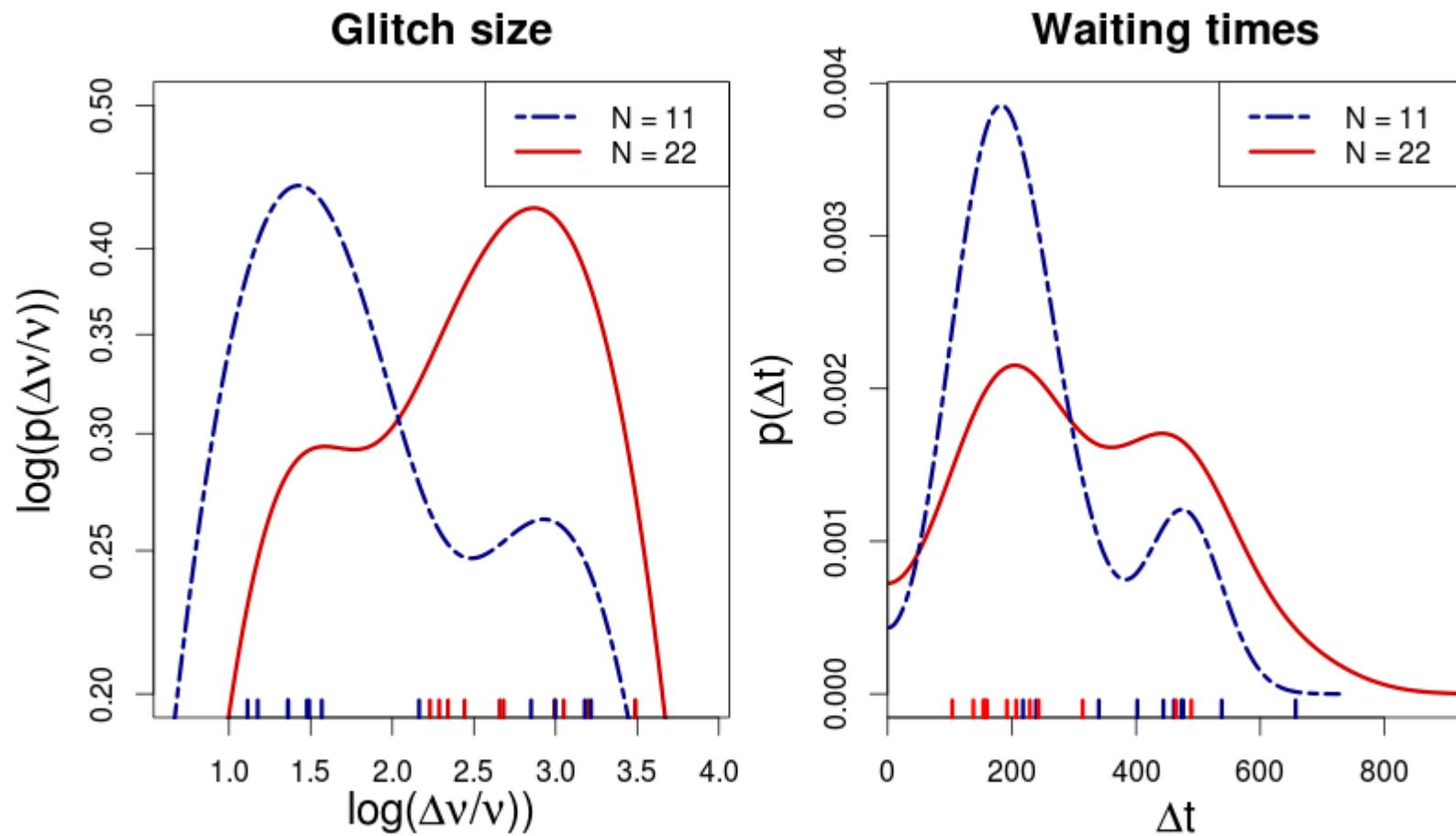


“Poisson” waiting times (Melatos et al. 08)



Power-law sizes (Melatos et al. 08)

$$p(\Delta\nu) \propto (\Delta\nu)^{-\alpha}$$



PSR 1341-6220: a leopard can change its spots
(Melatos et al. 15)

- **Avalanche dynamics**
- Self-organized criticality
- Earthquakes, sand piles
- Slow, global driver
- Impulsive, local relaxation
- “Stick-slip” motion



San Francisco
1906

SF vortices **unpin** and **move** → glitch

10^{16} vortices per star

10^6 to 10^{12} vortices per glitch

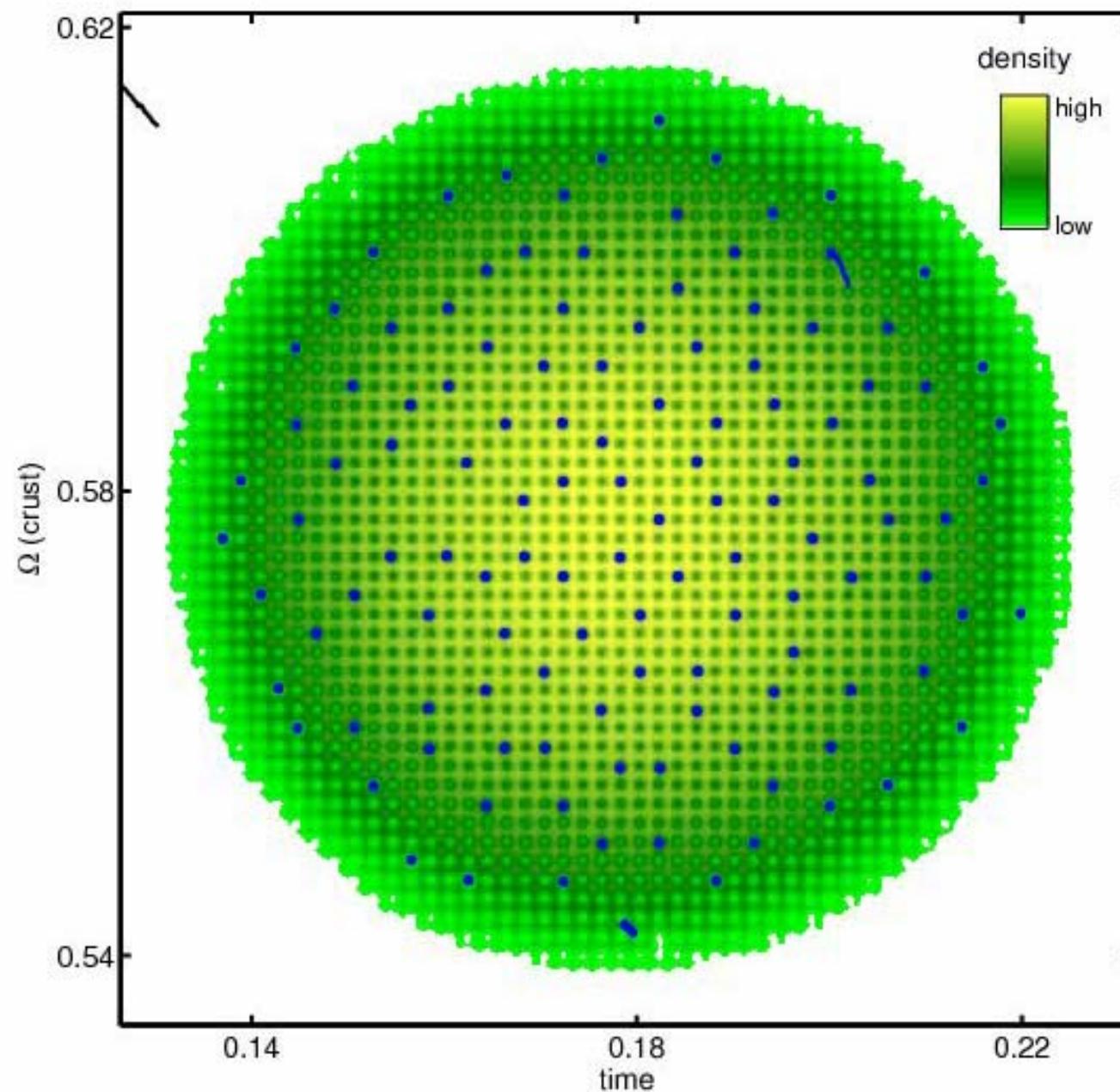
Central limit theorem →

narrow range of sizes and waiting times...

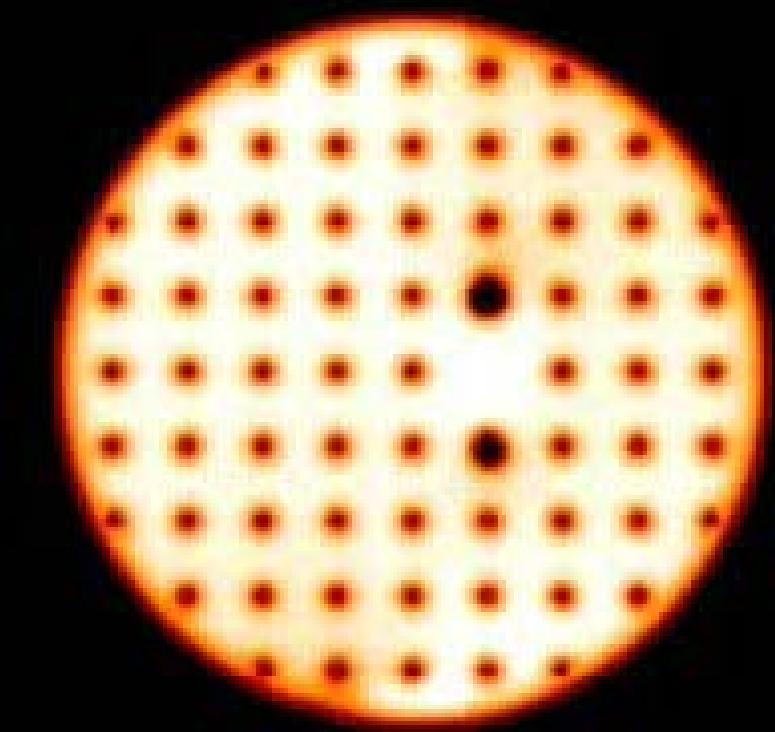
... not seen except in Vela and 0537

Vortex motion must be correlated – how?

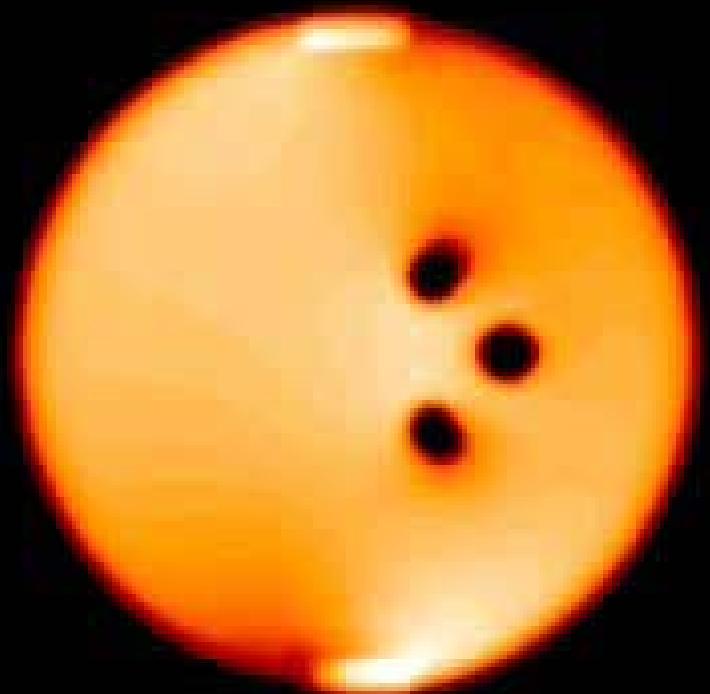
stochastic
GPE



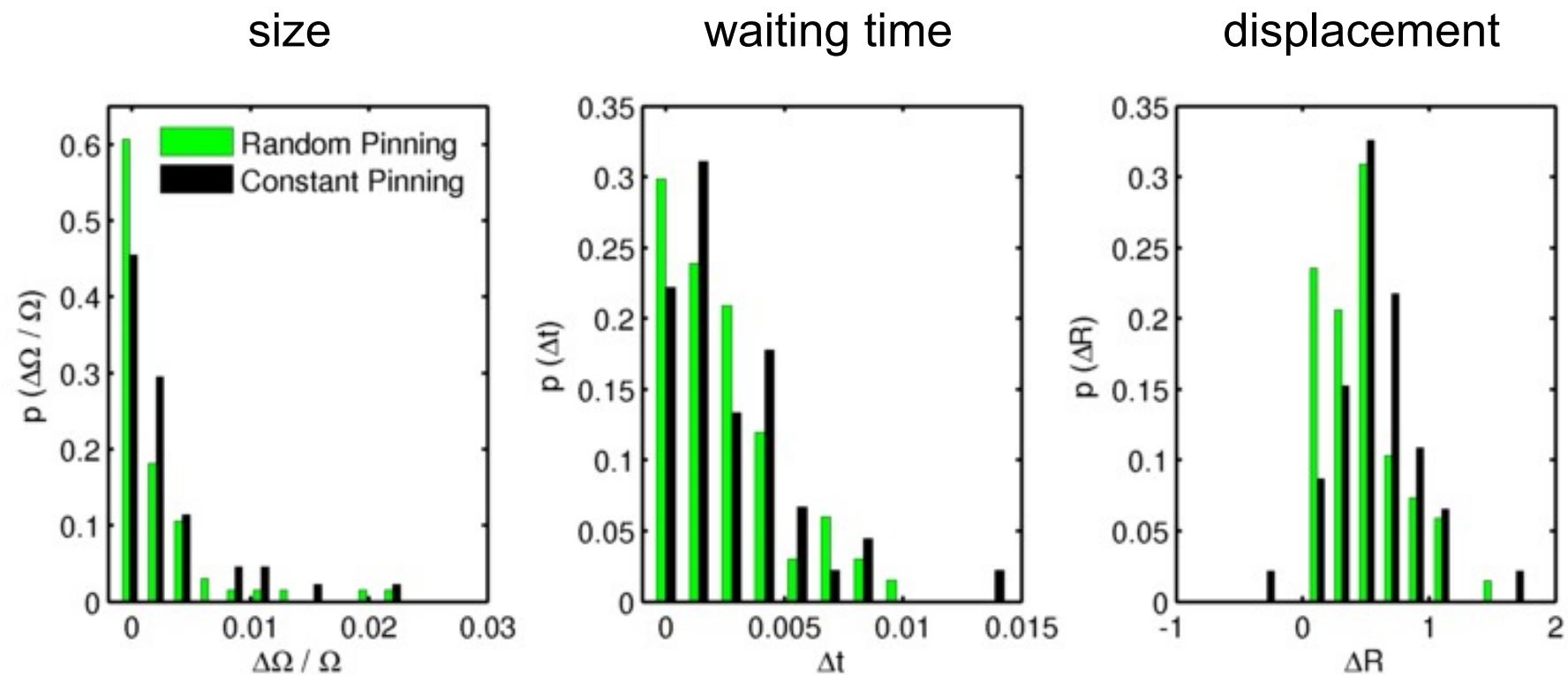
- Glitches occur at random times
- Range of sizes
- Vortices unpin **collectively**
- Move in “**herds**” covering a wide area
- **Dodge** sites and **exit** system (“slalom skier”)
- **Skip** sites and **repin** (“fill in gaps”)



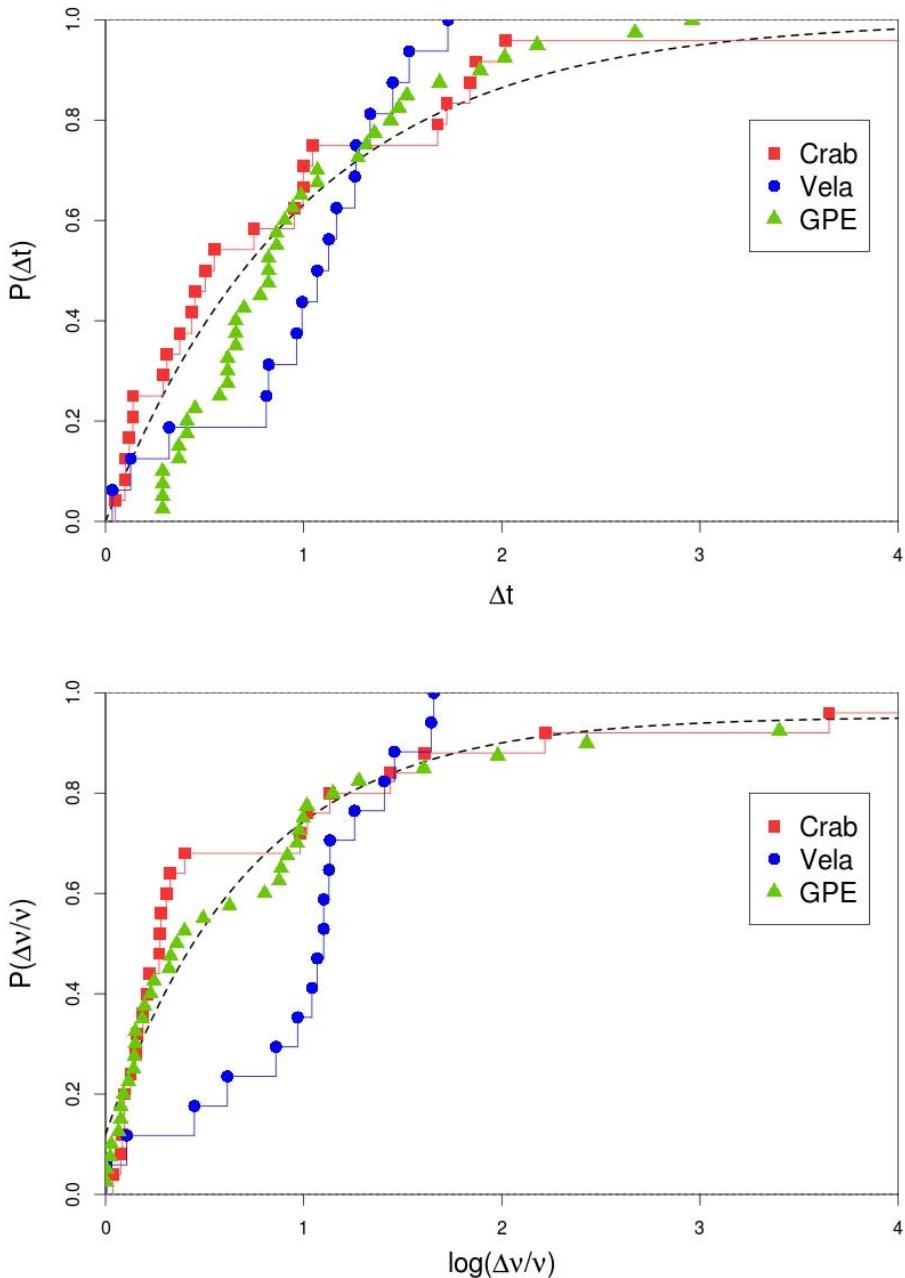
← Proximity knock-on



Acoustic knock-on →



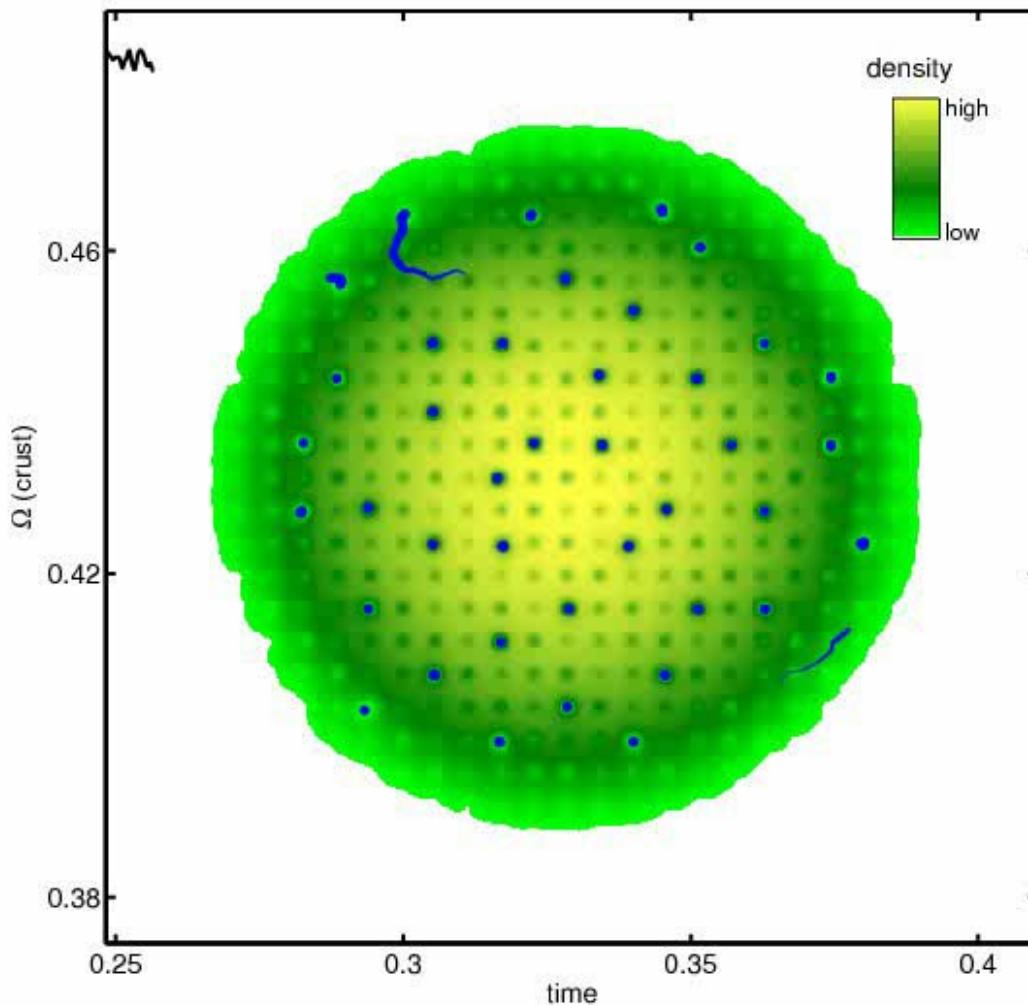
- Power-law $\Delta\Omega$, Poisson Δt (small N still...)
- Similar for uniform & random pinning



**Waiting times:
theory & data**

Sizes

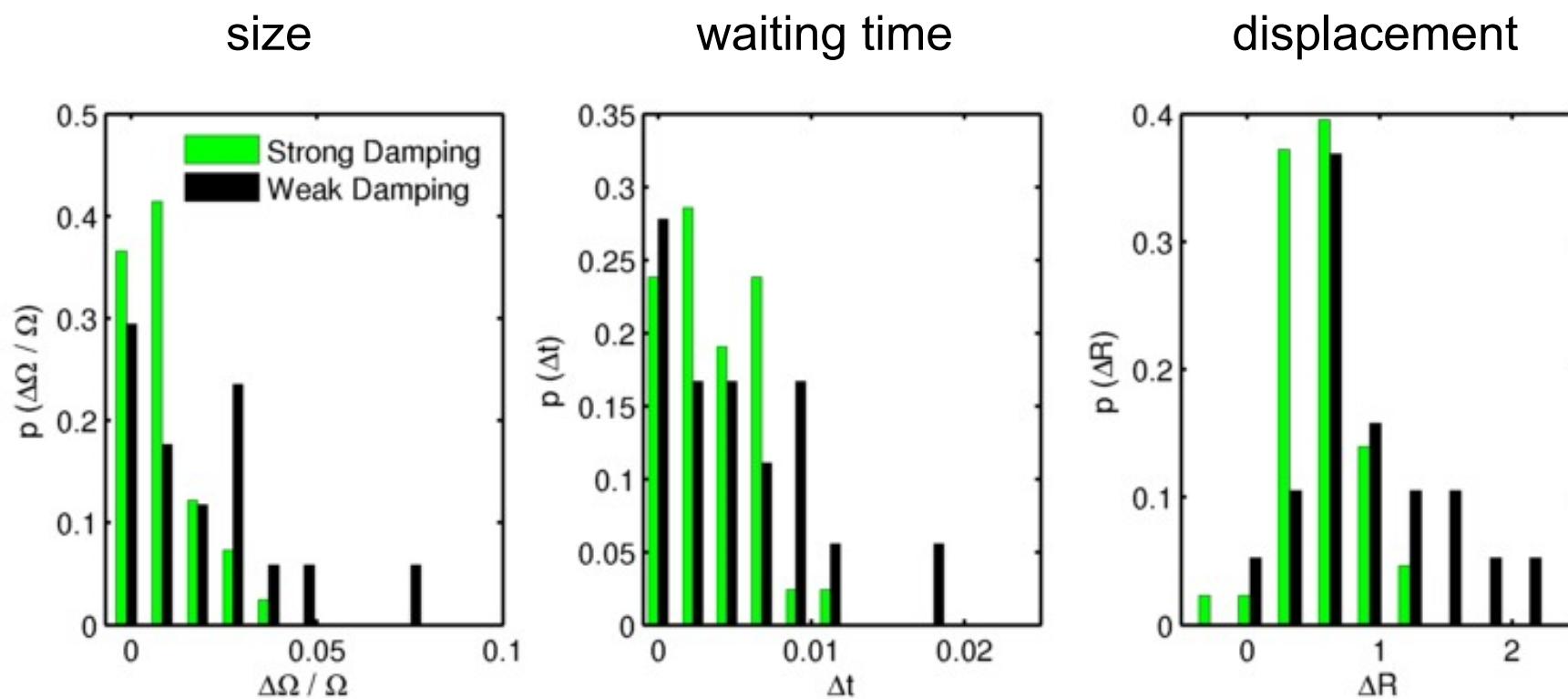
Minimum glitch size
resolved in Crab?
(Espinoza et al. 14)



Weak
damping

Acoustic
unpinning

- Avalanches cover **more area**
- Post-glitch **recovery** more **complete**



Unpin acoustically even if Magnus weak

INTERESTING NUMBERS

Damping coefficient (dimensionless) in GPE

- Rate: condensate → excited states

$$\gamma = \frac{32\pi m_n g a^2 k_B T}{h^2} \approx 0.2 \left(\frac{g}{3} \right) \left(\frac{a}{10 \text{ fm}} \right)^2 \left(\frac{T}{10^8 \text{ K}} \right)$$

borderline!

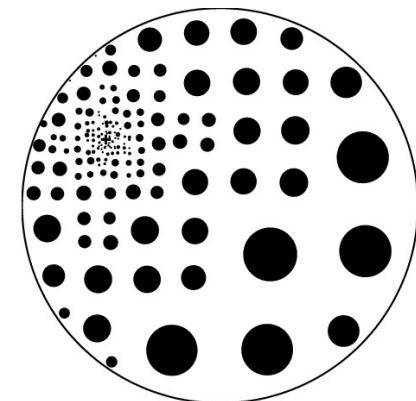
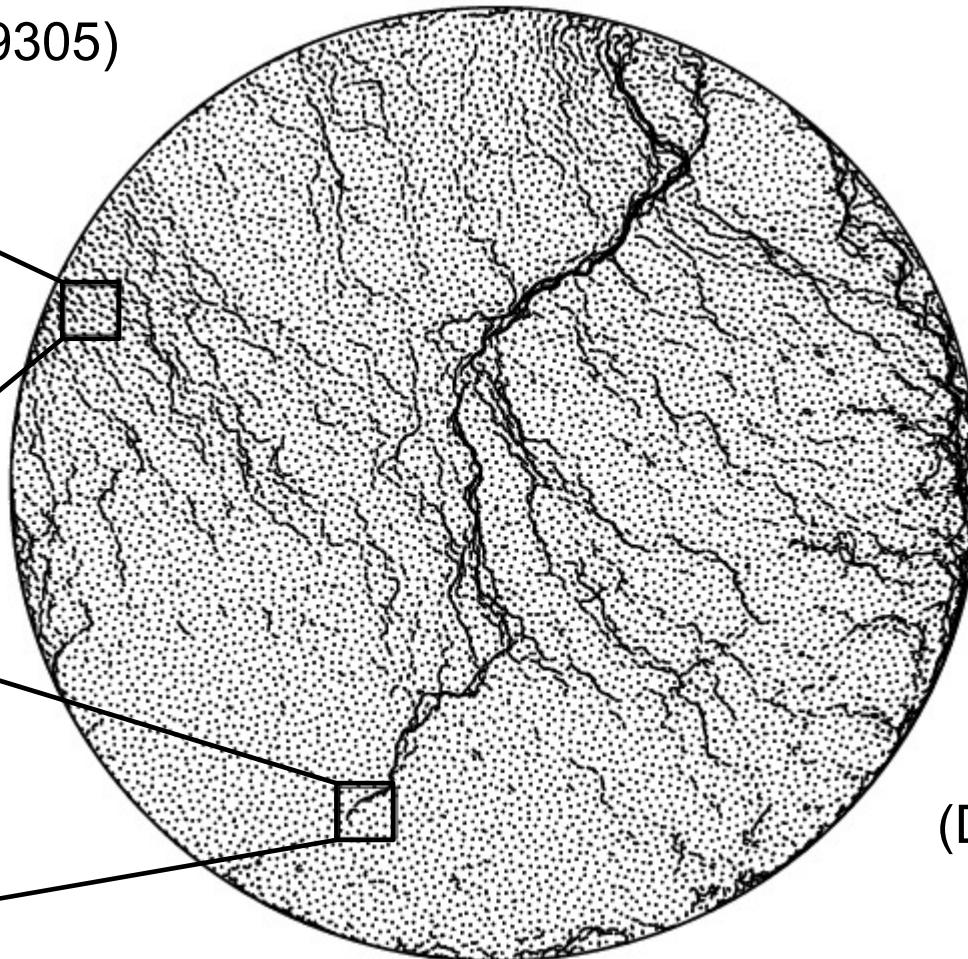
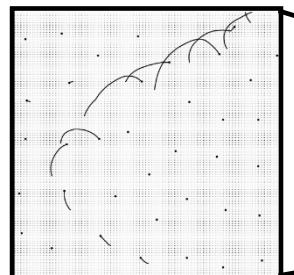
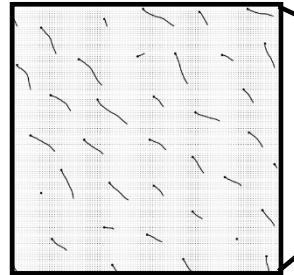
s-wave scatt'ng
length (-ve!)

Fractional **glitch size**

- Need $N_{unpin} \sim N_{total}$ and/or $\Delta R \gg \lambda_F \approx 10^{-7} R_*$ to explain largest glitches

$$\frac{\Delta\Omega_c}{\Omega_c} \approx \left(\frac{I_s}{I_c} \right) \left(\frac{N_{unpin}}{N_{total}} \right) \left(\frac{\Delta R}{R_*} \right)$$

Tracks of big avalanche
(5238 out of 9305)



Barnes-Hut
nesting

(Douglass et al. 15)

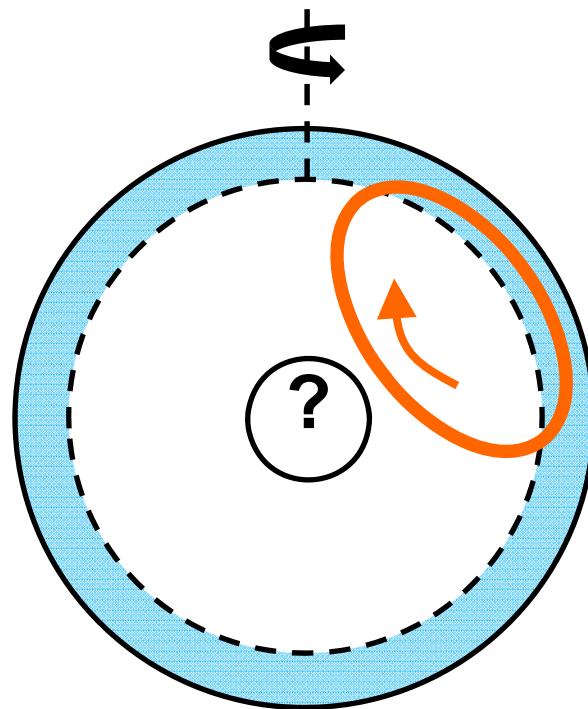
- Larger systems → **hierarchical** N-body code
- In progress (NB. can't do acoustic waves)

III. SF TURBULENCE

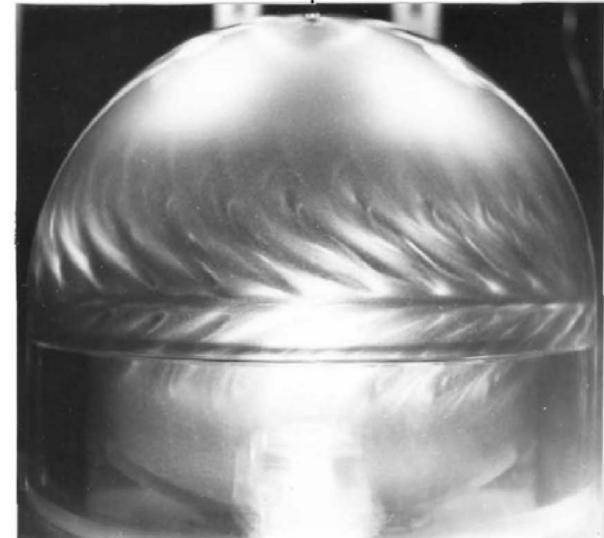
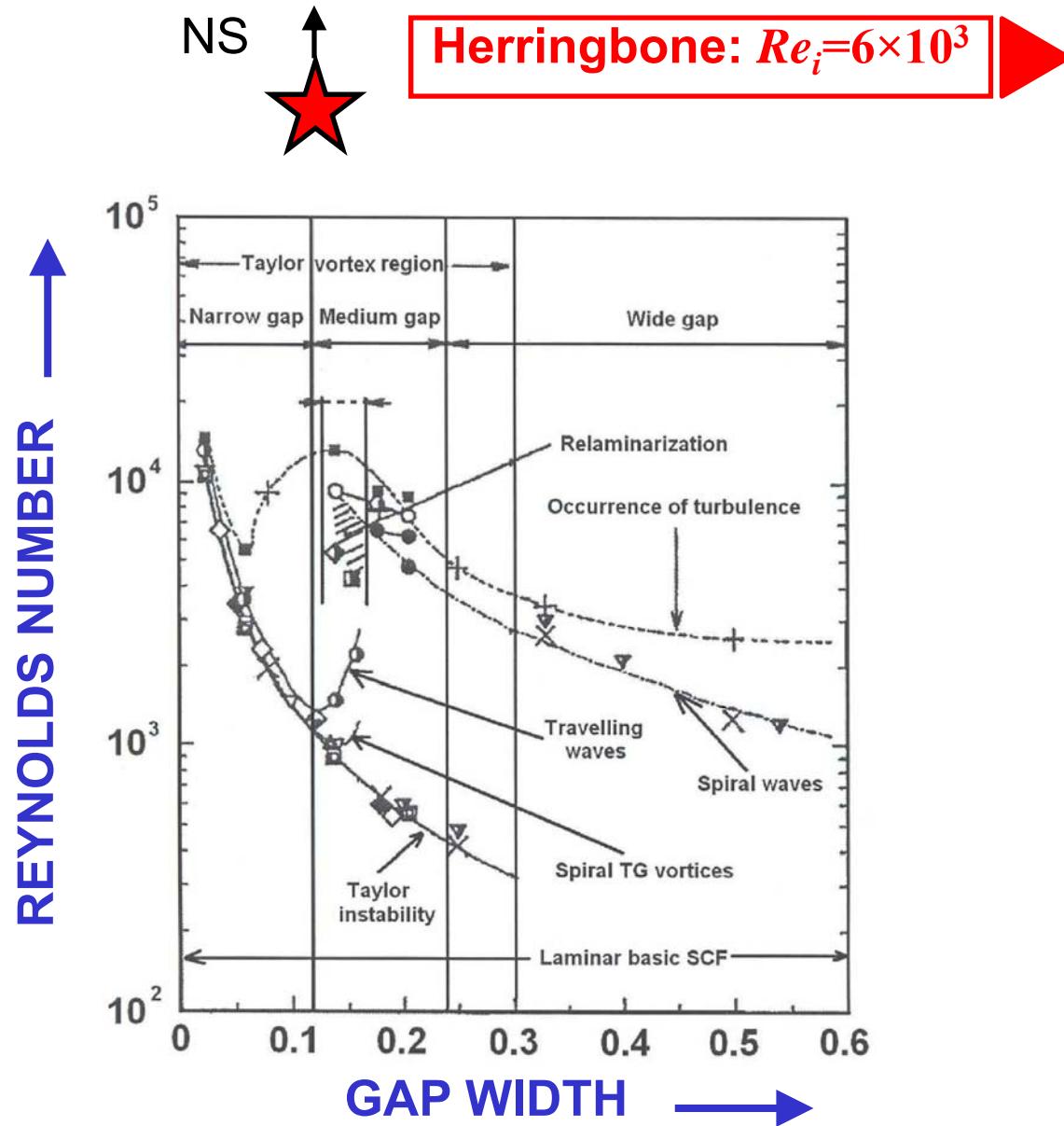
Macro... high- Re Kolmogorov eddies

Micro... tangled unstable vortices

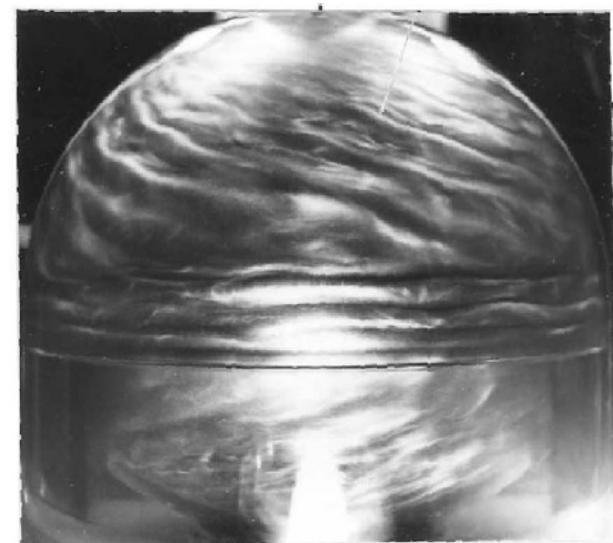
Interior fluid sucked into
boundary layer, spun down,
then recycled



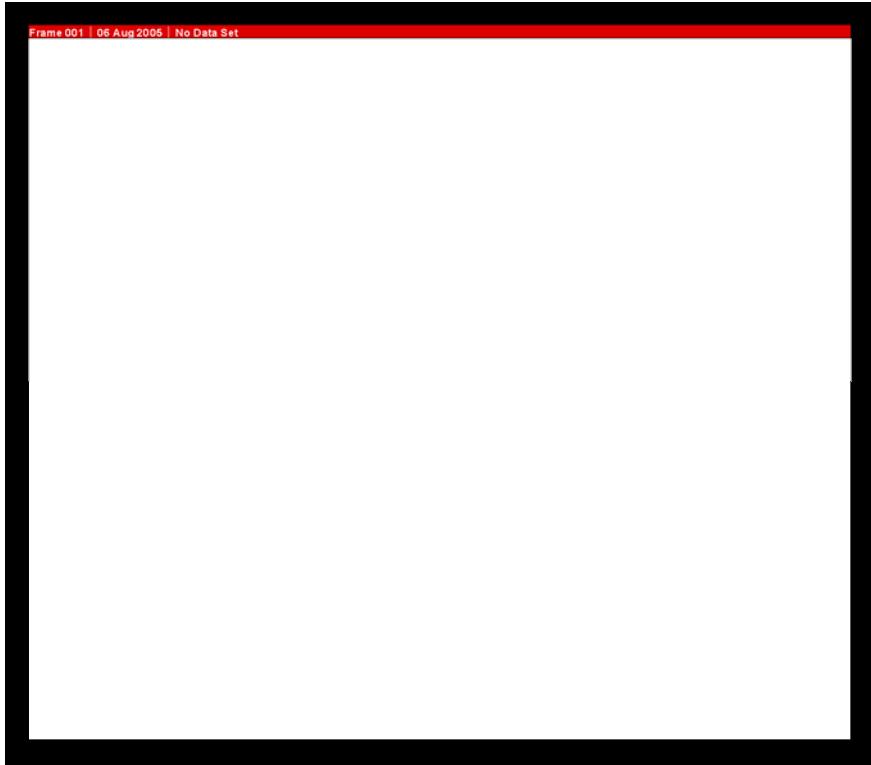
Ekman pumping (“cup of tea”)



(Nakabayashi 83)

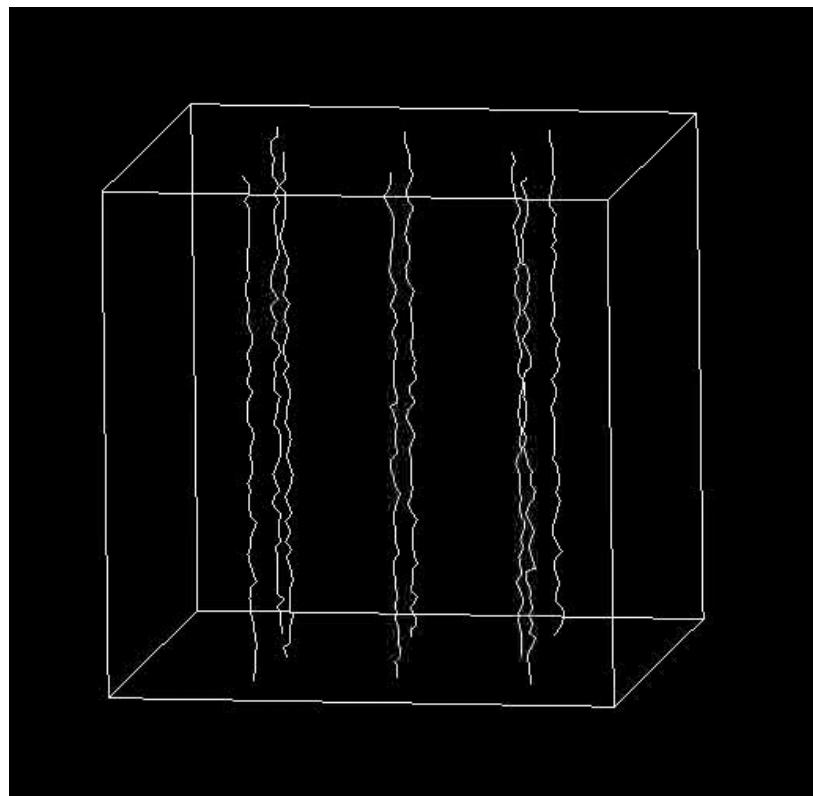


Taylor-Görtler: $Re_i=1\times10^4$



◀ **Two-component
HVBK simulation**

(Peralta et al. 05, 08)



**Kinematic
Schwarz equation** ▶

(Tsubota group)

VORTEX TANGLE

DONNELLY-GLABERSON INSTABILITY

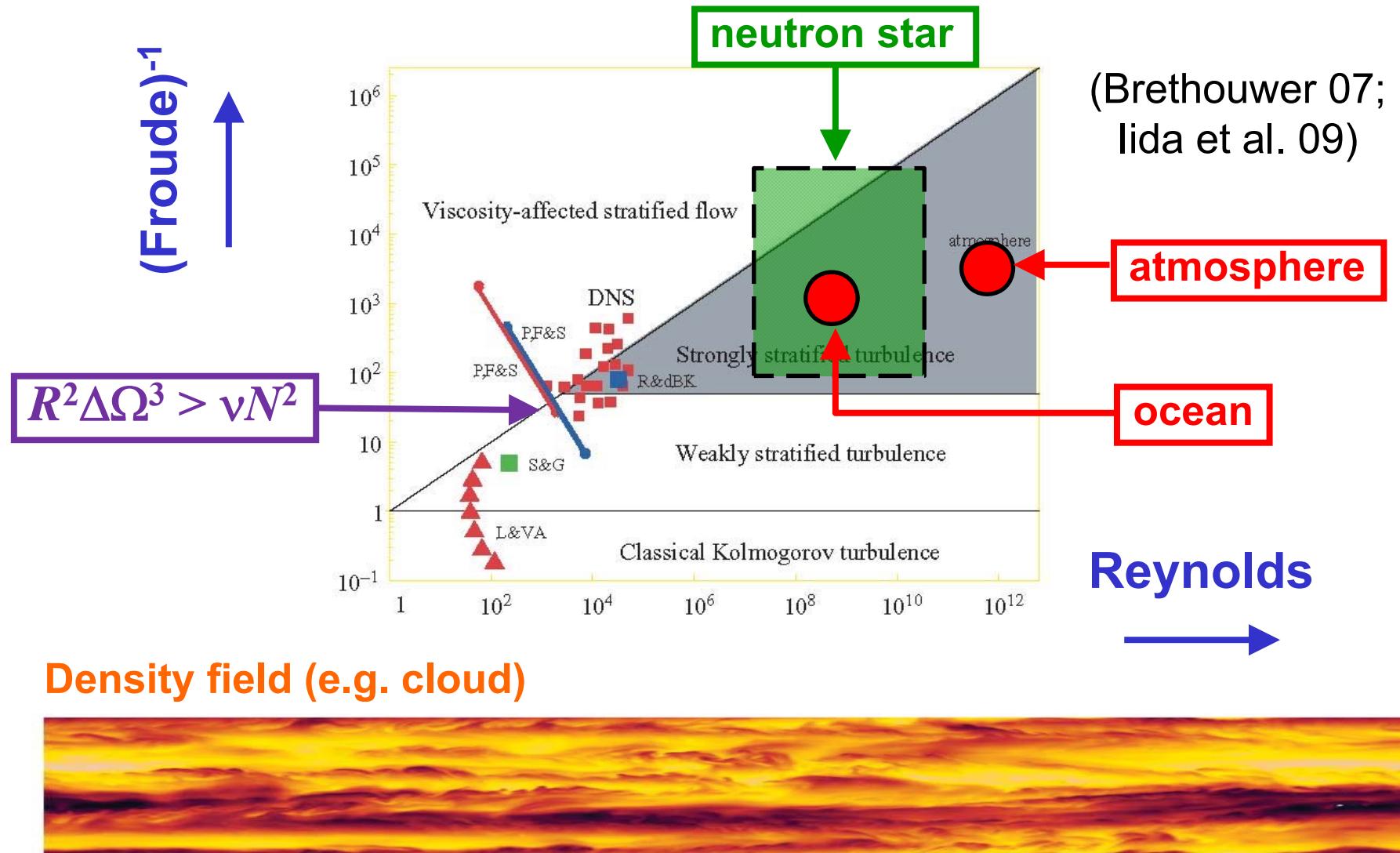
- Lab experiments (He, BEC) (Glaberson et al. 74)
- Ekman **counterflow** $V_{np} \approx R\Delta\Omega$ along vortices
- Mutual friction amplifies **Kelvin waves**
- Low threshold $V_{np} \sim \text{mm s}^{-1}$, fast growth $> \Omega$

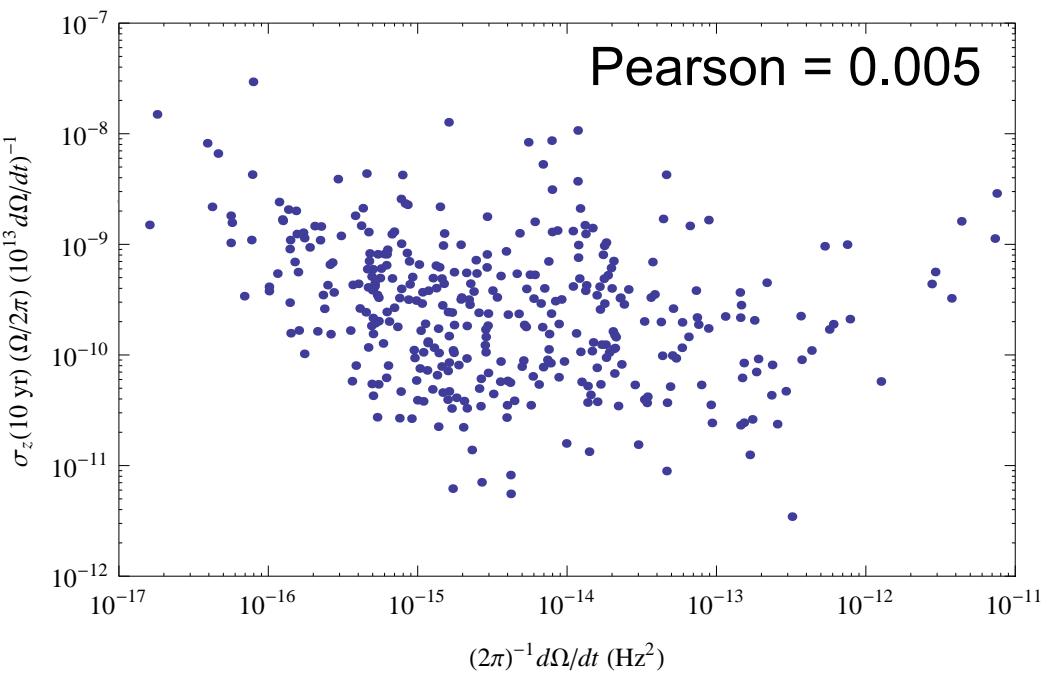
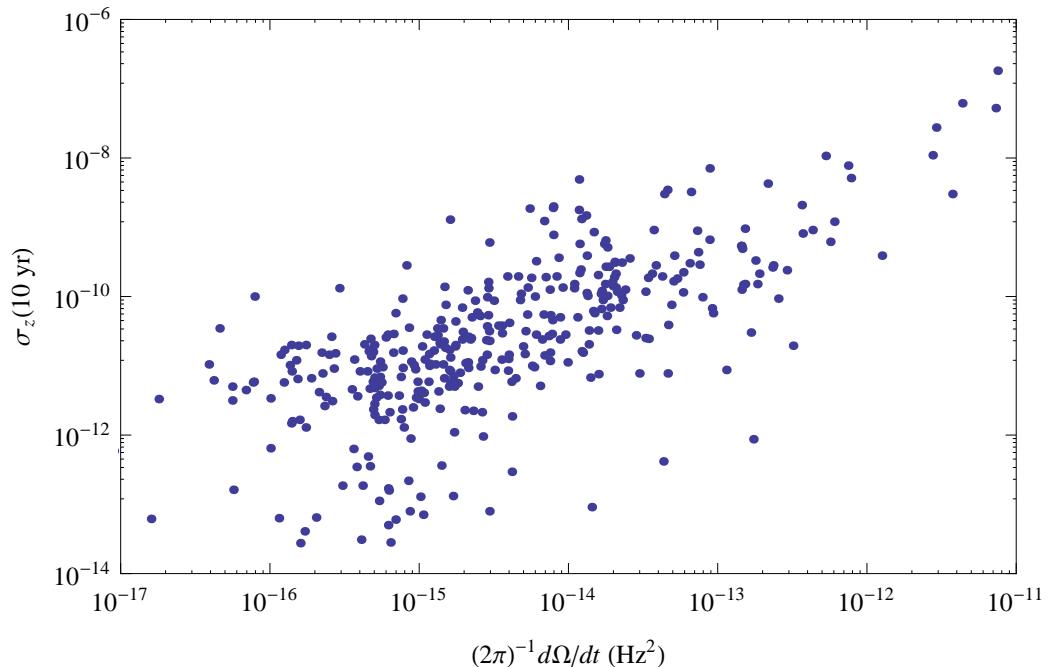
PINNING INSTABILITY (Glampedakis et al. 09; Link 12)

- Imperfect pinning → vortex creep → V_{np}
- Grows over days

Quenched by stratification (ρ_p/ρ_n)?

(Reisenegger & Goldreich 92; Gusakov & Kantor 13)





**Timing noise
measurements**
(Hobbs et al. 10)

$$\sigma_z = (720)^{-1/2} \Omega^{-1} \langle \ddot{\Omega}^2 \rangle^{1/2} T_{obs}^2$$

**Stochastic torque
theory**
(Melatos & Link 14)

$$\langle \ddot{\Omega}^2 \rangle \propto \left. \frac{d^4 \langle J_z(t) J_z(t+\tau) \rangle}{d\tau^4} \right|_{\tau=0}$$

IV. MAGNETIC ACTIVITY

Type I or II superconductor;
realistic magnetic geometry



Dendritic flux avalanche in MgB₂ (Johansen et al. 02)

**“Many magnetic topologies (e.g. closed loops)
cannot enforce corotation”** (Easson 79)

Are there realistic topologies which can? Unknown!

Fossil super-rotation of core (Melatos 12)

- Tayler or MRI **dynamo** (Braithwaite 06)
- “Geomagnetic jerks”, precession, GWs...

Shear in closed flux tubes (Glampedakis & Lasky 15)

- Kelvin-Helmholtz turbulence? Field → crust?

- Proof: slight departure from corotation; $\mathbf{B} = \mathbf{B}_0 + \mathbf{B}_1$

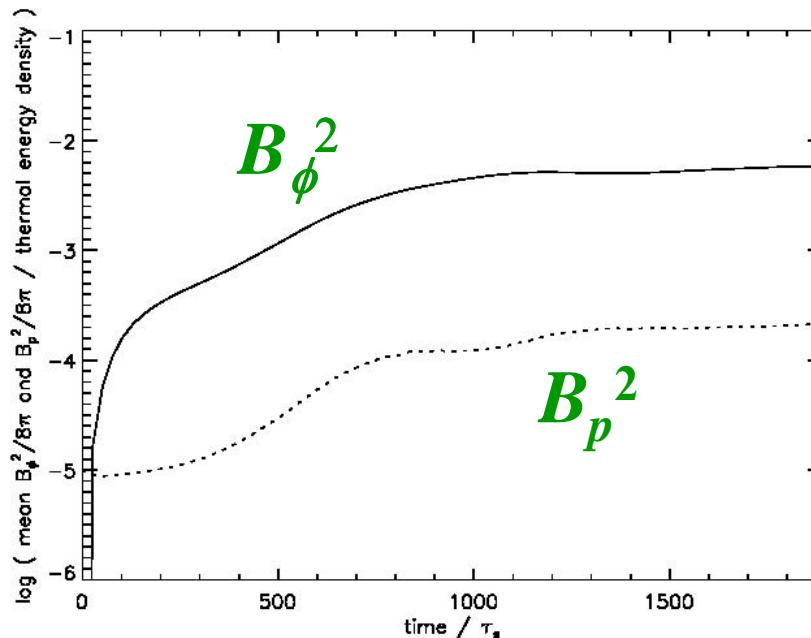
$$(4\pi)^{-1}(\mathbf{B}_0 \cdot \nabla)(RB_{1\phi}) = [K(\Omega_{line} - \Omega_{crust}) - k\dot{\Omega}_{crust} + c\dot{\Omega}_n]R^2 + F_{B\phi}R$$

- **Non-conservative** Fermi liquid forces etc on **RHS**
can't be balanced by pressure gradient
- Integrate along **closed B loop** → multivalued $B_{1\phi}$
- Plasma can't adjust; RHS depends on **unperturbed** state, except Ω_{line} (eq'n of motion independent of \mathbf{B})
- Generalized to “twisted torus” (Glampedakis & Lasky 15)
- Role of stratification unsolved

A dynamo can exist in a stably stratified star...

...in fact it works better! (Braithwaite 06)

- Driven by shear not thermal convection
- Tayler or MRI instabilities



~1% KE

Wound-up B_ϕ
too weak
to shut off shear

V. GRAVITATIONAL WAVES

New observational constraints

$$h_{lm} = \frac{G}{c^5 d} \frac{\partial^2}{\partial t^2} \int d^3x Y_{lm}^* r^l \mathbf{x} \cdot \text{curl}(\rho \mathbf{v})$$

$$\frac{GM}{Rc^2} \left(\frac{Rf}{c} \right)^2 \left(\frac{d}{R} \right)^{-1} \frac{\varepsilon_{\rho v} V}{c}$$

Current quadrupole \propto momentum flux $\propto T^{0i}$

- Vortices reorganize during **glitch rise** → GW burst (Warszawski & Melatos 12)
 $\Delta t_{rise} > 10 \text{ ms}$
- Ekman pumping during **glitch recovery** → monochromatic “long transient” (Bennett et al. 10)
 $N > 0.5$ and $K > 3$

- SF turbulence → **stochastic GW** (Melatos & Peralta 10; Lasky et al. 13)

$$\Delta\Omega/\Omega < 0.04 \text{ (individual)}$$

$$\Delta\Omega/\Omega < 0.01 \text{ (all MSPs in Universe)}$$

- Coherent LIGO searches for **known MSPs** near EM spin-down limits (Mastrano & Melatos 12)

$$h_0 < 2 \times 10^{-26}$$

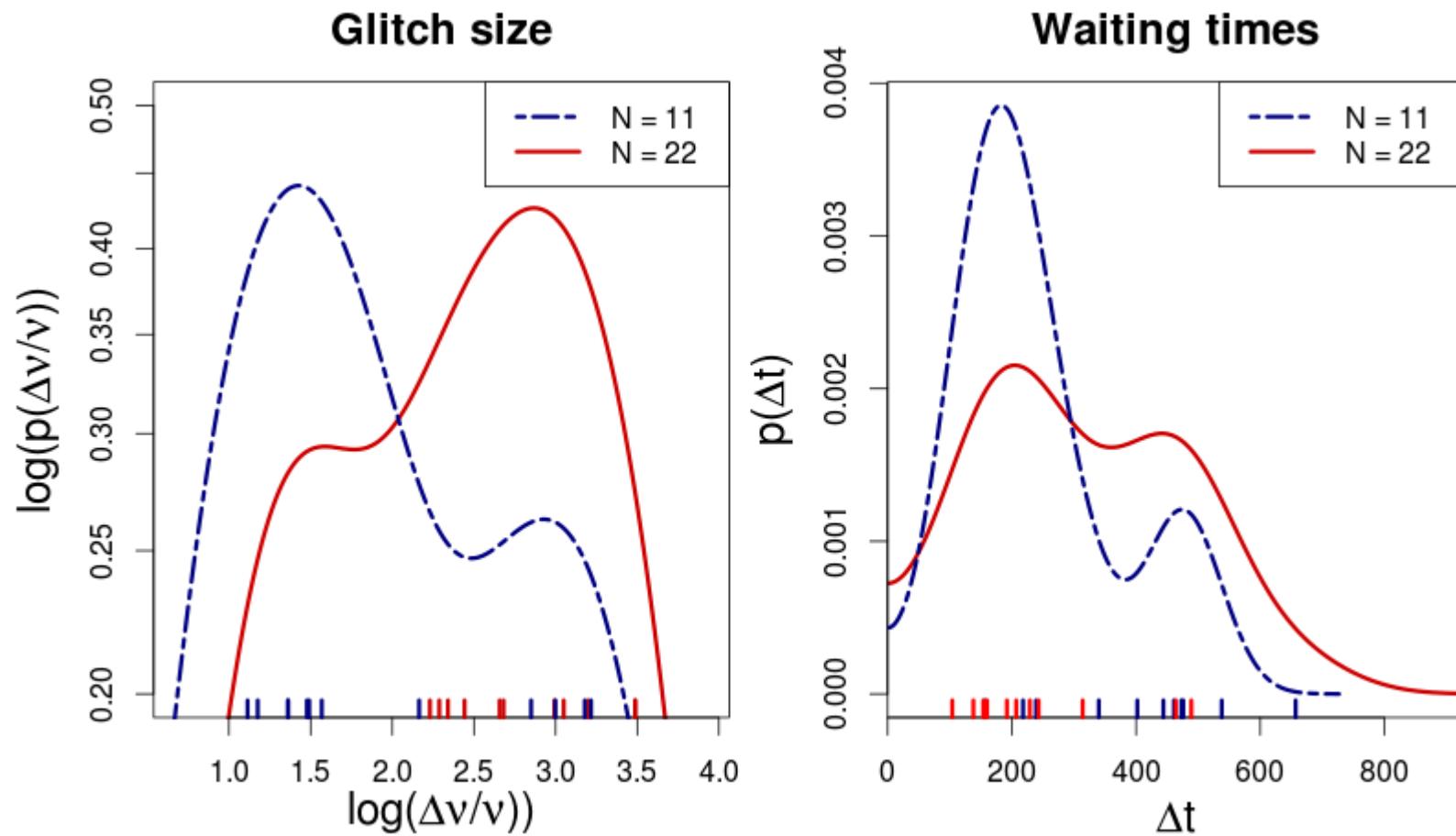
$$\varepsilon < 7 \times 10^{-8}$$

$$B_{int} < 10^{10} \text{ G (superconductor)}$$

NB. Burial or decay starts with $B_{int} > 10^{12} \text{ G}$

SUMMARY

- Intermittency \leftrightarrow storage \leftrightarrow self-organization
- **GPE** sim's of **vortex avalanches**
- Long-term statistics consistent with data
- **SF turbulence** (macro, micro) & buoyancy
- Timing noise
- Realistic magnetic geometry
- Gravitational wave constraints



PSR 1341-6220: a leopard can change its spots
(Melatos et al. 15)

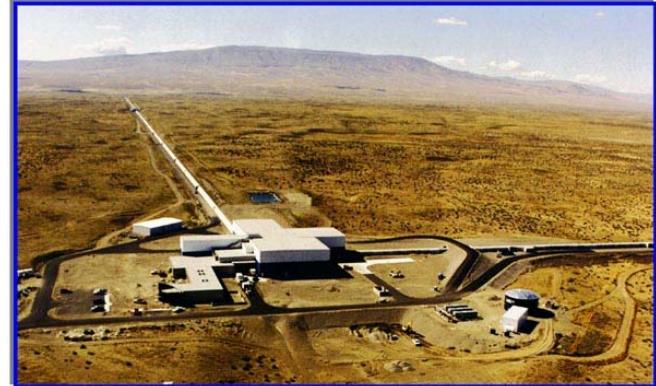
RECENT SF HIGHLIGHTS

- Energy gap (Gusakov & Kantor 13)
- Neutrino emissivity (Leinson 13)
- **Transport coefficients** & mode damping with hyperons (Kantor & Gusakov 09; Shternin & Yakovlev 08)
- Thermal conductivity (Chamel 12)
- Color-flavor-locked **viscosity** & **mutual friction** (Mannarelli et al. 10, 08; Alford et al. 10, 08)
- **Entrainment** couples SF to crust (Chamel 13) → **extra** angular momentum **reservoir** for glitches

- Magnetic axis **alignment** (Barskuov et al. 13)
- Ab initio **pinning** (Avogadro et al. 08; Pizzochero 11)
- “**Snowplow**” glitch model (Haskell et al. 12)
- Modes, instabilities, **gravitational waves**
(Passamonti & Andersson 12; Jones 10; Sidery et al. 10)
- **r-modes** (Ho et al. 11; Andersson et al. 10; Bondarescu et al. 09)
- **X-ray burst** cooling in LMXBs (Ho et al. 13)
- Rotochemical heating in MSPs (Reisenegger et al. 10)
- **Dark matter** condensate (Kouvaris 12)



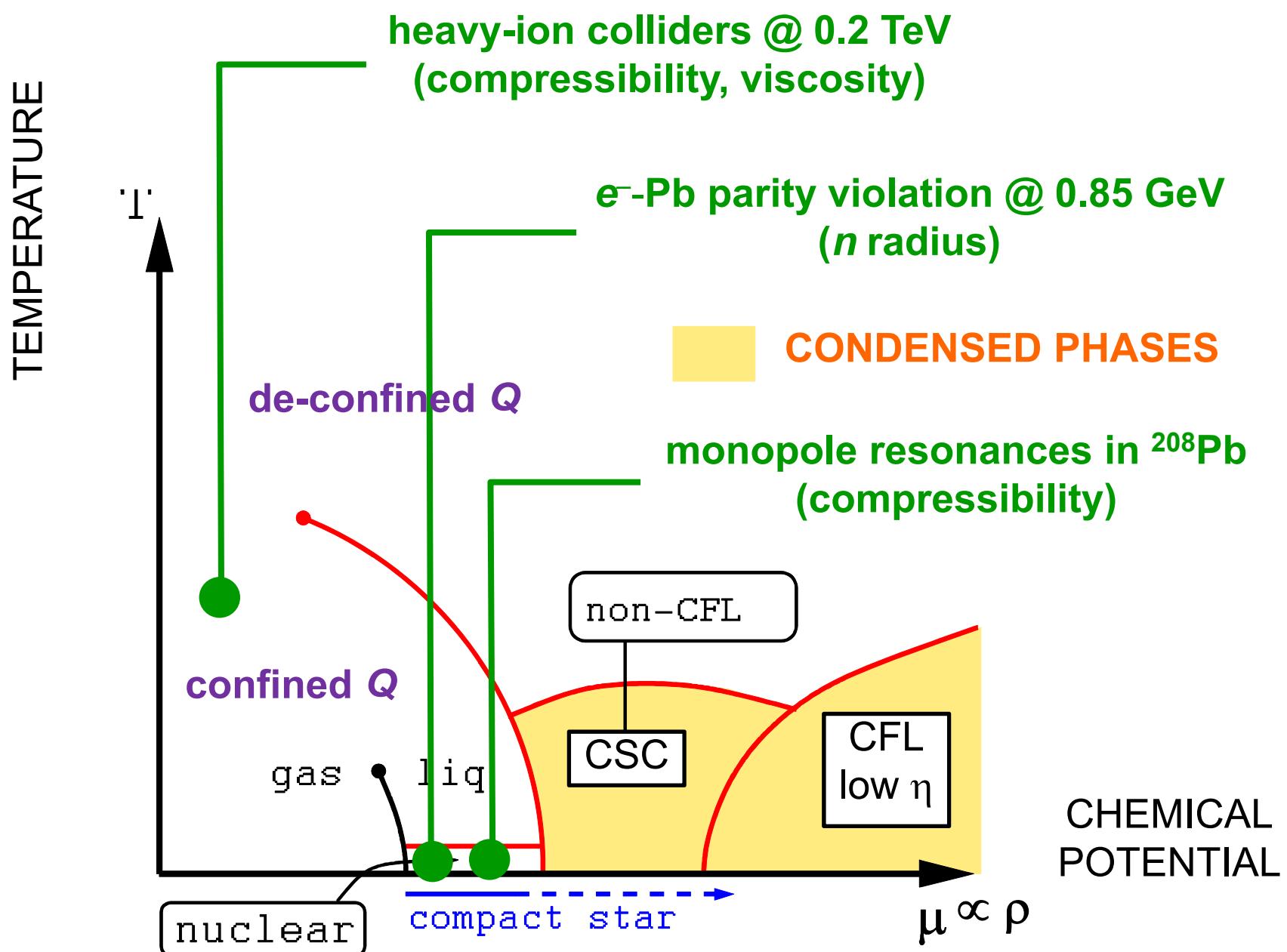
Radio



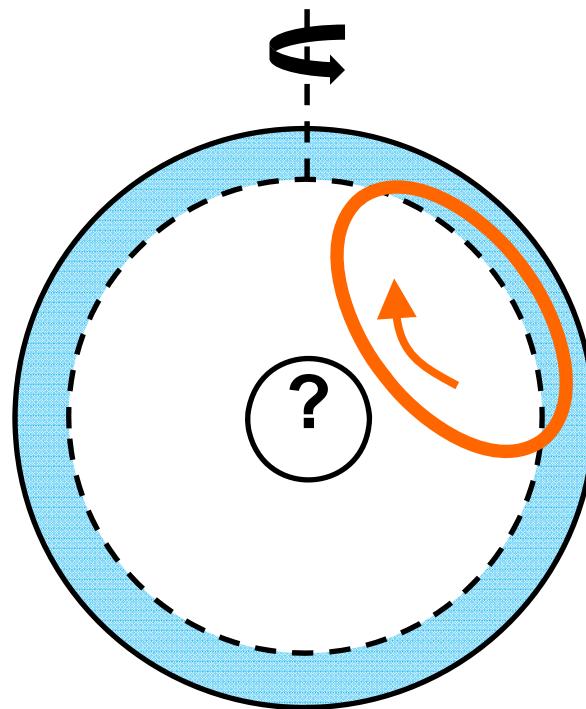
GW

NUCLEAR EXPERIMENTS

Multi-messenger lessons
from post-glitch recoveries



Interior fluid sucked into
boundary layer, spun down,
then recycled

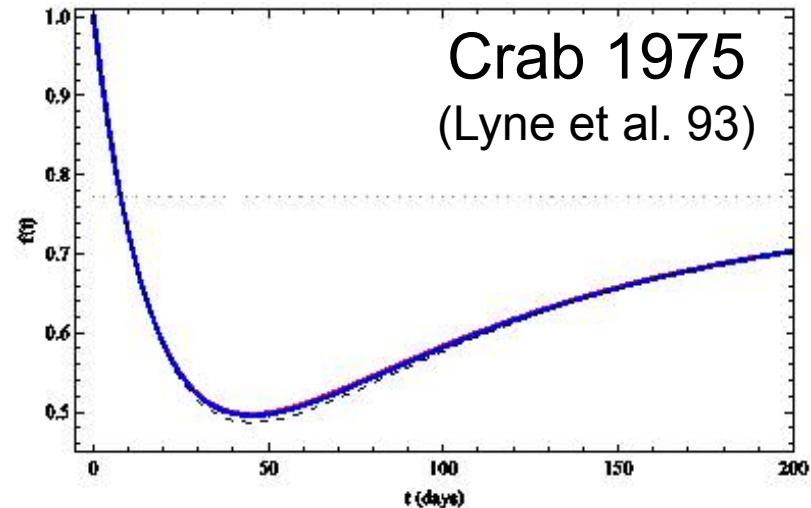
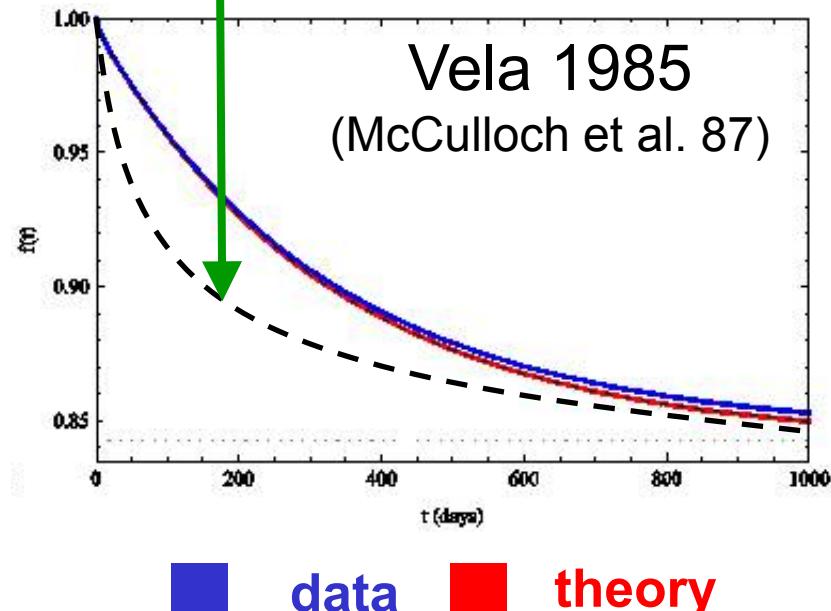


Ekman pumping (“cup of tea”)

- Radio data → **two** time-scales
 - viscous $p^+ - e^-$ component = Ekman circul'n
 - n condensate = mutual friction
- Data inconsistent with magnetic locking
- Theory matches ${}^4\text{He}$ laboratory data to 1% with no free parameters (van Eysden & Melatos 11)

RADIO

single exponential \neq fit!



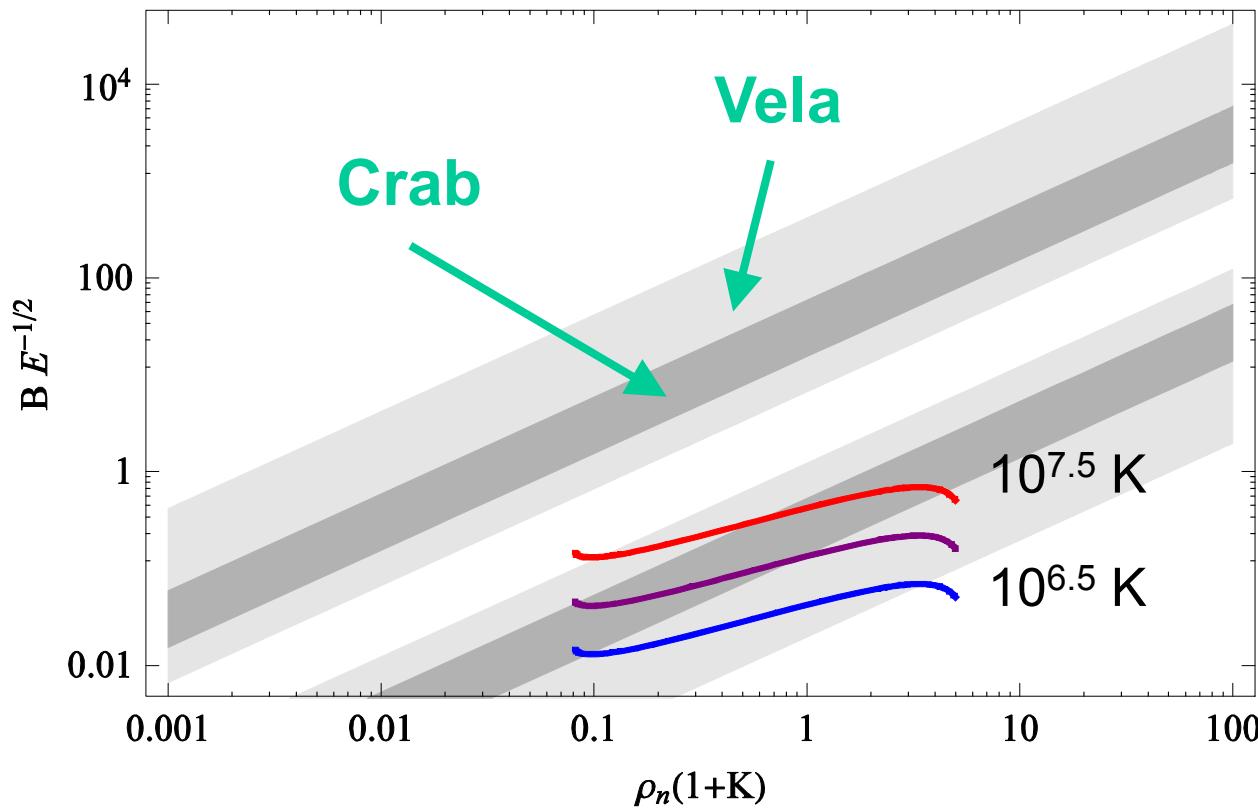
█ data █ theory

- Dual exponentials: Ekman, mutual friction
- Predict **overshoot** if internal lag obeys

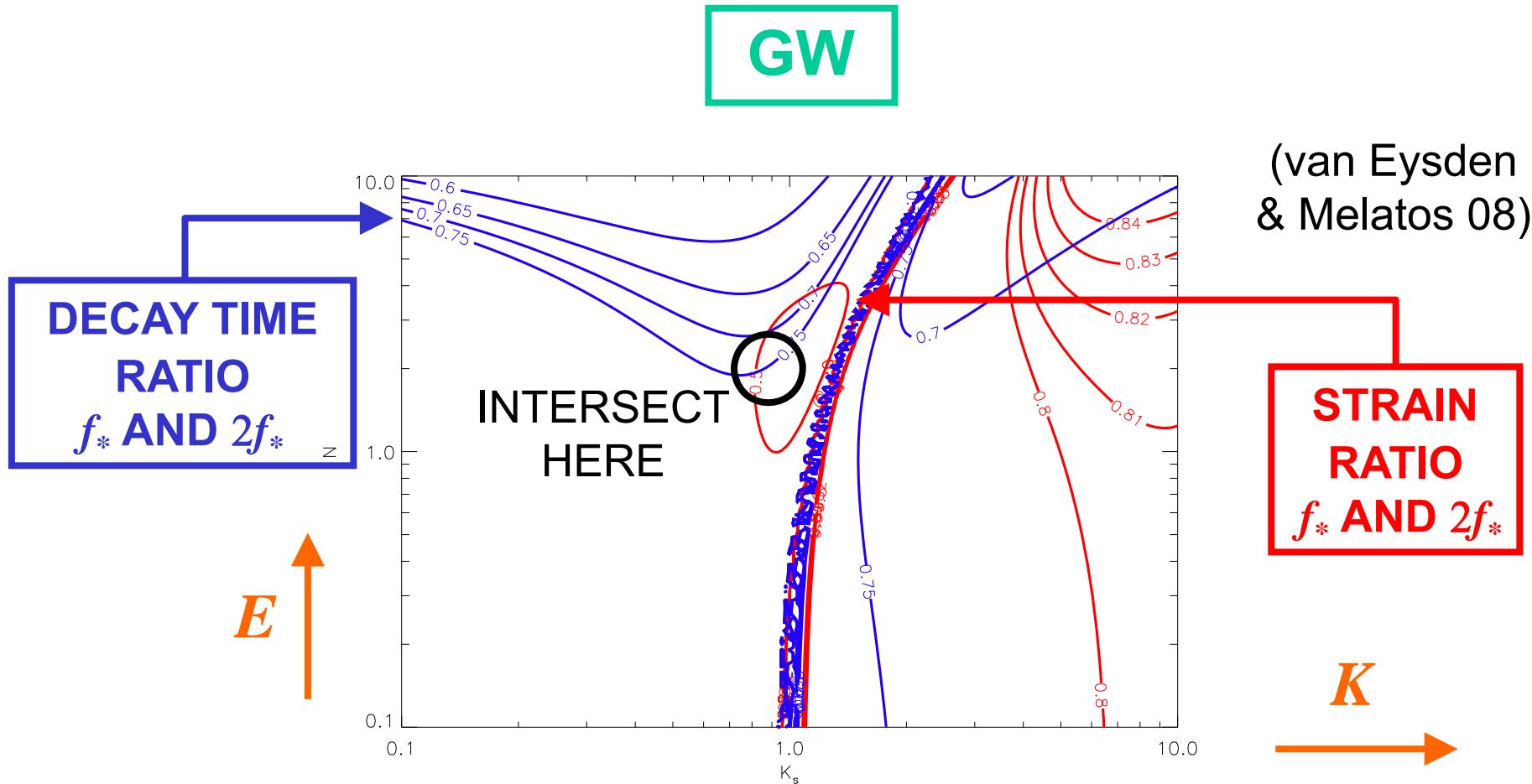
$$\Omega_0 - \Omega_{n0} < \frac{7BE^{-1/2}}{20\rho_n K} - 1$$

RADIO

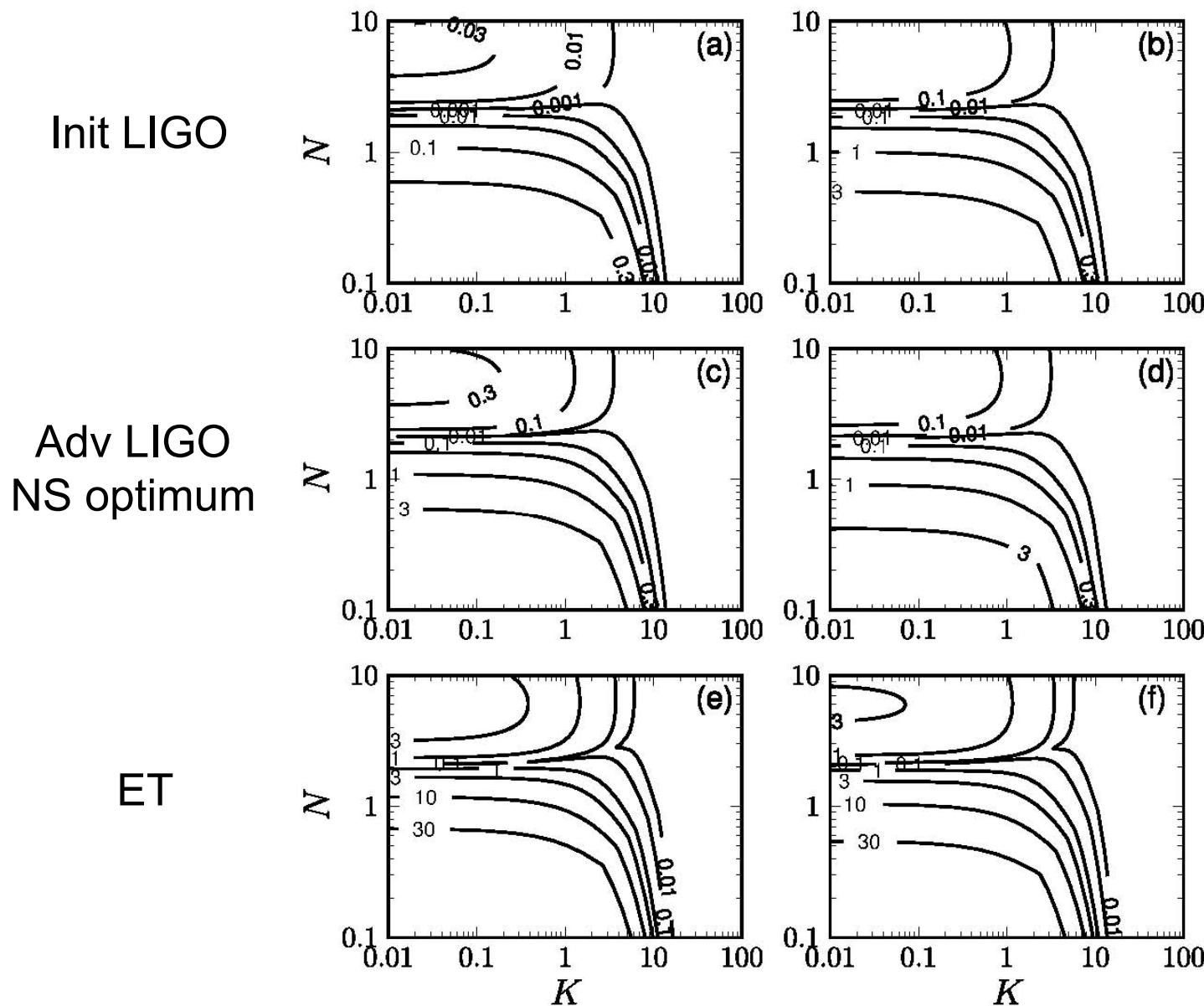
(van Eysden & Melatos 10)



- Good fit for “ordinary” $n-p-e-\mu$ matter
- $BE^{-1/2}$ too low for CFL (cf. 2SC)



- Periodic GW decaying over days to weeks
- Compressibility K , viscosity $E \rightarrow$ boundary layer thickness \rightarrow GW amplitude, decay time



Signal-to-noise contours (Bennett et al. 10)

Adv LIGO
Zero detuning

Adv LIGO
NS optimum

Adv LIGO
BH optimum

ET

ET
Xylophone

Init LIGO

Adv LIGO
Zero detuning

SUPERCONDUCTOR

Differential rotation drives magnetic activity

- **Cas A** cooling $\rightarrow ^1S_0$ protons in core
- Incomplete **type II** Meissner expulsion
 - Fluxoids with quantized magnetic flux $\Phi = \hbar/2e$
 - More fluxoids ($\sim 10^{31}$) than n vortices ($\sim 10^{16}$)
- **Entrainment** (current-current interaction) magnetizes n vortices
 - Opposite-current-carrying wires repel
 - **0.1 GeV** per junction, locked together (maybe...)
- **Maxwell stress** $\sim BH_{c1} \sim 10^3 B^2$

RECENT SC HIGHLIGHTS

- Multifluid “MHD” theory (Glampedakis et al. 11)
- Poloidal-toroidal **equilibria & stability** (Lander 13)
- Matching normal crust \leftrightarrow type II core (Henriksson & Wasserman 13; Sidery & Alpar 09)
- Type I in **macro** domains (Charbonneau & Zhitnitsky 07)
 - Chiral anomaly (e.g. QCD) \rightarrow current **along** fluxoids
 - Attractive force \rightarrow type I for $J > J_{crit}$
 - Cf. fluxoid instability \rightarrow **tangle** when $J < J_{crit}$

- **Magnetar oscillations** (incl. fluxoid cutting & damping) (Gabler et al. 13; Glampedakis & Jones 14)
- Post-glitch, quasiperiodic, **magneto-inertial oscillations** (van Eysden 14; Glampedakis et al. 14)
- Crystalline **color superconducting** core: shear modulus, gravitational waves, cooling (Alford et al. 08; Glampedakis et al. 12; Negreiros et al. 12)
- Indirect spin-down limit on **GWs** from **buried type II** field in MSPs (Mastrano & Melatos 12)