

Importance of stellar oblateness and relativistic effects on accretion disks around compact stars.

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1 Quasi-periodic Oscillations

- High Frequency QPOs
- Models of High Frequency QPOs

2 Assumptions

- Neutron Star and Strange Quark Star model
- Mass-Radius relation for NS and SQS
- Numerical code

3 Epicyclic frequencies around Strange Quark Stars

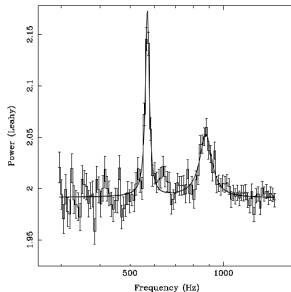
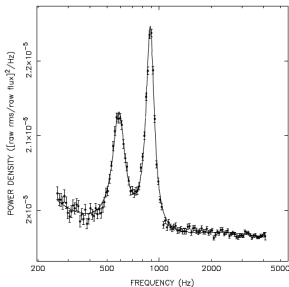
- Moderate-mass Strange Quark Stars

4 Epicyclic frequencies around Neutron Stars

High Frequency Quasi-periodic Oscillations

The kHz Quasi-periodic oscillations (**kHz QPOs**) are among the most important scientific result of Rossi X-ray Timing Explorer (RXTE)

<http://heasarc.gsfc.nasa.gov/docs/xte/GreatestHits/khz.qpo.html>

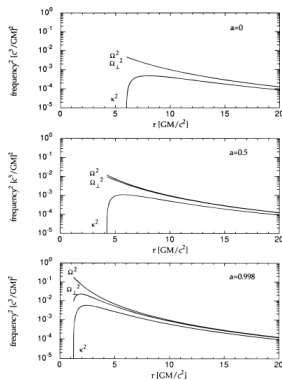


Twin kHz peaks in Sco X-1 (left; van der Klis et al. 1997) and 4U 1608-52 (right; Mendez et al. 1998)

To date kHz QPOs have been discovered in ~ 26 neutron star LMXBs (Wang et al. 2014) - mostly showing double peaks (ν_1, ν_2): 0.1-1.33 kHz (van der Klis 2000)

Models of HF QPOs

Many different models try to explain the **origin of kHz QPOs**. Most of them involve orbital Ω_{orb} and epicyclic (Ω_r , Ω_{vert}) frequencies. **Examples:** Stella et al. 1999 (Ω_{orb} , $\Omega_{orb} - \Omega_r$), Abramowicz and Kluźniak, 2003 (Ω_{vert} , Ω_r)



Perez et al. 1997

The effect of spin on the epicyclic frequencies around black hole:

- Newtonian $1/r$ gravity:
 $\Omega_{orb} = \Omega_r = \Omega_{vert}$.
- GR, Schwarzschild:
 $\Omega_r < \Omega_{orb}$
- GR, Kerr:
 $\Omega_{vert} < \Omega_{orb}$ (prograde)

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MIT bag model

- quark matter is composed of massless u, d quarks, massive s quarks and electrons.
- three physical quantities describing the model: the mass of strange quark, m_s , the bag constant B , and the strength of QCD coupling constant, α .

The equation of state is given by simple formula:

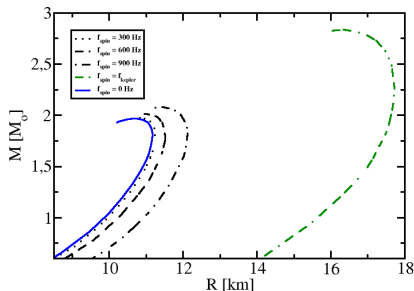
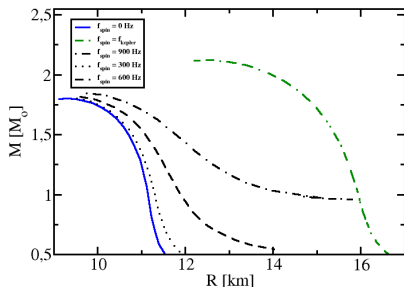
$$P = a(\rho - \rho_0)c^2$$

where P is the pressure, ρ the mass-energy density, and c is a speed of light.

FPS equation of state

- tabulated equation of state of Neutron Star
- developed by Friedman, Pandharipande and Skyrme (Pandharipande and Ravenhall 1989).

Mass-Radius relation for NS and SQS



Gravitational mass (in the units of the mass of Sun) versus **equatorial radius** in kilometers for neutron stars described by the FPS equation of state (left panel) and strange quark stars described by the MIT bag model (right panel). The **blue solid line** corresponds to **static case**, the **green line** corresponds to **keplerian limit**, the **black dotted line** correspond to configurations with spin frequency **300 Hz**, the **black dashed line** corresponds to configurations with spin frequency **600 Hz** and the **black dotted-dashed line** corresponds to configurations with spin frequency **900 Hz**.

- We have calculated axisymmetric models of strange quark stars and neutron stars and their exterior metrics using a highly accurate relativistic code, **RNS** (Stergioulas and Friedman 1995, see Stergioulas 1998 for a description)
- the equilibrium models are obtained following KEH method (Komatsu et al. 1989), in which the field equations are converted to integral equations using appropriate Green's functions.
- We have computed the metric outside uniformly rotating neutron stars and strange quark stars of masses and rotation rates typical for LMXBs.

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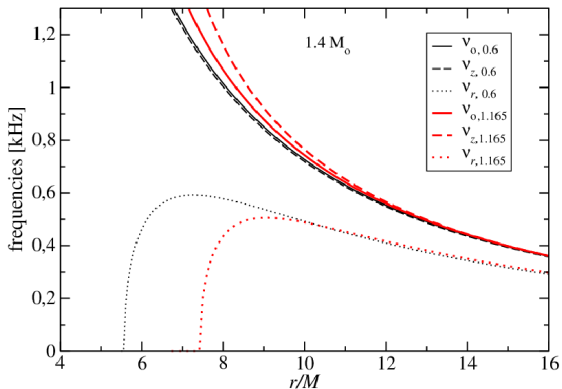
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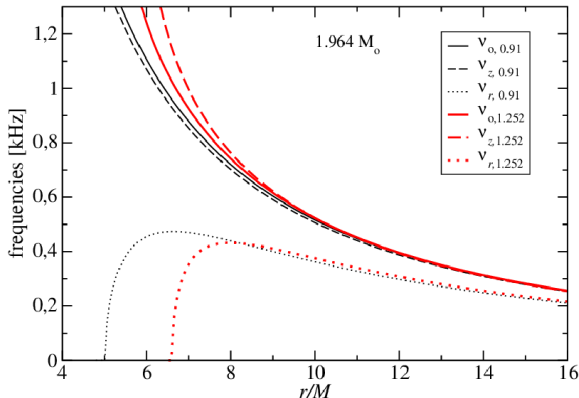
1.4 M_{\odot} Strange Quark Star



Orbital and epicyclic frequencies versus radius (scaled with gravitational stellar mass M) for numerical models of an $M = 1.4M_{\odot}$ uniformly rotating **strange quark star** rotating at a fixed frequency, **600 Hz** (thin black lines) and **1165 Hz** (thick red lines).

Gondek-Rosińska, Kluźniak, Stergioulas, Wiśniewicz, 2014

1.964 M_{\odot} Strange Quark Star



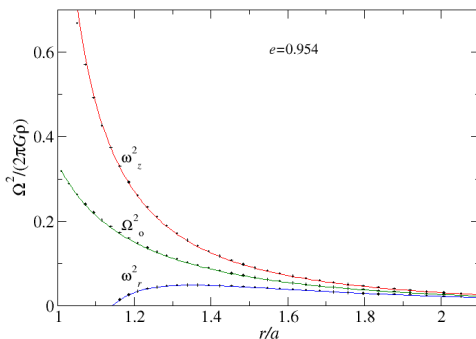
Orbital and epicyclic frequencies versus radius (scaled with gravitational stellar mass M) for numerical models of an $M = 1.964M_{\odot}$ uniformly rotating **strange quark star** rotating at a fixed frequency, **910 Hz** (thin black lines) and **1252 Hz** (thick red lines).

Gondek-Rosińska, Kluźniak, Stergioulas, Wiśniewicz, 2014

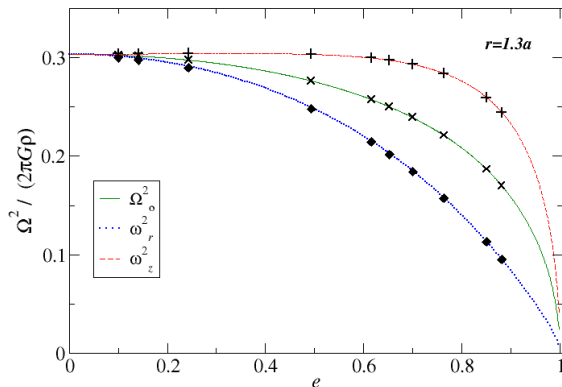
Orbital and epicyclic frequencies in Newtonian gravity (Maclaurin spheroids)

ISCO exists in the Newtonian Theory for $e > e_{\text{crit}} = 0.83458$ - Amsterdamski, Bulik, Gondek-Rosińska, Kluźniak, 2002 (analytic formulae), Zdunik & Gourgoulhon, 2001

Ω_{vert} **always higher** than Ω_{orb} , and $\Omega_{\text{vert}}^2 + \Omega_r^2 = 2\Omega_{\text{orb}}^2$ (Kluźniak & Rosińska, 2013)



Orbital and epicyclic frequencies in Newtonian gravity



symbols - numerical results of RNS **relativistic code** for $M = 0.001 M_{\odot}$ **strange quark stars**
Gondek-Rosińska, Kluźniak, Stergioulas, Wiśniewicz, 2014

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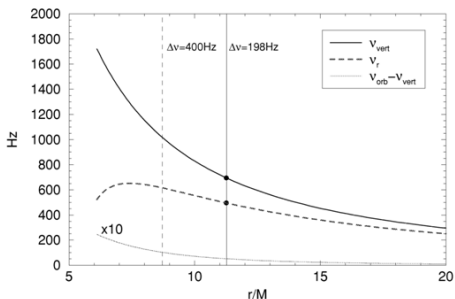
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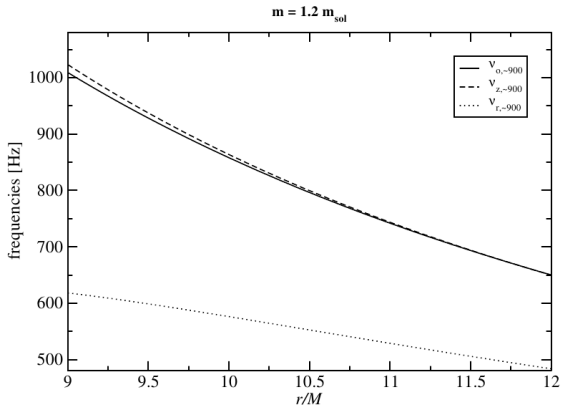
4 Epicyclic frequencies around Neutron Stars

Previous studies - Epicyclic frequencies around $1.22M_{\odot}$ neutron star (Kluźniak et al. 2004)



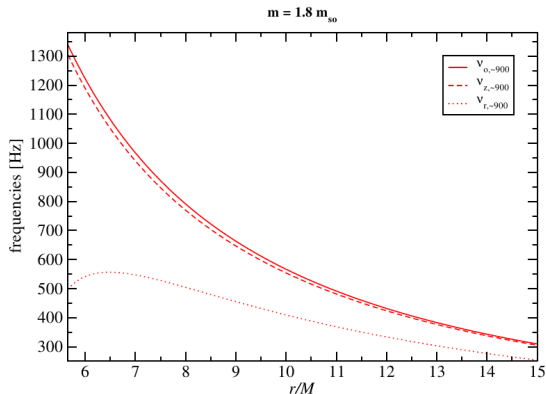
The effect of rotation on the epicyclic frequencies in numerical solutions for a $1.22 M_{\odot}$ neutron star (FPS) rotating at **400 Hz** has been clearly seen in the unusually small difference $\Omega_{orb} - \Omega_{vert} \simeq 0$ between the orbital frequency and the vertical epicyclic one (Kluźniak et al. 2004)

1.2 M_{\odot} Neutron Star



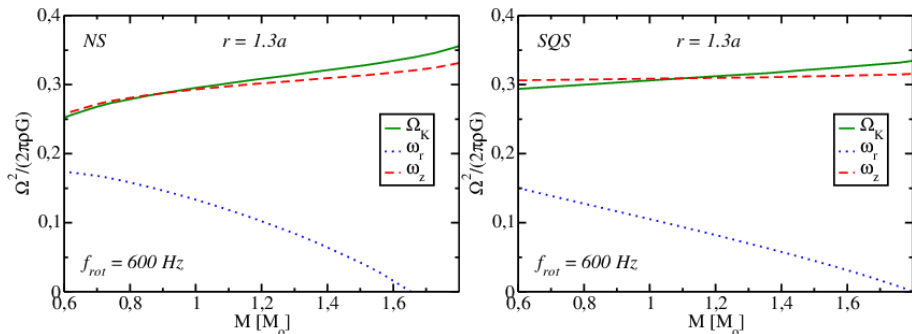
Orbital and epicyclic frequencies versus radius for numerical models of an $M = 1.2 M_{\odot}$ neutron star uniformly rotating at ~ 900 Hz.

1.8 M_{\odot} Neutron Star



Orbital and epicyclic frequencies versus radius (scaled with gravitational stellar mass M) for numerical models of an $M = 1.8 M_{\odot}$ uniformly rotating **neutron star** rotating at a fixed frequency, ~ 900 Hz.

Epicyclic frequencies for Neutron Stars and Quark Stars



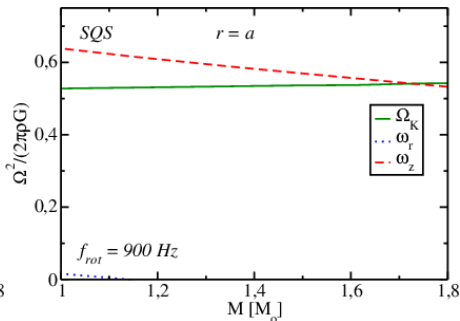
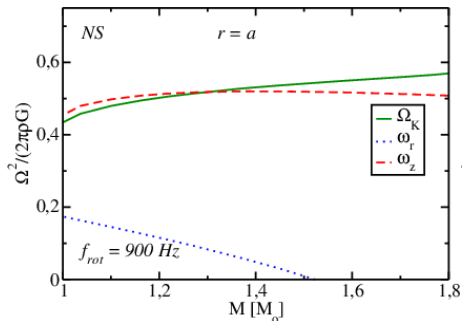
Frequencies (squared) at $r = 1.3a$ versus gravitational mass for **neutron stars** (left panel), and **quark stars** (right panel), rotating at **600 Hz**.

The solid green line: orbital frequency.

The dashed red line: vertical epicyclic frequency.

The dotted blue line: radial epicyclic frequency.

Epicyclic frequencies for Neutron Stars and Quark Stars



Frequencies (squared) at $r = a$ versus gravitational mass for **neutron stars** (left panel), and **quark stars** (right panel), rotating at **900 Hz**.

The solid green line: orbital frequency.

The dashed red line: vertical epicyclic frequency.

The dotted blue line: radial epicyclic frequency.

- Stellar spin has two opposing effects on epicyclic frequencies: **frame dragging** vs. **stellar oblateness**
- Frame dragging decreases the vertical epicyclic frequency and increases the radial epicyclic frequency of prograde orbits
- Stellar oblateness increases the vertical frequency and decreases the radial epicyclic frequency
- In rapidly rotating strange quark stars and **neutron stars** the effects of oblateness dominate the behavior of the vertical epicyclic frequency near the star. The effect is also visible in rapidly rotating neutron stars.

THANK YOU FOR YOUR ATTENTION!