

Rotation and stability of neutrons stars with strong phase transitions

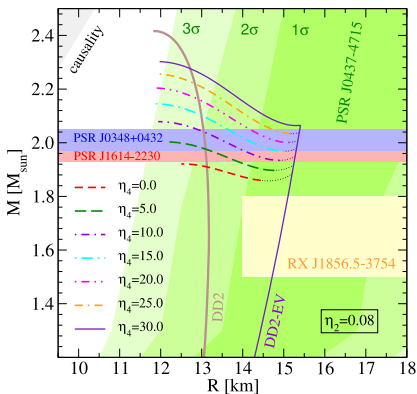
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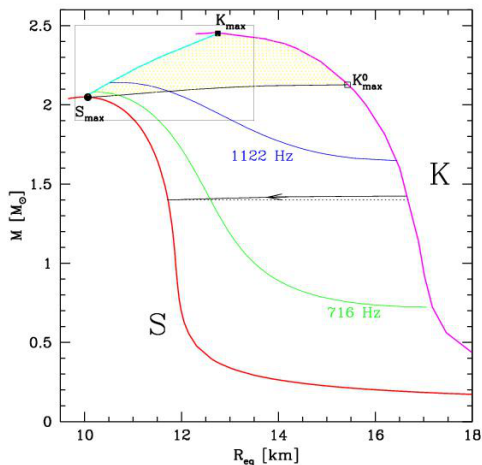


Quark-core twins – rotating configurations and their stability

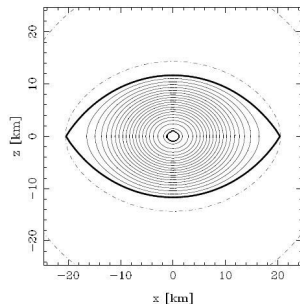


- ★ Since PSR J1614-2230 and PSR J0348+0432, the discussion about exotic (beyond $npe\mu$) dense matter is really interesting
- ★ „A new quark-hadron hybrid equation of state for astrophysics - I. High-mass twin compact stars”, Benić et al. (2015) arXiv:1411.2856
 - Exotic quark phase is related to massive NSs.
- ★ Here - remarks about the stability of rotating configurations with relation to astrophysics (using DD2-EV $\eta_2 = 0.12$, $\eta_4 = 5$ EOS)
- ★ results from LORENE/rotstar.

Rotation on the $M(R)$ diagram



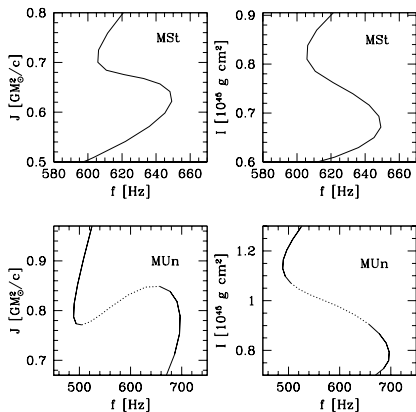
- ★ S: static configurations (TOV),
- ★ K: "Keplerian" (mass-shedding) configuration - maximally-rotating, rigid stars at a given mass,



- ★ in cyan: the instability line (star loses stability w.r.t. axisymmetric oscillations)★

Stability indicators: J and M_b

Sufficient condition for instability (turning-point criterion):
Sorkin (1981, 1982), Friedman et al. (1988)★



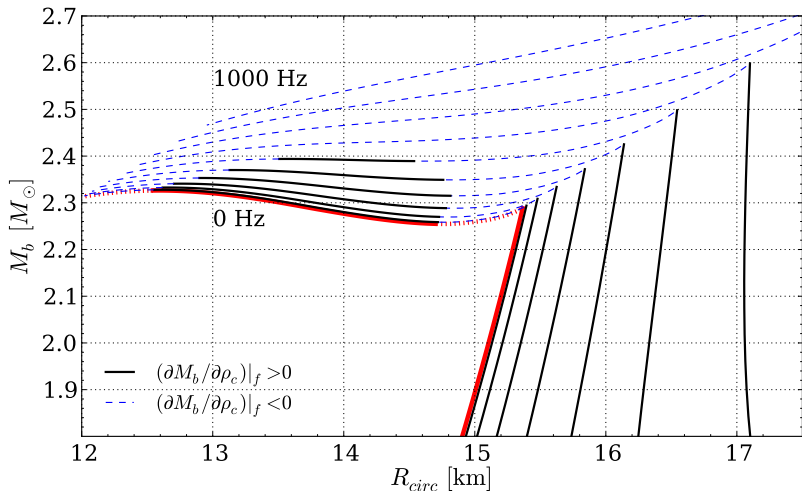
- ★ *Change in stability* corresponds to extremum of M or M_b at fixed J , or to extremum of J at fixed either M or M_b :

$$\left(\frac{\partial M_b}{\partial \lambda_c}\right)_J = 0, \quad \left(\frac{\partial J}{\partial \lambda_c}\right)_M = 0,$$

- ★ *Back-bending* is related to the existence of a minimum of M_b along $f = \text{const.}$ sequence,
- ★ **Conjecture:** character of stability persists for all rotation rates (A&A **450**, 2006, 747)

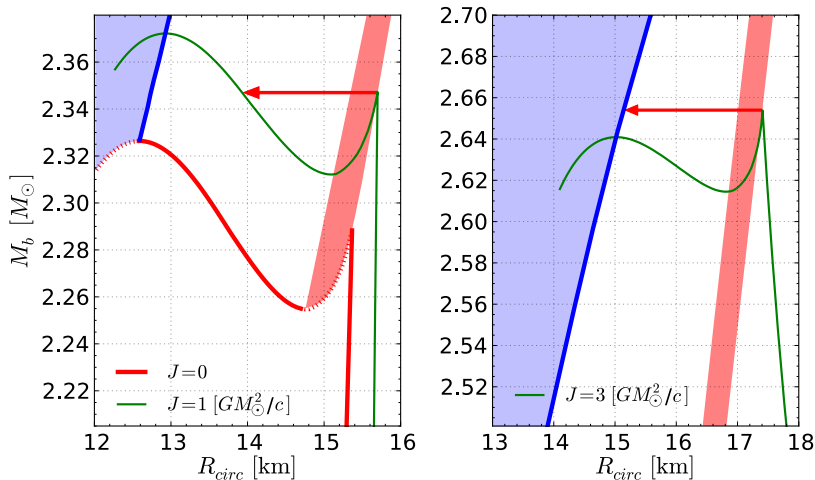
★ However, see Takami et al. (2011) for comparison with dynamical calculations

$f = \text{const.}$ curves on $M_b(R)$ plane



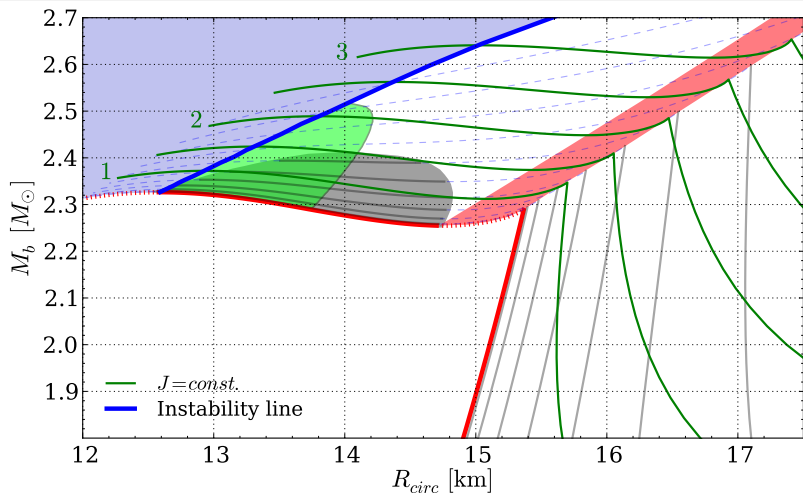
→ Dashed lines - *back-bending* is present (NS spins-up while monotonically losing angular momentum)

$J = \text{const.}$ curves, loss of stability and critical angular momentum J



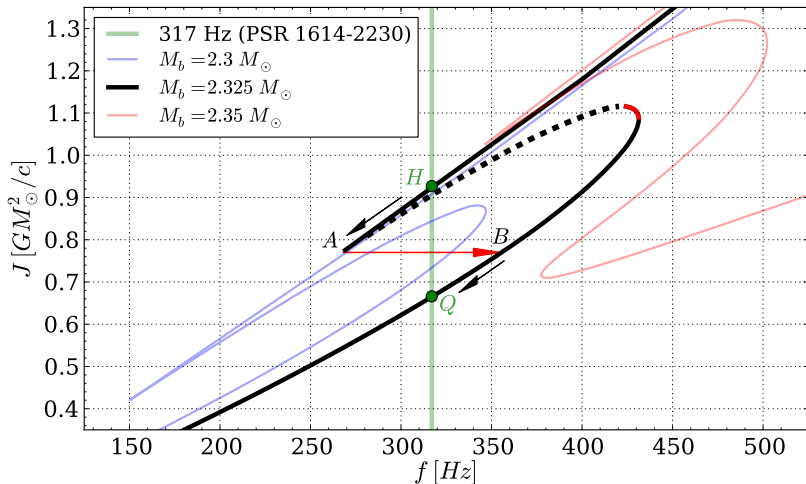
Analysis of $J = \text{const.}$ sequences: stars with too much angular momentum (e.g., spun-up by accretion) end up in the instability.

$J = \text{const.}$ curves on $M_b(R)$ plane



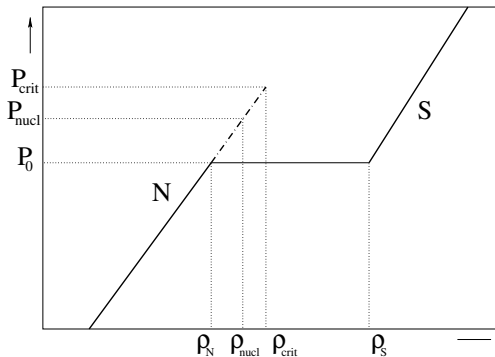
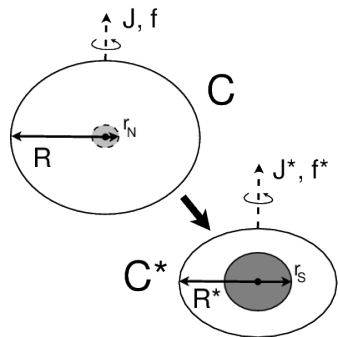
Red region - strong phase-transition instability,
Blue region - unstable w.r.t axisymmetric oscillations,
Grey region - no back-bending,
Green region - stable twin branch reached after the mini-collapse from the tip of $J = \text{const.}$ curve, along $M_b = \text{const.}$

$M_b = \text{const.}$ curves on $J(f)$ plane



For NSs with measured gravitational mass M and frequency - possibility to put limits on M_b , J , moment of inertia I , core EOS composition etc.

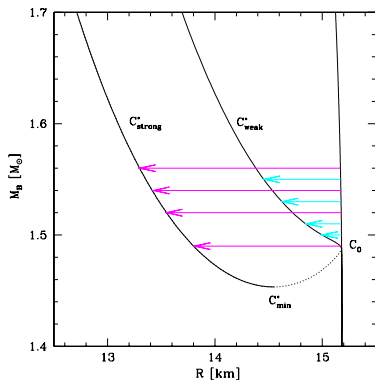
Energy release (A&A 479, 2008, 515)



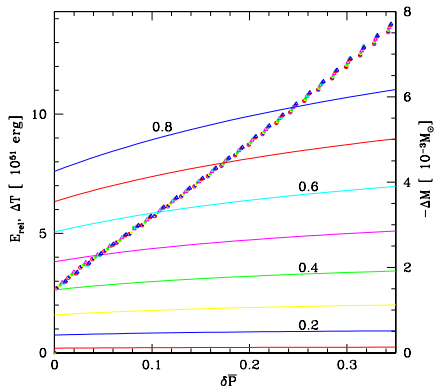
Strong phase transition if

$$\rho_S / \rho_N > \frac{3}{2} (1 + P_0 / \rho_N c^2)$$

Energy release (A&A 479, 2008, 515)



Strong phase transition if
 $\rho_S / \rho_N > \frac{3}{2}(1 + P_0 / \rho_N c^2)$



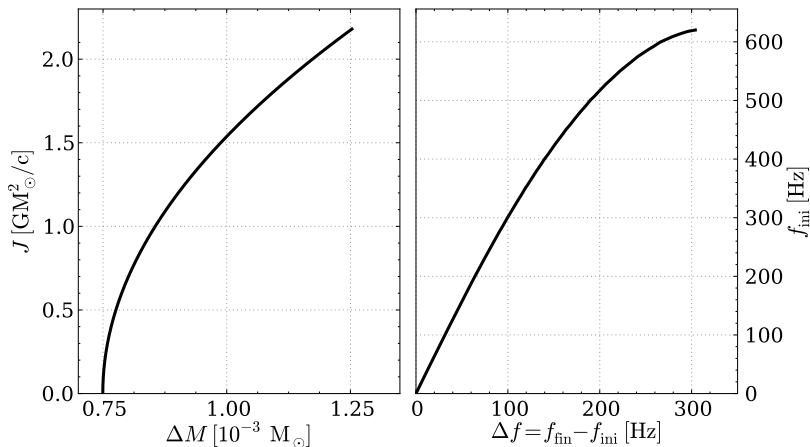
Angular momentum

$J = 0.1, \dots, 0.8 \times GM_{\odot}^2 / c,$

Energy release $E_{\text{rel}} = (M - M^*)c^2,$

Kinetic energy $\Delta T = T^* - T.$

Energy release in case of DD2-EV $\eta_2 = 0.12$, $\eta_4 = 5$ EOS

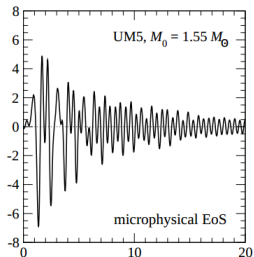
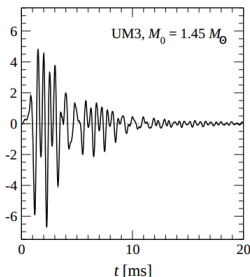
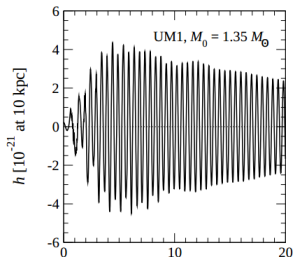
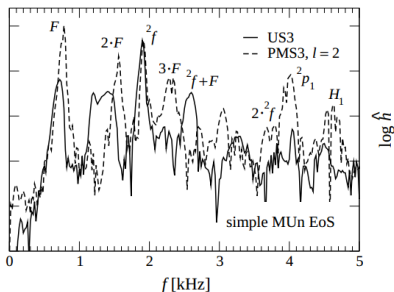


Left panel: energy release (difference in the gravitational mass) vs J of the configuration entering the strong phase-transition instability.

Right panel: spin-up Δf (difference between the final and initial spin frequency) against the spin frequency of the initial configuration.

Burst-like GW emission (MNRAS 502, 2009, 605)

Time evolution of a dynamical mini-collapse induced by a phase transition (simulations with the CoCoNuT code)



Instability in the EOS

- ★ bypasses back-bending regions,
- ★ provides a "natural" spin frequency cut-off at some moderate (but >716 Hz) frequency,
- ★ resembles Fast Radio Burst 'blitzar' engine (Falcke & Rezzolla 2014):
 - ★ catastrophic mini-collapse to the second branch (or to a black hole),
 - ★ massive rearrangement of the magnetic field \rightarrow energy emission.

Other astrophysically-interesting questions:

- ★ Way to constraint on M_b , J , I , core EOS etc.,
- ★ Specific shape of NS-BH mass function (no mass gap?)
- \rightarrow population of massive, low B-field NSs (radio-dead?),
- \rightarrow population of massive, high B-field NSs (collapse enhances the field?),
- ★ Characteristic burst-like signature in GW emission during the mini-collapse.