

# Laser plasma diagnostics in rubidium vapor cell

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# Motivation and issues found in measurements

- Plasma generation in Rb vapor by ultrashort laser pulses
- Plasma diagnostics by CW diode lasers: plasma density

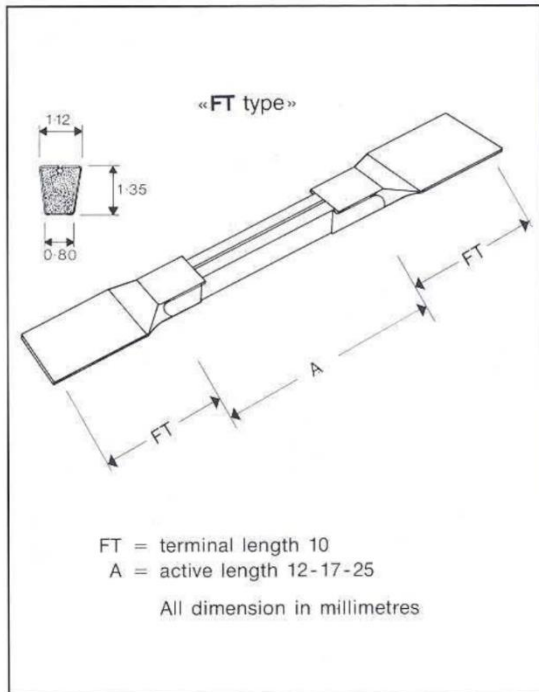
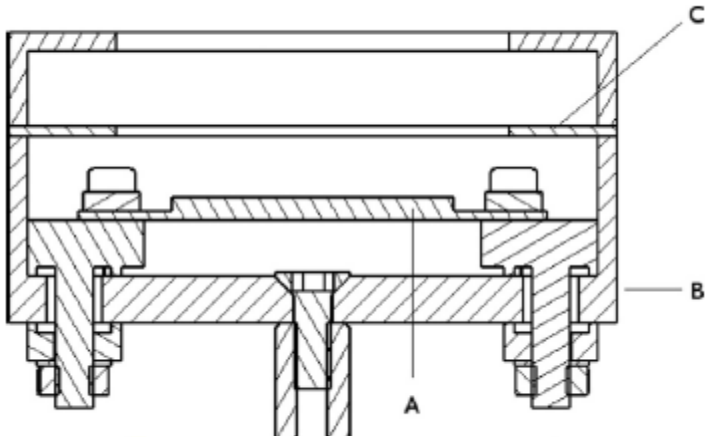
Why rubidium cell?

Easily vaporized Rb  
Convenient spectral lines  
780nm  
Vapor density simply  
controllable by temperature

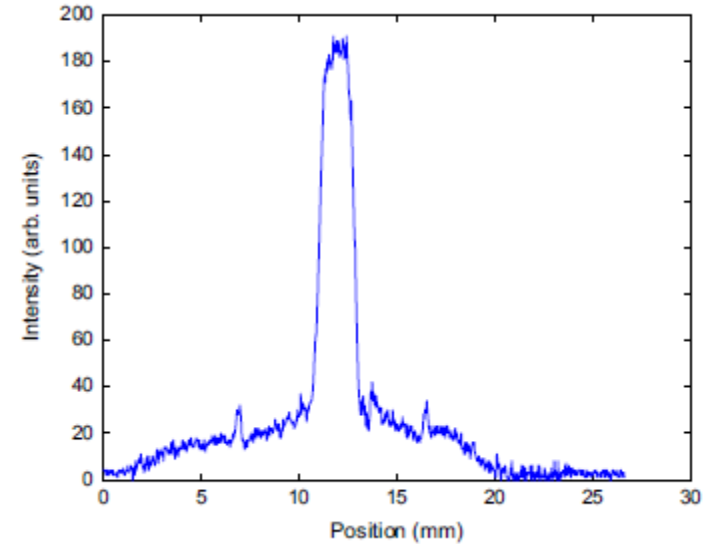
Why diode laser?

Commercially available  
Cheap (CD writer 780nm)  
Simple to operate  
Easy frequency tuning

# Another simple plasma source



Rb vapor source .  
getter @ double  
slit



Rb vapor distribution  
above the slit

# Direct way of plasma diagnostics: collecting charged particles

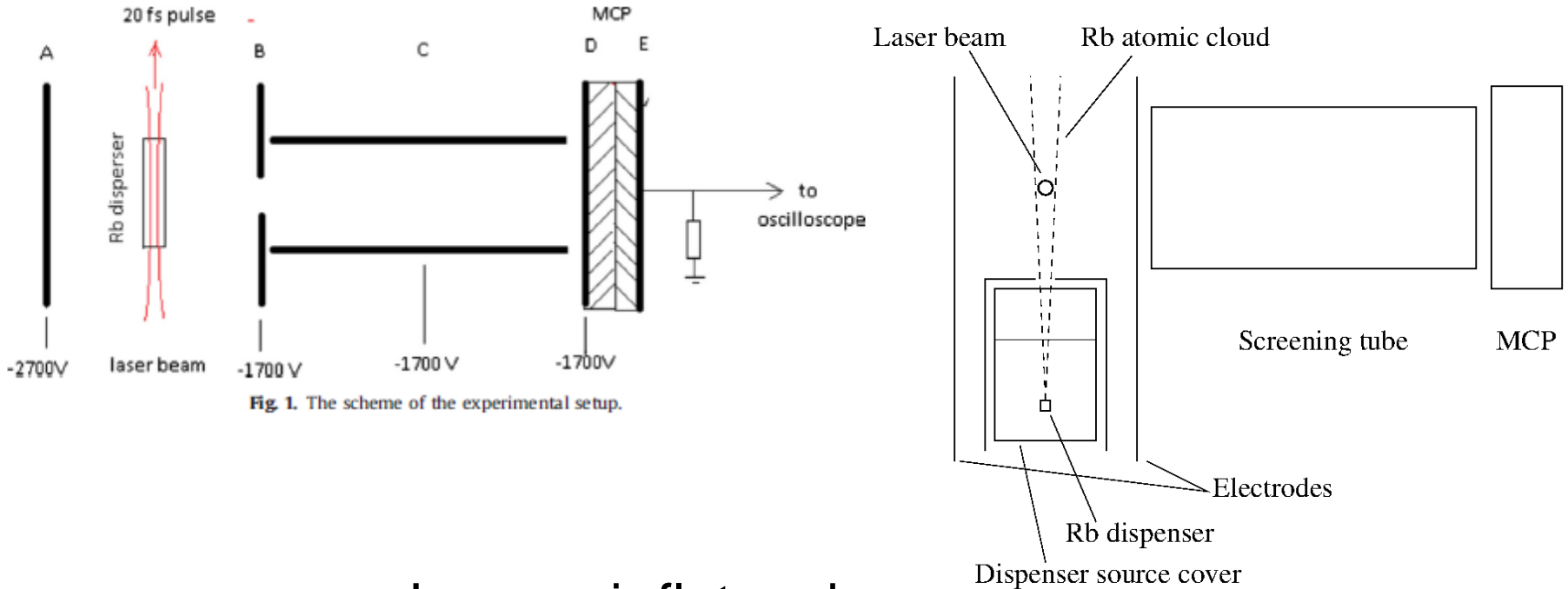


Fig. 1. The scheme of the experimental setup.

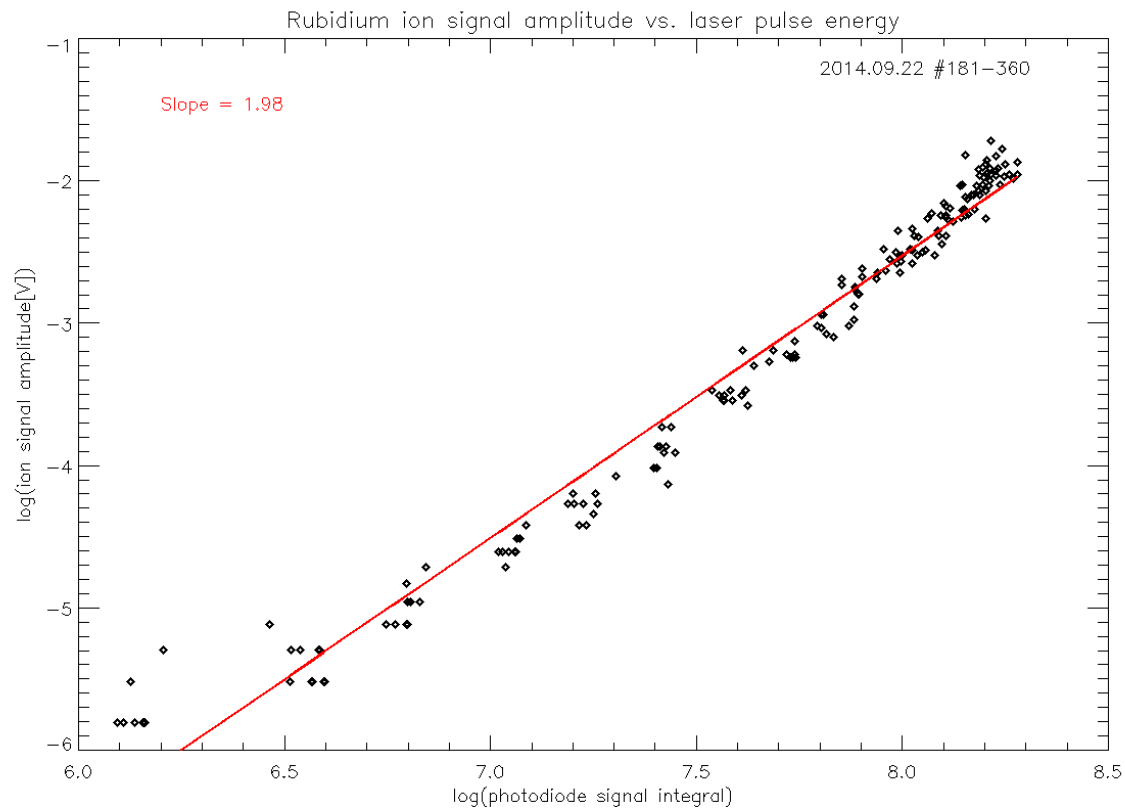
Langmuir flat probe:

1. Simple design
2. Ions/electrons come from 'somewhere', calibration difficulties

# Results of direct ion detection

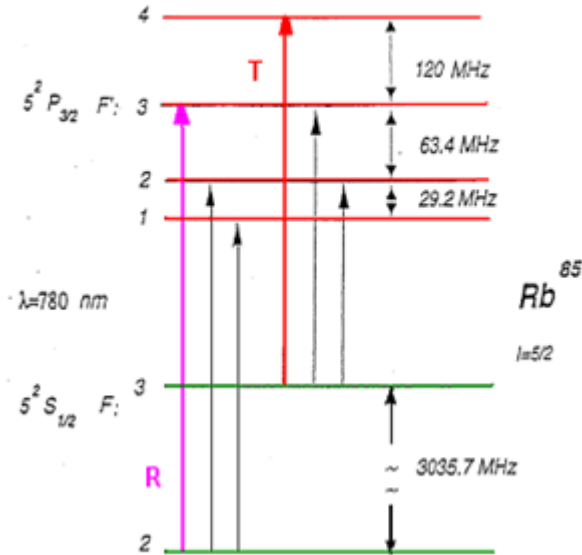
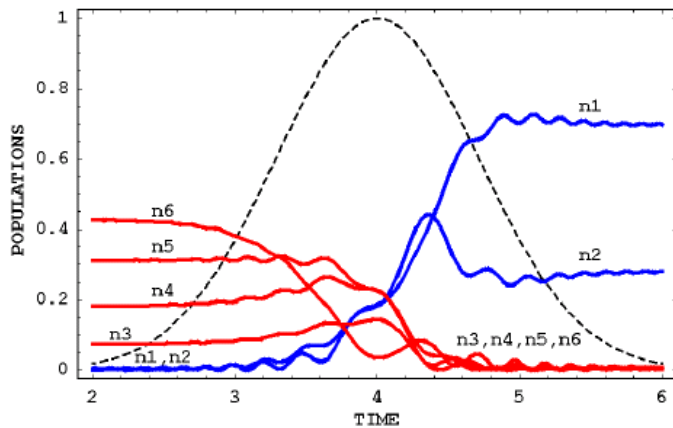
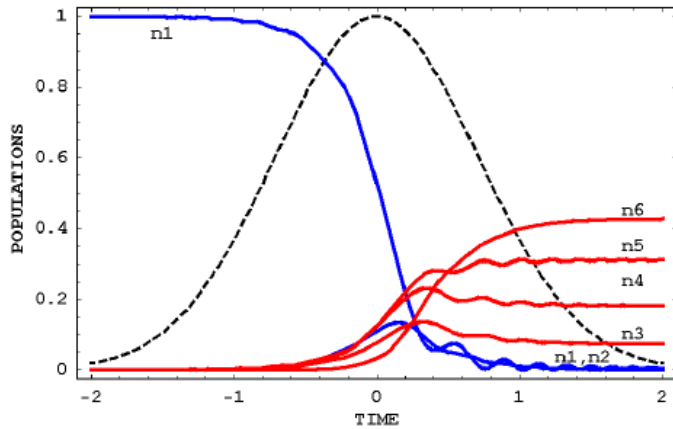
ionization dependence on laser intensity

Slope:  $\sim 2$



Maximum laser intensity:  $10^{11}$  W/cm<sup>2</sup>

# Indirect plasma diagnostics: plasma = 'lack' of neutral atoms

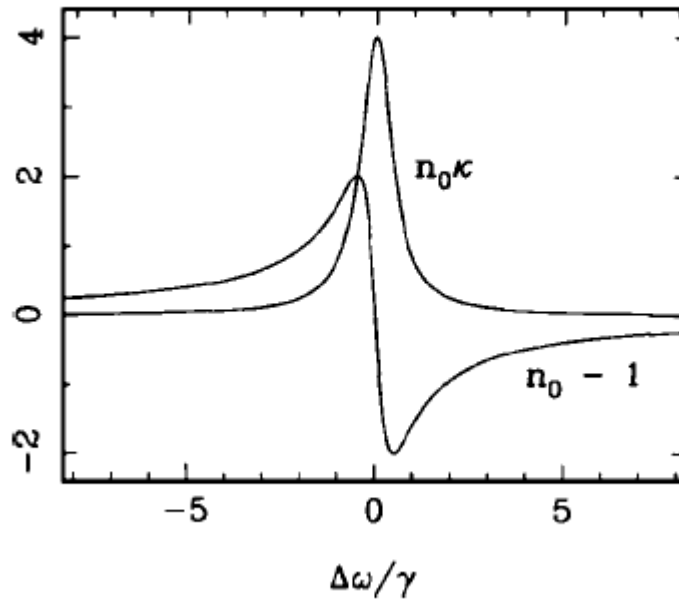


Atomic processes:  
Decay time some 10 ns

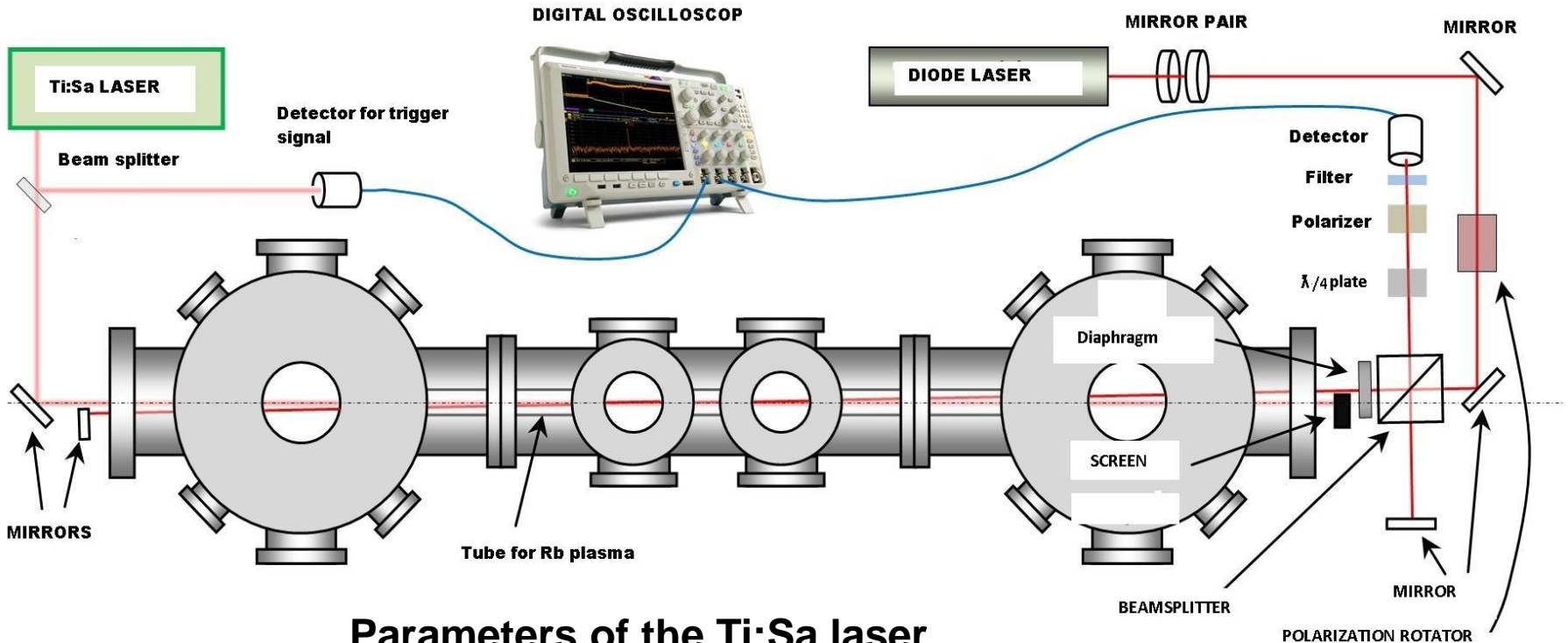
Population dynamics for a pair of resonant pulses

# Plasma diagnostics by CW diode lasers

Atomic Lorentz model:  
resonant absorption @  
interferometry



# Experimental layout



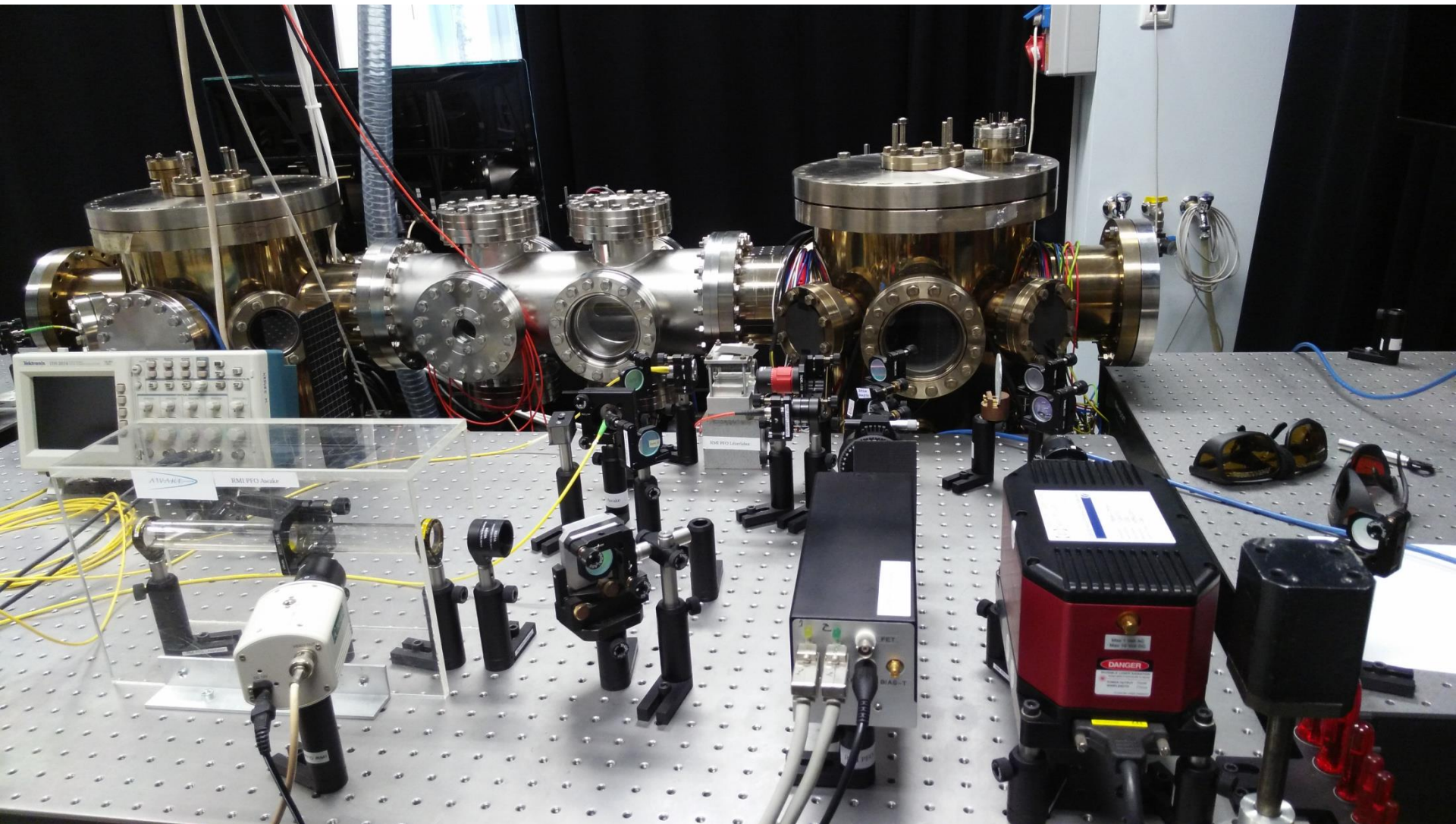
## Parameters of the Ti:Sa laser

Mean wavelength 806 nm  
 Beam Diameter: 9 mm (1/e<sup>2</sup>Gauss)  
 Polarisation: Linear, vertical  
 Repetition Rate 1 kHz  
 Pulse duration (FWHM): 35 fs  
 Pulse 3.5 mJ

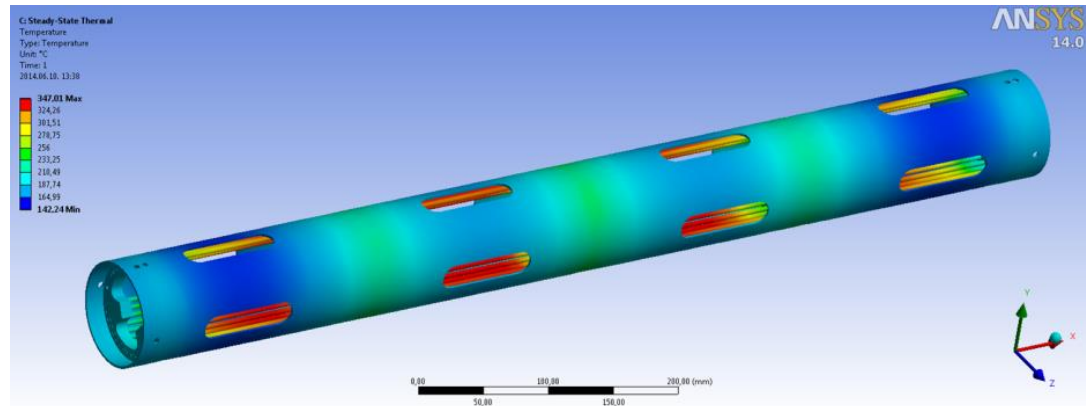
Courtesy of  
 A. Czitrovsky, P. Dombi,  
 P. Rácz, A. Nagy, I. Márton



# Experimental layout



# Vapor cell, heating wires, reflector



Temperature  
distribution

Courtesy  
A. Bendefy (BME)

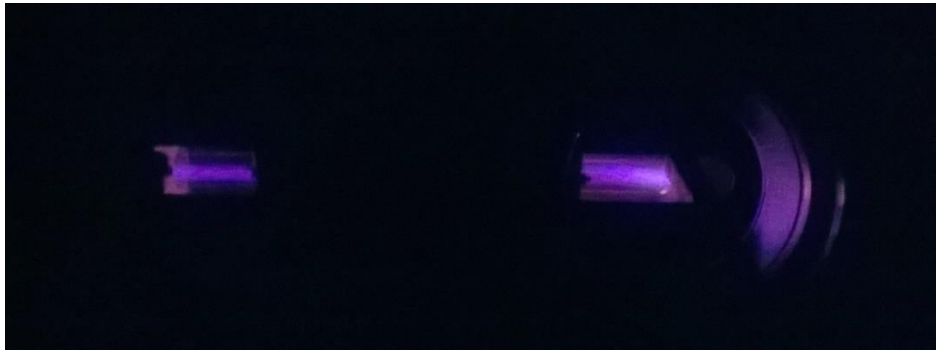
# Spectroscopic observations

Detection of the radiation of the plasma by a fast spectrograph (Andor Mechelle 5000)

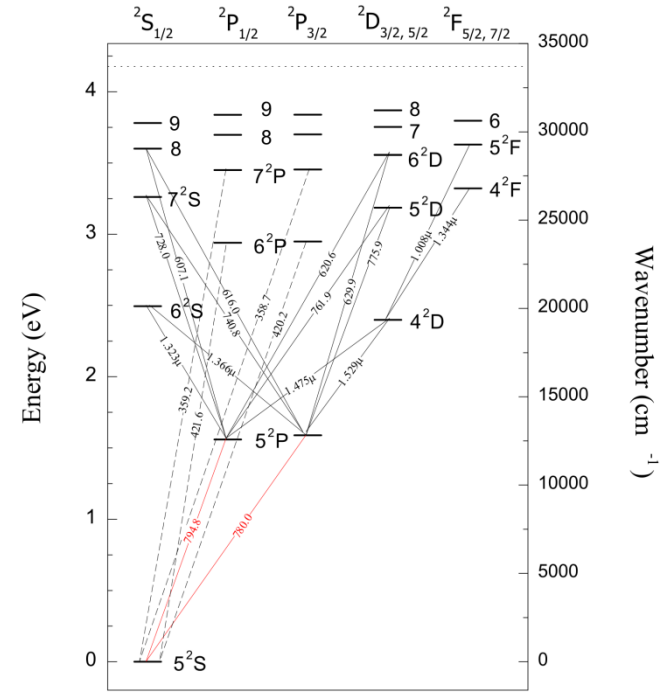
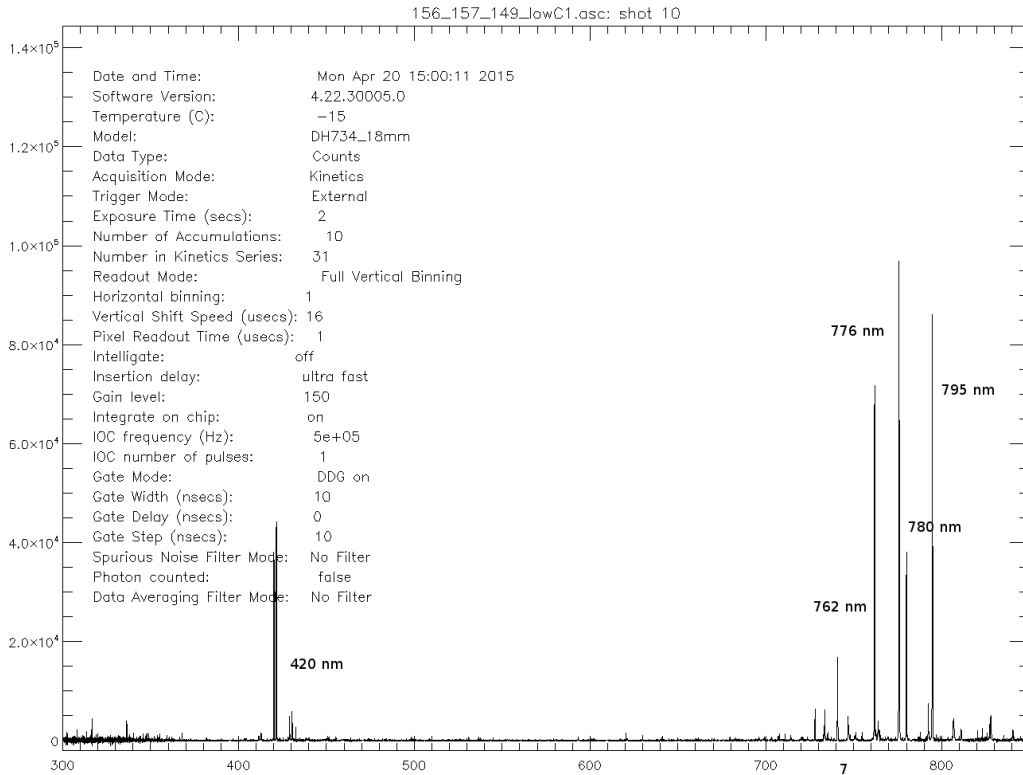
High spectral resolution (0.05 nm accuracy)

High temporal resolution with intensified camera ( $\sim$  ns)

Spectrograph courtesy of L. Kocsányi (BME), and help with the measurements R. Bolla (WRCP)



# Observed spectral lines of Rb



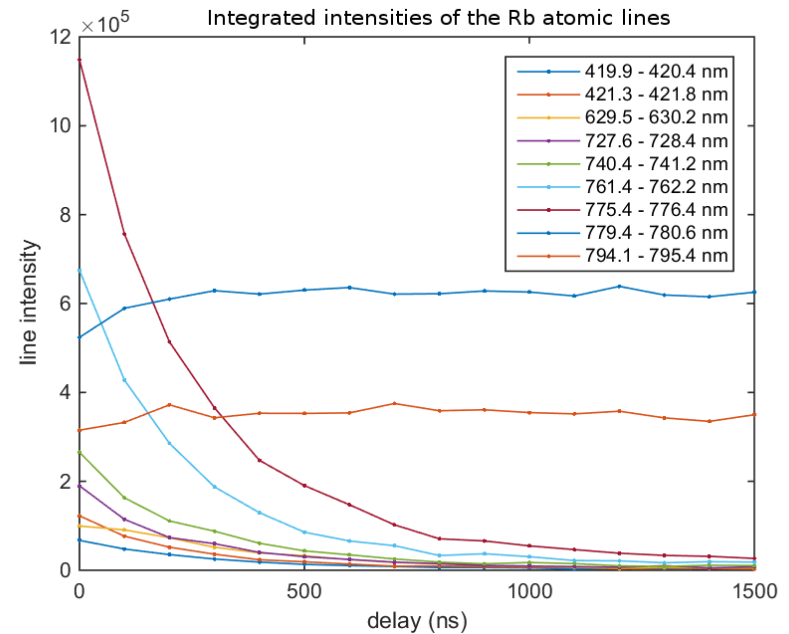
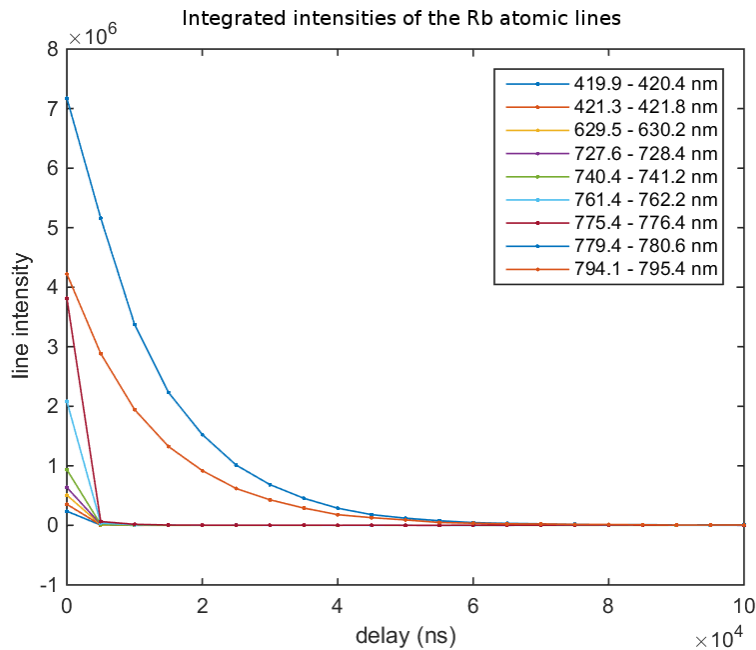
## Rubidium

Z : 37

Ioniz. Pot. : 4.176 eV

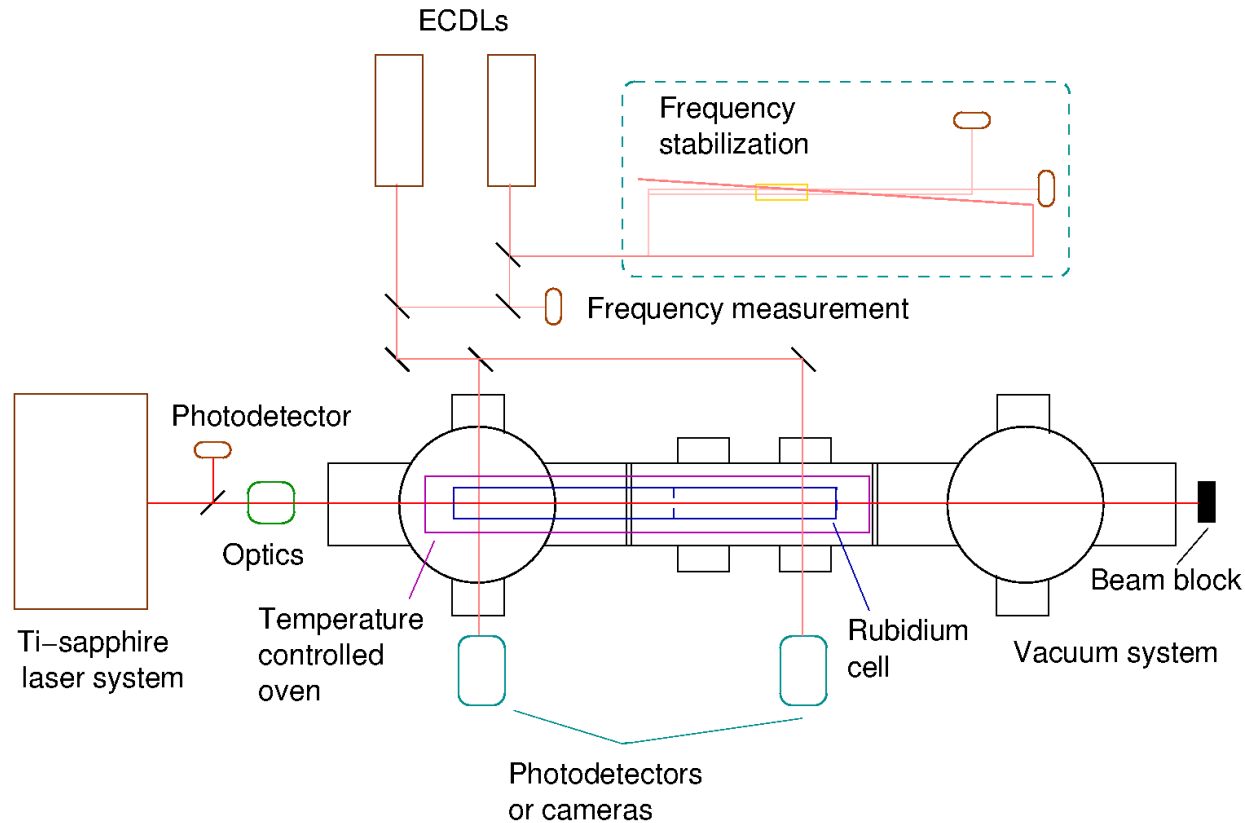
ground state :  $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^2 4p^6 5s$

# Time dependence of the spectral emission



Temperature:  $\sim 200\text{ C}^\circ$   
Ion relaxation mainly through D2 lines (and D1)

# Transversal absorption measurements



- Parameters:
1. Ionizing laser intensity
  2. Probe laser detuning
  3. Vapor density

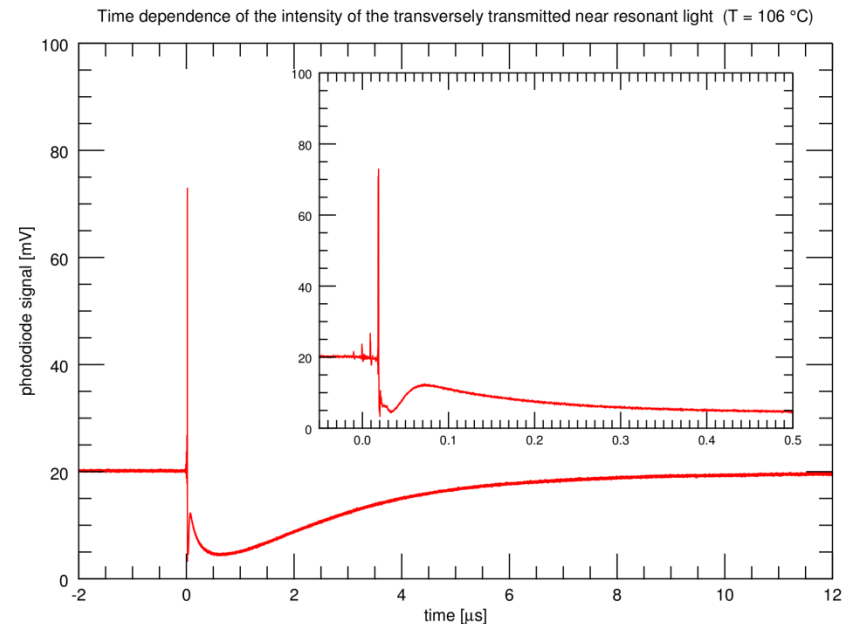
# Typical transmission signals on microsec scale

(different) CW level: Positive peak @ Negative peak and relax.  
(New Focus 1591NF): 4.5 GHz

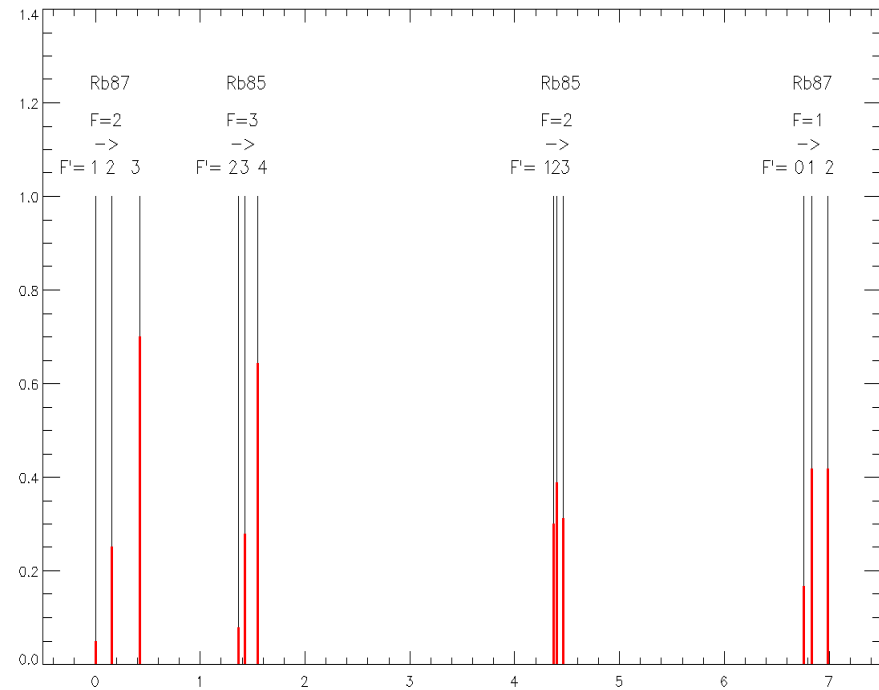
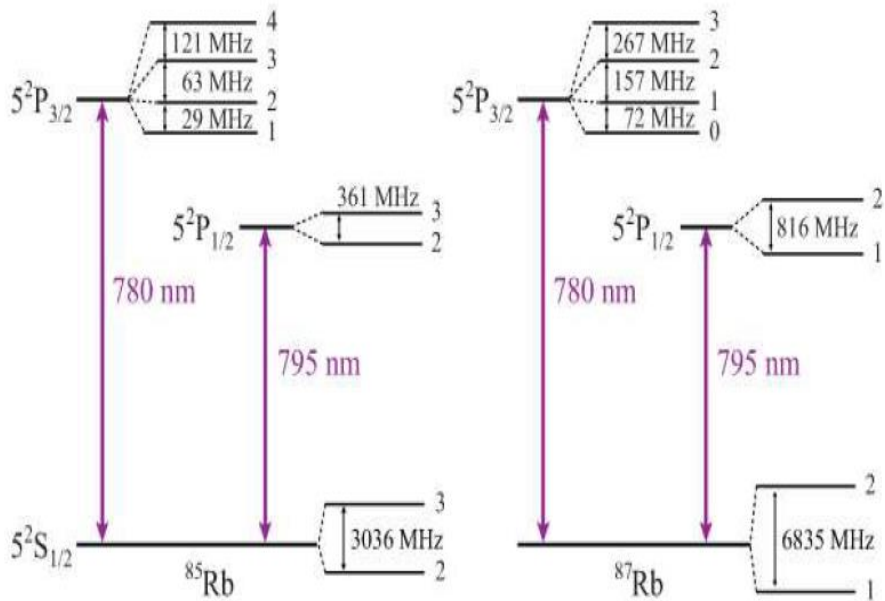
Very fast peak: AC Stark shift  
10 ns decay: atomic relaxation  
Slow (1-10 microsec) decay:  
plasma relaxation

Decrease of transmission is  
attributed to reflection on the  
boundaries of the plasma  
channel.

Initial condition: atoms in the ground state

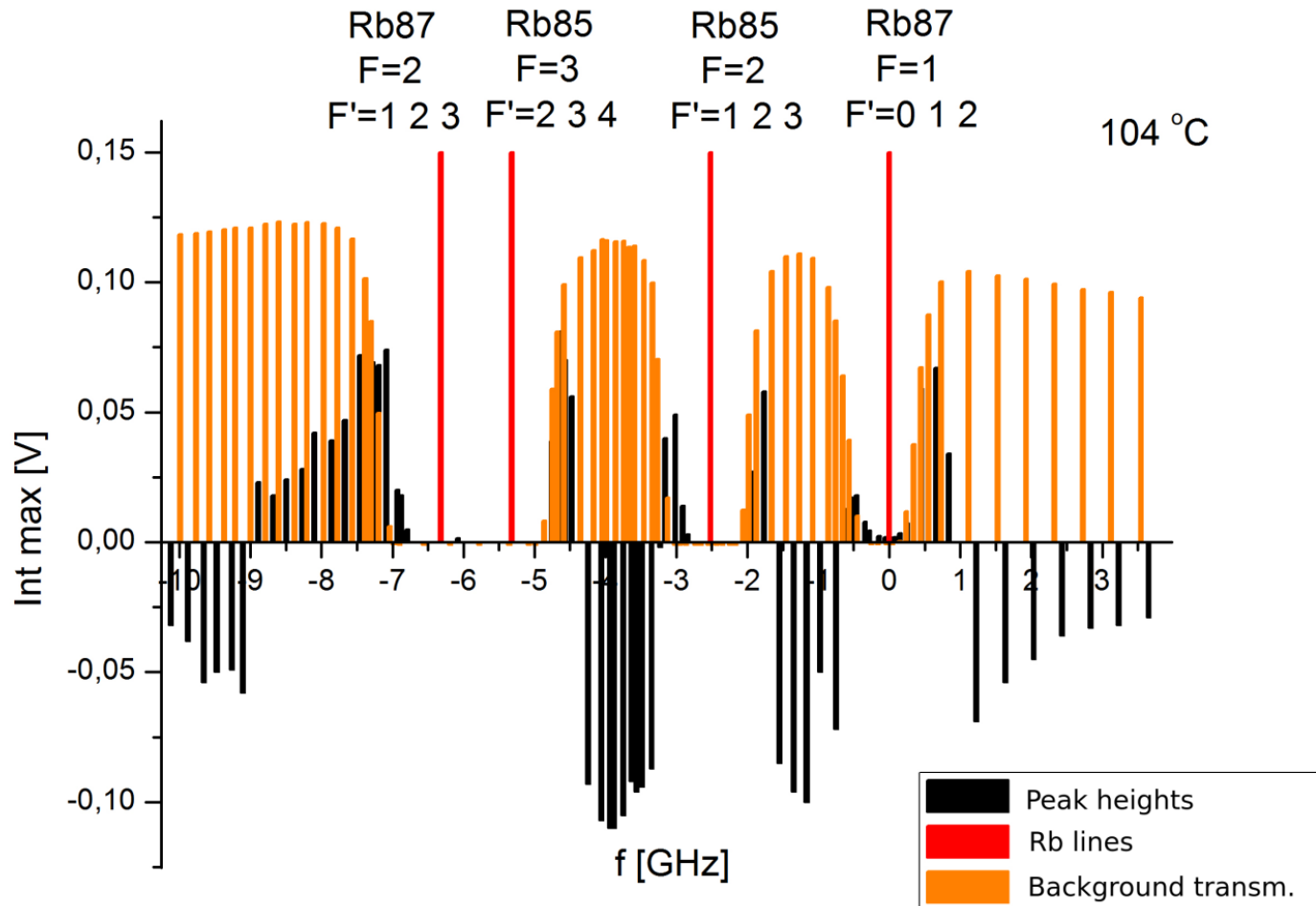


# Detuning: Rubidium frequency reference

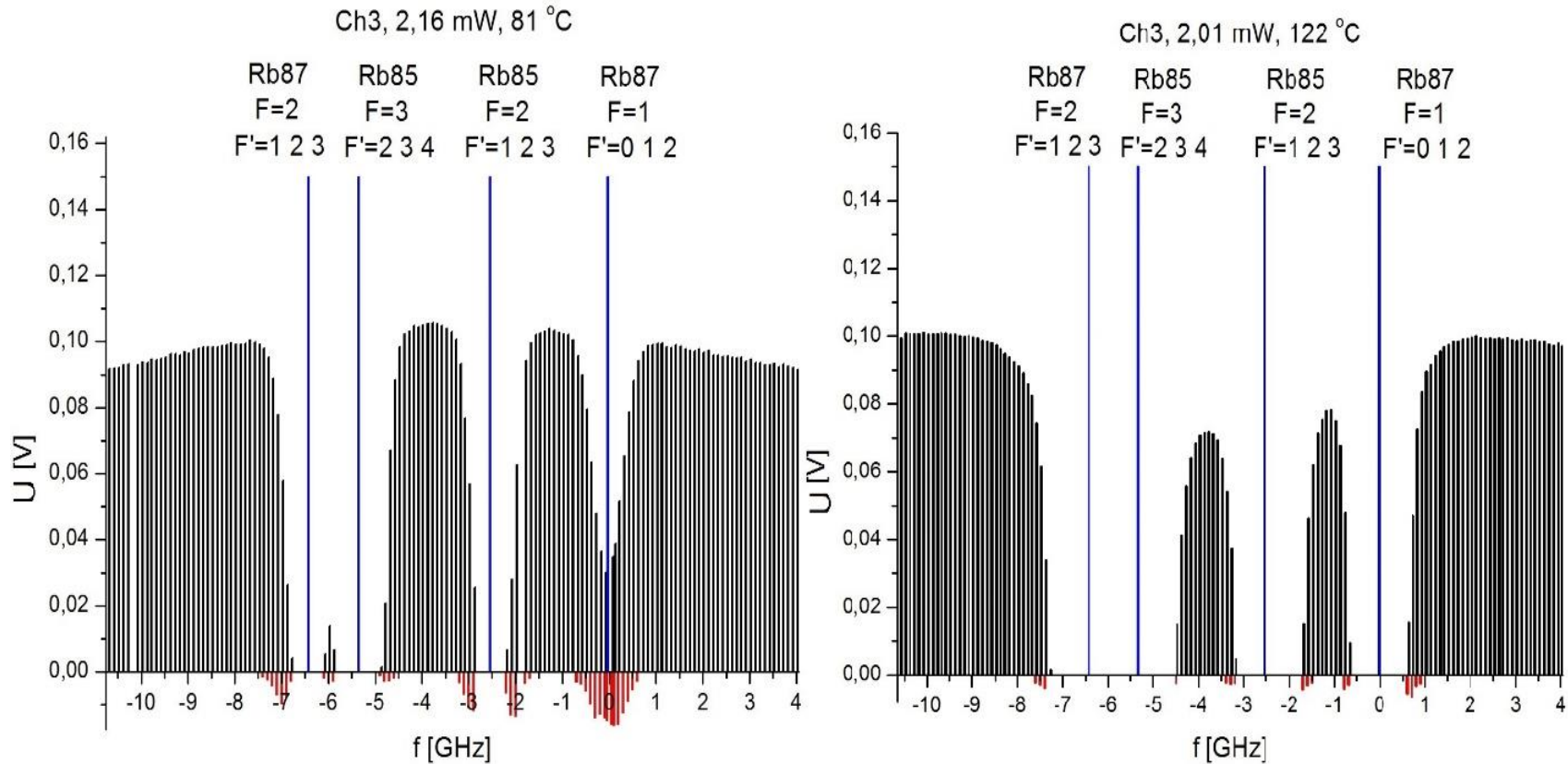




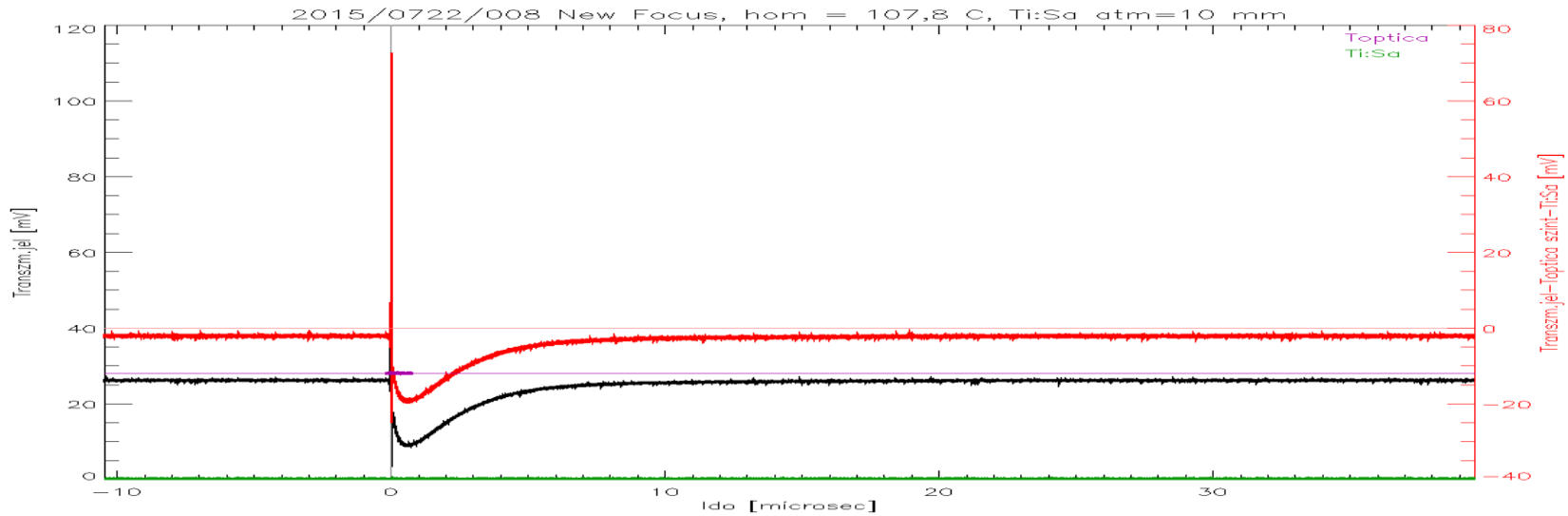
# Dependence of the fast peak maxima on the laser frequency



# Slow relaxation component (negative peak) at different vapor densities

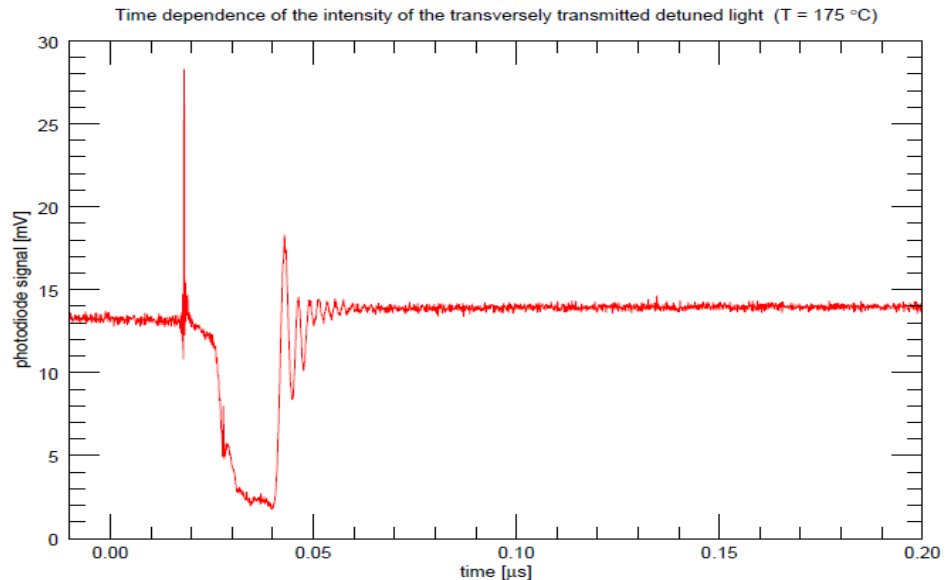


# Transmission signal vs. vapor density



Signal oscillations ?  
 Plasma freq. 100 GHz

$$\omega_p = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}}$$



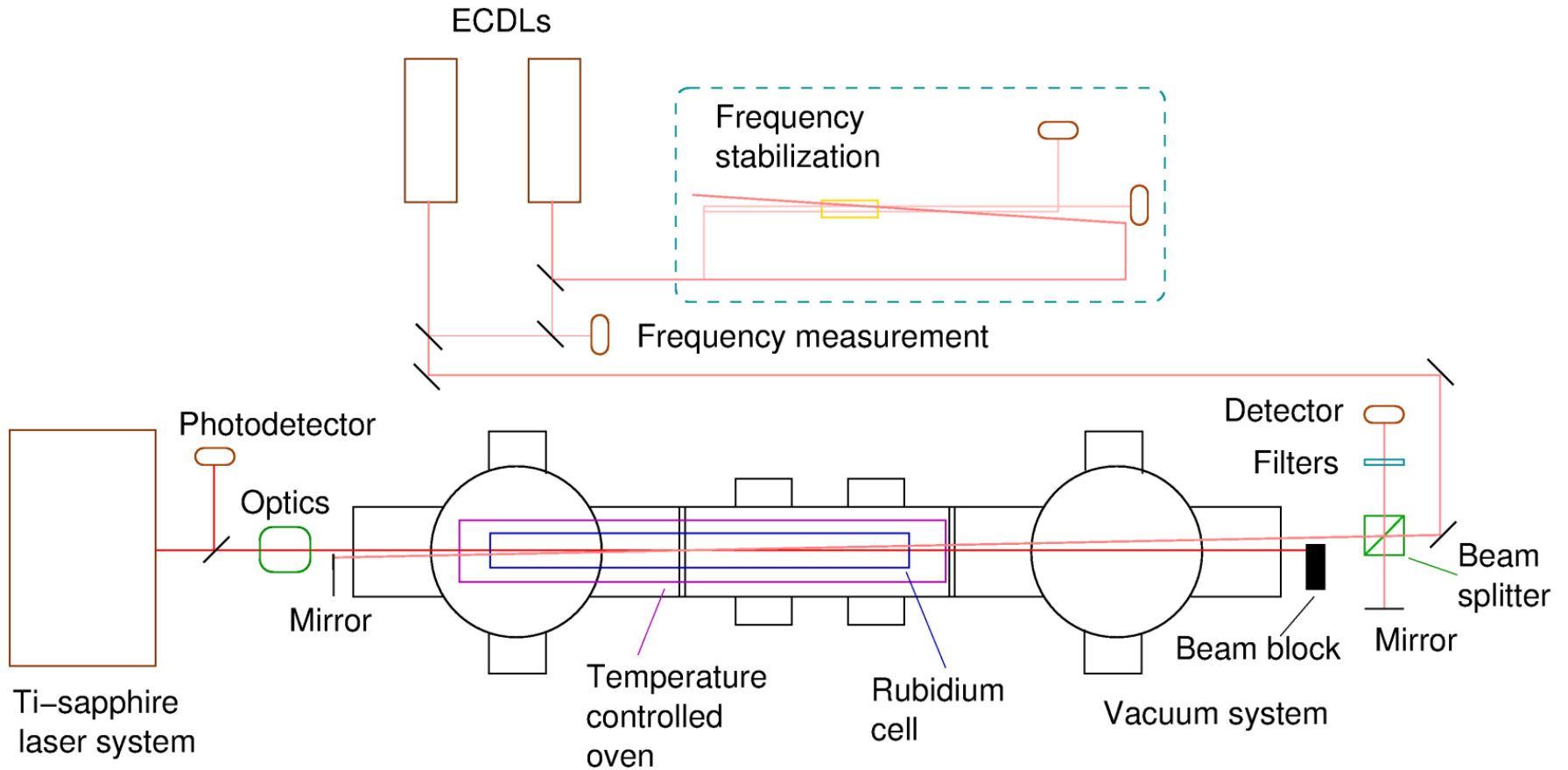
Repeated reflections on the boundaries of the plasma channel

# Summary of transmission signal detection

Cw level is different for detector 1 and detector 2:

- beam divergency, different coupling into the detector fiber
- condensed Rb on the windows surface
- different vapor temperature and density
  
- CW signal is absorbed close to the resonance lines
  
- Negative peak signal is missing far from the atomic lines
  
- 'Plasma oscillations'

# Plasma density measurements by longitudinal interferometry



# Phase variation

$$I_{\text{interf}}(t) = I_{\text{tr}}(t) + I_{\text{ref}} + 2\varepsilon \sqrt{I_{\text{tr}}(t)I_{\text{ref}}} \cos(\varphi_0 + \varphi_1(t))$$

$$\varphi_1(t) = (2\pi / \lambda)L\Delta n(t)$$

Phase variation

$$n(\Delta\omega) = 1 - \frac{N\pi f e^2}{2m} \sum_{i=1}^2 p_i \sum_{j=1}^2 \frac{\Delta\omega_j^{(i)}}{\omega_{0j}^{(i)} (\Delta\omega_j^{(i)2} + \Gamma^2)}$$

Refractive  
index

$$\Delta N_p(t)L = \varphi_1(t) \frac{2\lambda_L m}{\pi^2 f e^2} / \left[ \sum_{i=1}^2 p_i \sum_{j=1}^2 \frac{\Delta\omega_j^{(i)}}{\omega_{0j}^{(i)} (\Delta\omega_j^{(i)2} + \Gamma^2)} \right]$$

Plasma  
density  
\*  
length

# Phase variation @ Doppler broadening

$$n(\Delta\omega) = 1 - \frac{\pi\Delta\omega N f e^2 / m\omega_0}{\Delta\omega^2 + \Gamma^2}$$

$$n(\Delta\omega) - 1 = -\Gamma \alpha_0 \int_{-\infty}^{\infty} D(\sigma) \frac{(\Delta\omega + \sigma)}{(\Delta\omega + \sigma)^2 + \Gamma^2} d\sigma$$

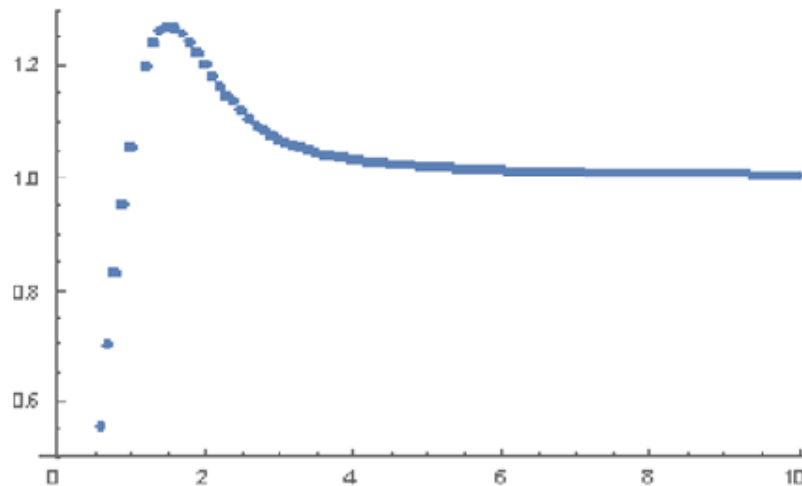
$$\alpha_0 = \pi N f e^2 / (\Gamma m \omega_0)$$

Absorption coefficient

$$D(\sigma) = \frac{1}{\sqrt{\pi}\sigma_0} e^{-\sigma^2/\sigma_0^2}$$

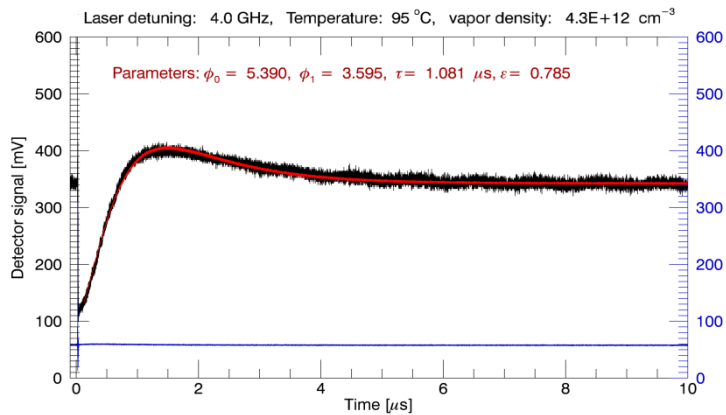
Doppler broadening

Comparative function:  $\Theta(\Delta\omega) = \Delta N_p(t) / \Delta N_p^{(D)}(t)$

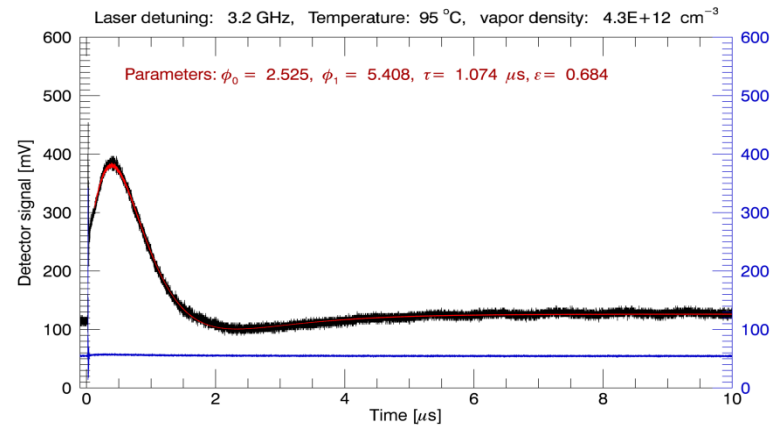


Normalized detuning

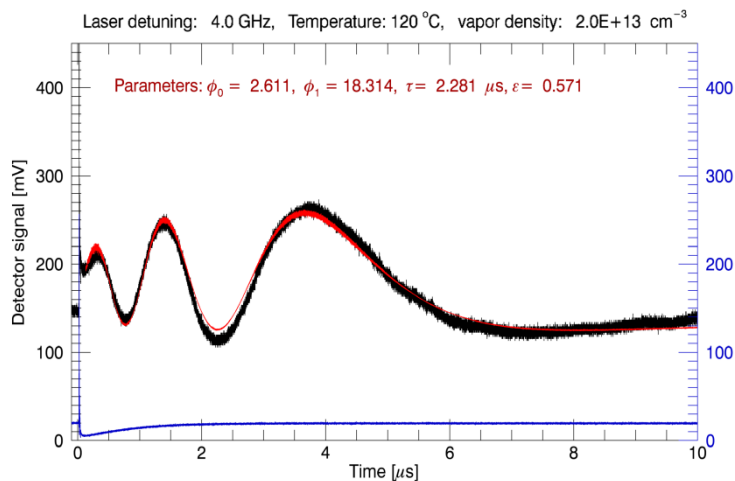
# Results: time dependent fringes



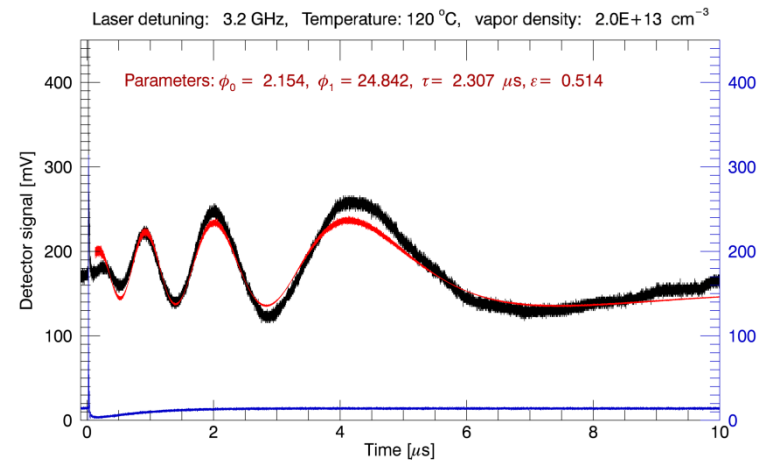
$$\Delta N = 2.0 \times 10^{11} \text{ cm}^{-3} \quad 7.8\% \quad 3.6 \text{ rad}$$



$$\Delta N = 2.4 \times 10^{11} \text{ cm}^{-3} \quad 10.8\% \quad 5.4 \text{ rad}$$



$$\Delta N = 1.0 \times 10^{12} \text{ cm}^{-3} \quad 8.5\% \quad 18.3 \text{ rad}$$



$$\Delta N = 1.1 \times 10^{12} \text{ cm}^{-3} \quad 10.6\% \quad 24.8 \text{ rad} \quad 24$$



# Plasma relaxation

$$I_{\text{int erf}}(t) = I_{\text{tr}}(t) + I_{\text{ref}} + 2\varepsilon \sqrt{I_{\text{tr}}(t)I_{\text{ref}}} \cos(\varphi_0 + \varphi_1(t))$$

$$\frac{dN}{dt} = -\frac{1}{\tau} N$$

$$N_D = N_0 e^{-t/\tau_{N0}}$$

Diffusion model

$$\frac{dN}{dt} = -\alpha N^2$$

$$N_{3B} = \frac{N_0}{1 + N_0 \alpha t}$$

3 body  
recombination  
model

$$\frac{dN}{dt} = -\beta N^3$$

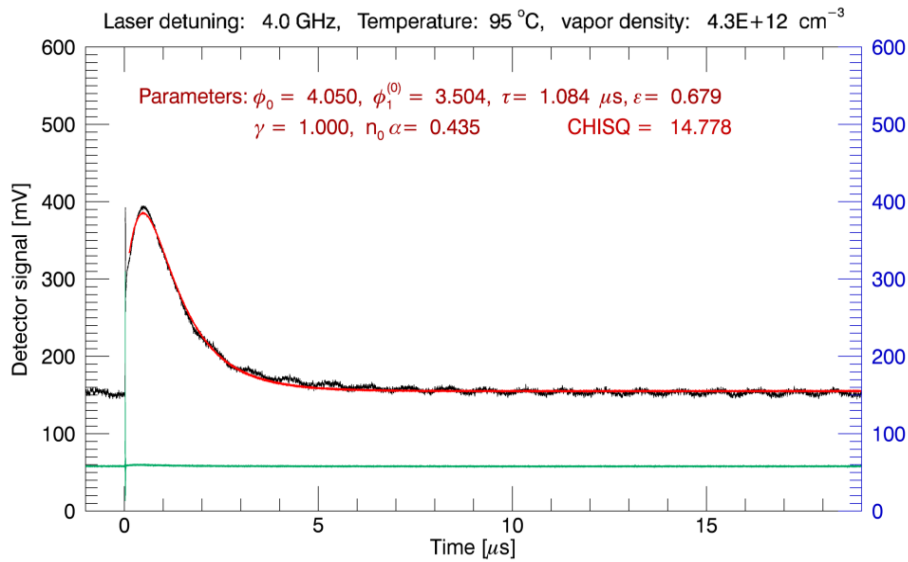
$$N_{3BP} = \frac{N_0}{\sqrt{1 + 2N_0^2 \beta t}}$$

Pitaevski:  $\alpha = \beta N$

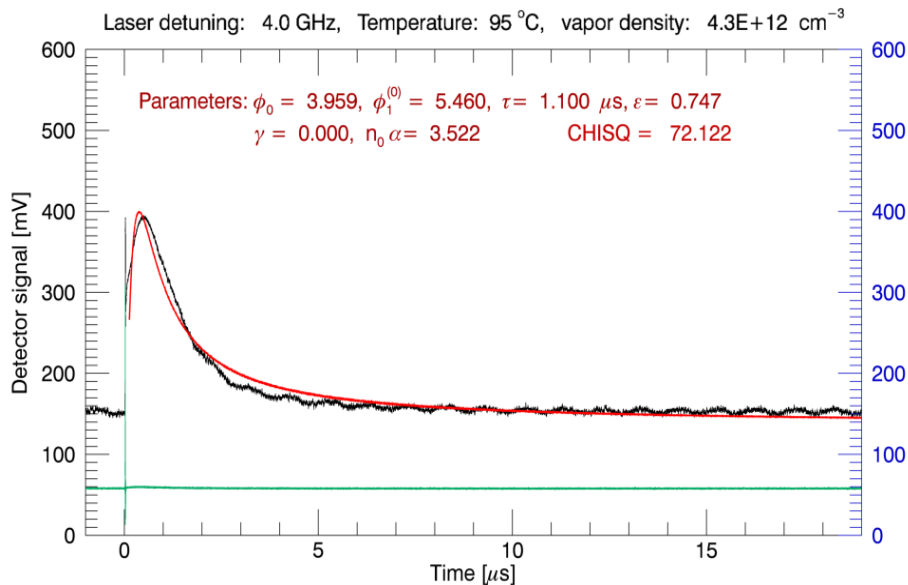
$$N_{PM} = \gamma N_0 e^{-t/\tau_{N0}} + (1 - \gamma) \frac{N_0}{1 + N_0 \alpha t}$$

P. Muggli MPP

# Curve fitting for diffusion @ 3body model

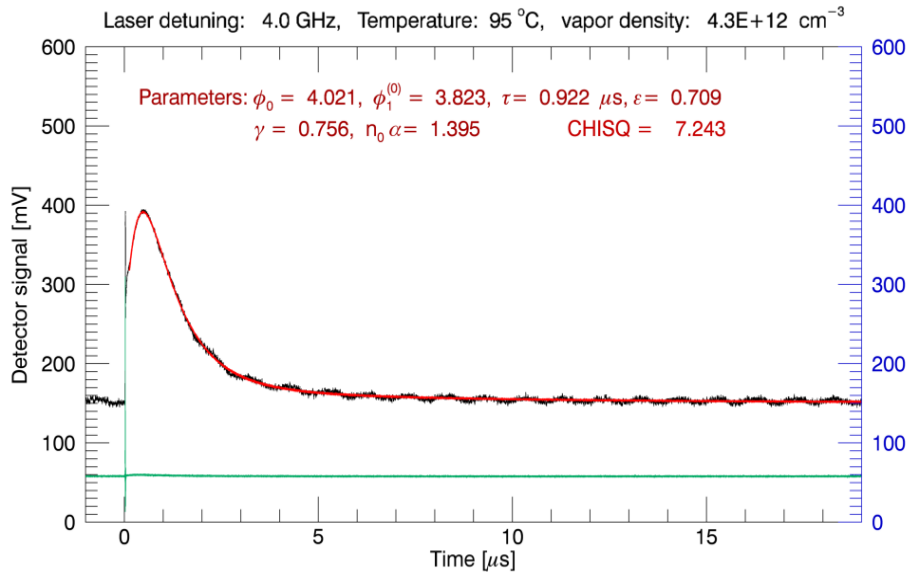


$$N_D = N_0 e^{-t/\tau_{N0}}$$

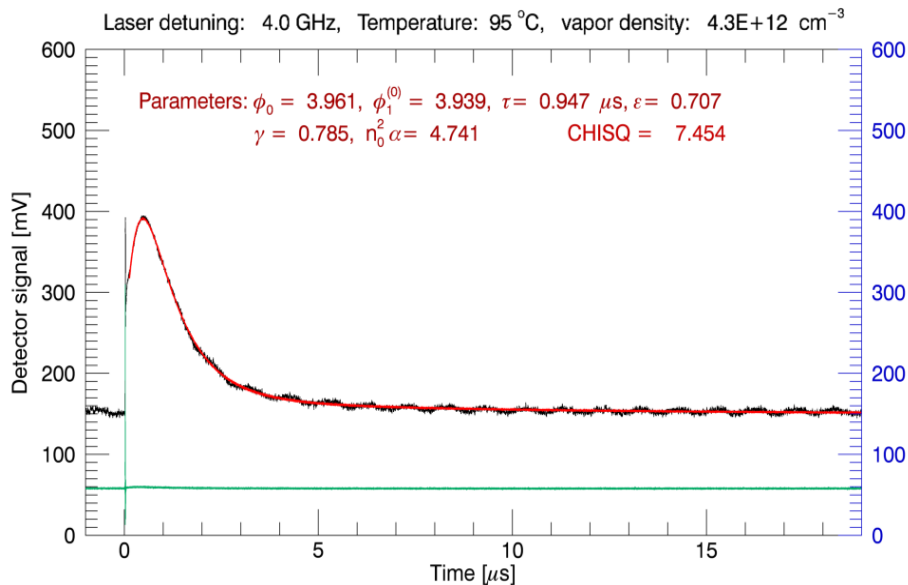


$$N_{3B} = \frac{N_0}{1 + N_0 \alpha t}$$

# Curve fitting for mixed models



$$N_{PM} = \gamma N_0 e^{-t/\tau_{N0}} + (1 - \gamma) \frac{N_0}{1 + N_0 \alpha t}$$



$$N_{D+3BP} = N_0 \left[ \gamma e^{-t/\tau_{N0}} + (1 - \gamma) \frac{1}{\sqrt{1 + 2N_0^2 \beta t}} \right]$$

Fit courtesy of M. Kedves

# Interpretation of decay time

Knudsen regime: mean free path  $\sim$  characteristic length

Intermediate state between molecular flow and viscous flow

Mean free path in Rb vapor:

$$L = \frac{1}{\sqrt{2}d^2\pi N}$$

$$L = 4.5\text{cm} \quad \text{at } 120\text{ C}^\circ \quad \text{and} \quad 2 \times 10^{13} \text{ cm}^{-3}$$

$$L = 20.9\text{cm} \quad \text{at } 95\text{ C}^\circ \quad \text{and} \quad 4,3 \times 10^{12} \text{ cm}^{-3}$$

$$d = 5 \times 10^{-10} \text{ m} \quad \text{atomic diameter for Rb}$$

Rb vapor cell below 120 C<sup>o</sup> : quasi collisionless flight of atoms:

Probe beam channel is filled with neutral atoms out of the channel

$$v_{rms} = \sqrt{\frac{3k_B T}{m}} \quad \sim \quad 330 \text{ m/s at } 95\text{ C}^\circ \quad \text{and} \quad 340 \text{ m/s at } 120\text{ C}^\circ$$

$$\frac{dN}{dt} = -\frac{1}{\tau_{N0}} N \quad \text{Linear kinetic equation} \quad N = N_0 e^{-t/\tau_{N0}} \quad \text{Exponential decay}$$

$$\text{Ratio of collisions on a characteristic length } l = 1\text{cm} \quad N_C / N_0 = (1 - e^{-l/L})$$

$$N_C / N_0 = 0.05 \quad \text{at } 95\text{ C}^\circ$$

$$N_C / N_0 = 0.2 \quad \text{at } 120\text{ C}^\circ$$

The greater the density  
The greater the decay time

Thank you

for your

attention