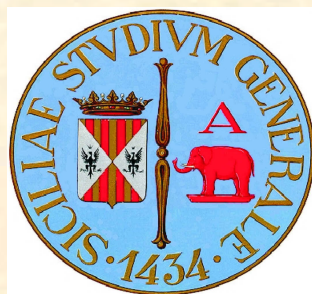




Gazing at Matter above a Trillion of degrees

Vincenzo Greco - University of Catania



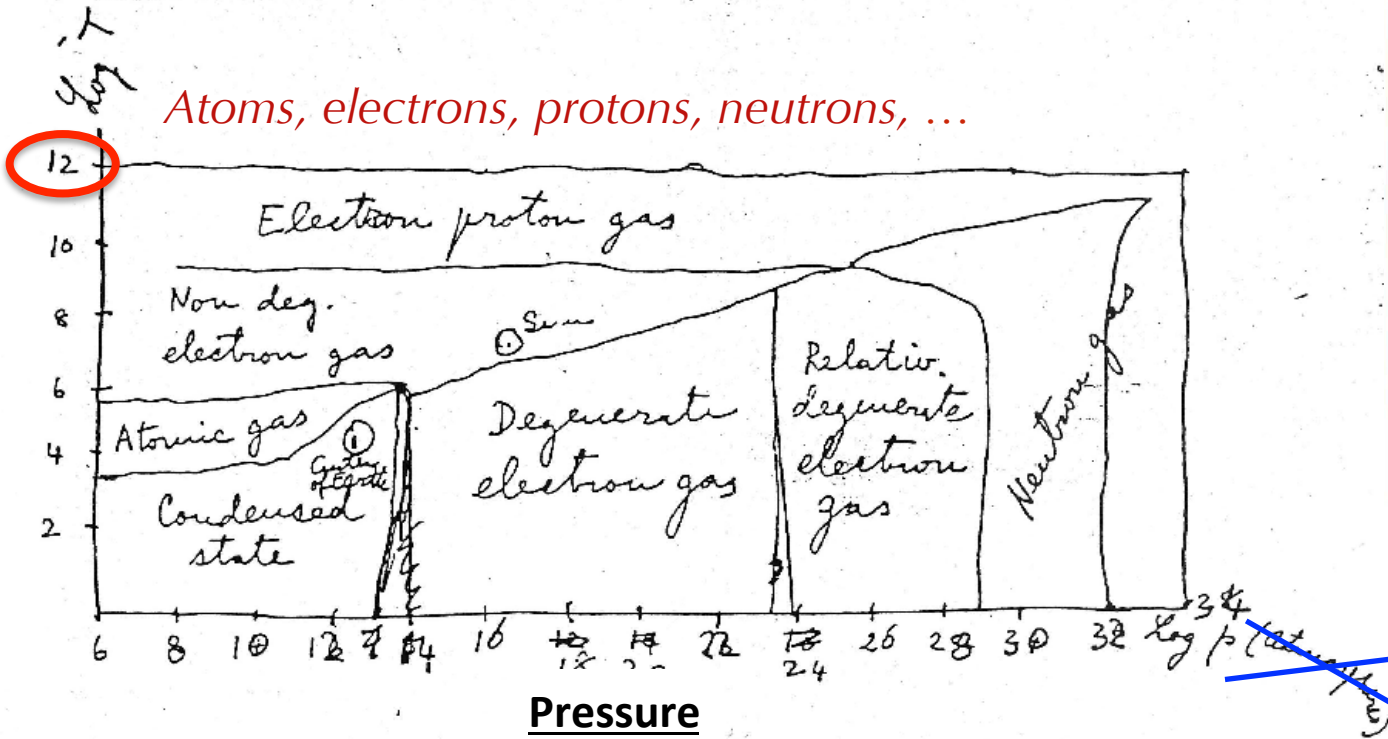
Inaugural Lecture AE P&E sciences, 3rd September 2017, Budapest, Hungary

Matter in unusual conditions...

Fermi's Notes on Thermodynamics and Statistics (1953)

Atoms, electrons, protons, neutrons, ...

Temperature



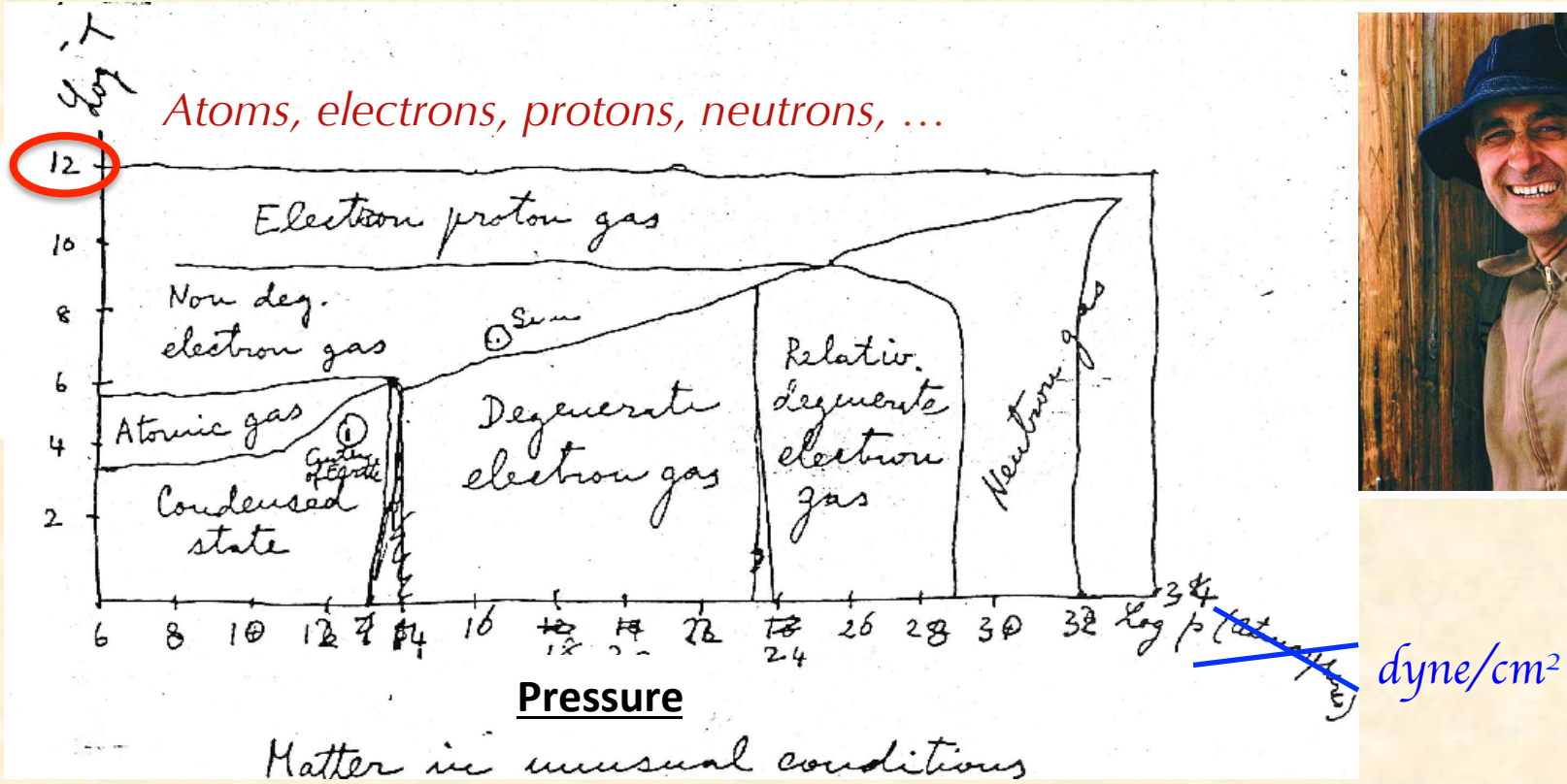
dyne/cm²

Matter in unusual conditions

Matter in unusual conditions...

Fermi's Notes on Thermodynamics and Statistics (1953)

Temperature



Fermi put Nothing above $10^{12}K$!

if $T > 10^{12}K \approx 200 \text{ MeV} \rightarrow KT = E \approx 1/L$

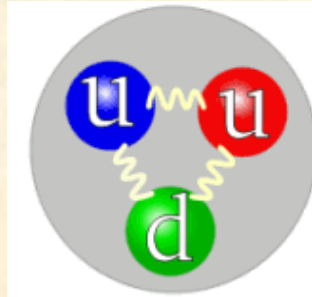
$\rightarrow L < 1 \text{ fm}$ go inside a proton

In the '50 and '60 there was nothing inside a proton

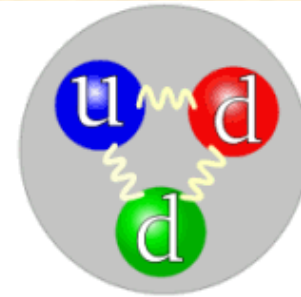
Now we know that...

Elementary Particles

Quarks	u up	c charm	t top	γ photon
	d down	s strange	b bottom	
	g gluon			
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z Z boson
	e electron	μ muon	τ tau	W W boson
	Force Carriers			



proton

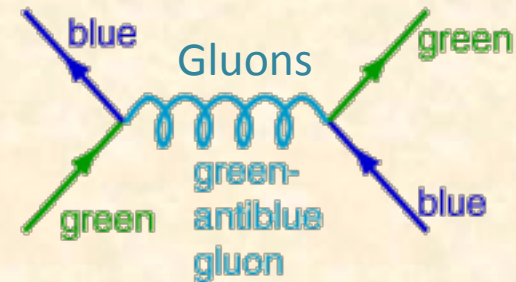


neutron

Quarks and Gluons dynamics is driven by The Strong Interaction

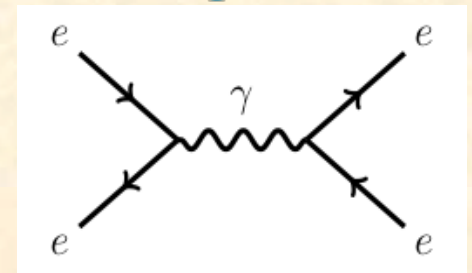
Quantum ChromoDynamics (QCD) - 1973

$$L_{QCD} = \bar{\Psi}(i\gamma_\mu \partial_\mu - m_i)\Psi - gA_a^\mu \bar{\Psi}\gamma_\mu t_a \Psi - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}$$



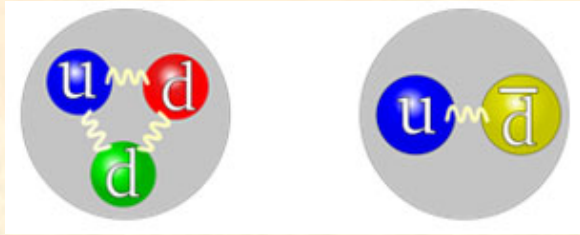
Quantum Electrodynamics (QED)

$$L_{QED} = \bar{\Psi}(i\gamma_\mu \partial_\mu - m_i)\Psi - gA^\mu \bar{\Psi}\gamma_\mu \Psi - \frac{1}{4}F_{\mu\nu} F^{\mu\nu}$$



Quantum Chromodynamics

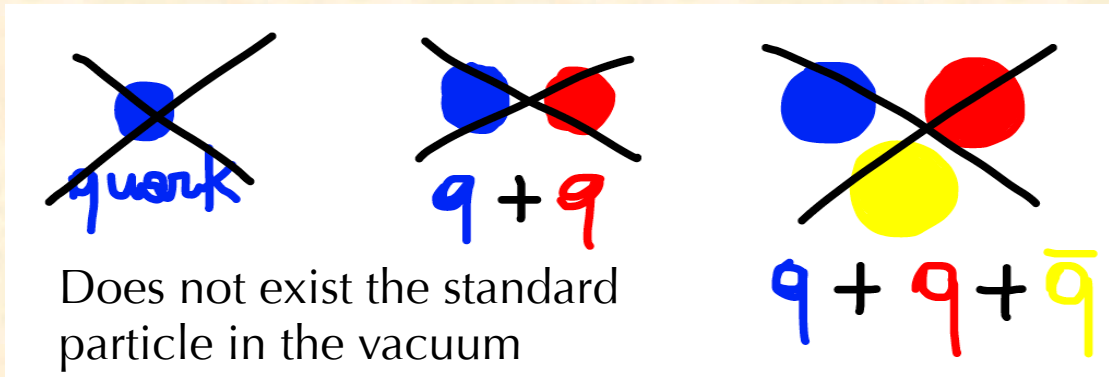
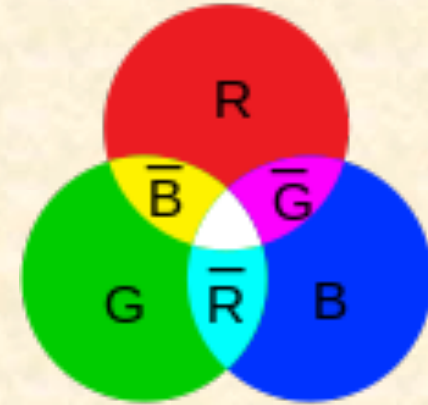
- ✧ There are no free quark! → **Confinement**
- ✧ There are *only white (neutral) objects*



Baryons: qqq

Mesons : qq

with 2 colors "protons" would have been bosons!



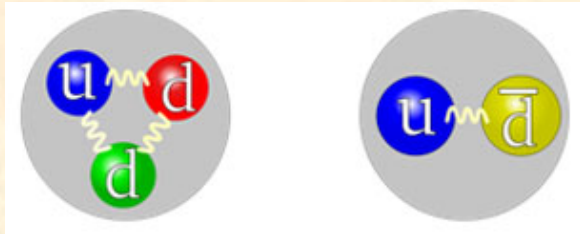
Does not exist the standard particle in the vacuum

All non-white combination do not exist!

- ❖ QCD is very strange and unique: **built on particles that cannot be detected experimentally.** *Before QCD this would have been seen as anti(pre)-scientific!*

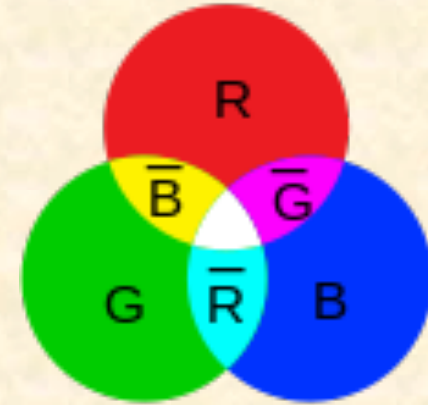
Quantum Chromodynamics \neq QED

- ✧ There are no free quark! \rightarrow **Confinement**
- ✧ There are *only white (neutral) objects*

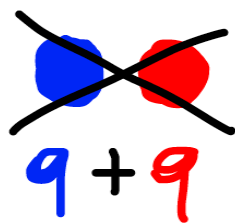


Baryons: qqq

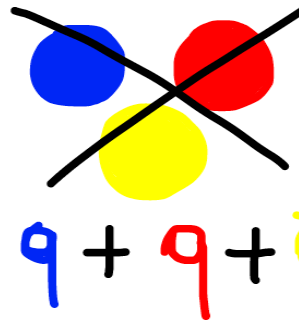
Mesons : qq



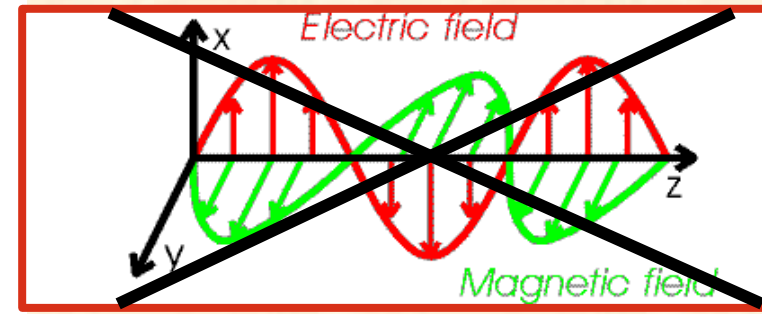
Does not exist the standard particle in the vacuum



$q + q$



$q + q + \bar{q}$

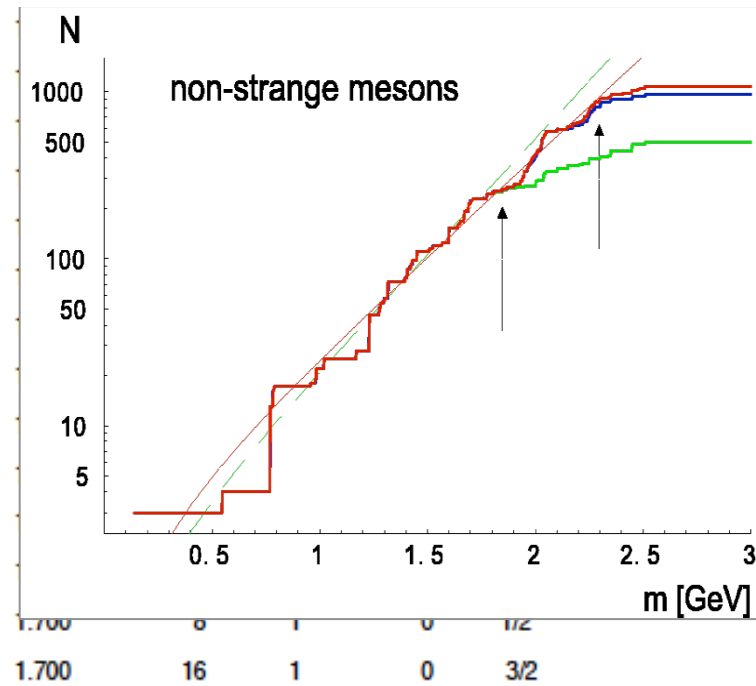


- ❖ QCD is very strange and unique: **built on particles that cannot be detected experimentally.** *Before QCD this would have been seen as anti(pre)-scientific!*
- ❖ **No Chromomagnetic waves propagating in the vacuum!**

There are still a lot of hadrons ...

hadron	m_i (GeV)	d_i	B_i	S_i	I_i	hadron	m_i (GeV)	d_i	B_i	S_i	I_i
π	0.140	3	0	0	1	N (1535)	1.530	4	1	0	1/2
K	0.496	2	0	1	1/2	π_1 (1600)	1.596	9	0	0	1
\overline{K}	0.496	2	0	-1	1/2	Δ (1600)	1.600	16	1	0	3/2
η	0.543	1	0	0	0	Λ (1600)	1.600	2	1	-1	0
ρ	0.776	9	0	0	1	Δ (1620)	1.630	8	1	0	3/2
ω	0.782	3	0	0	0	η_2 (1645)	1.617	5	0	0	0
K^*	0.892	6	0	1	1/2	N (1650)	1.655	4	1	0	1/2
\overline{K}^*	0.892	6	0	-1	1/2	ω (1650)	1.670	3	0	0	0
N	0.939	4	1	0	1/2	Σ (1660)	1.660	6	1	-1	1
η'	0.958	1	0	0	0	Λ (1670)	1.670	2	1	-1	0
f_0	0.980	1	0	0	0	Σ (1670)	1.670	6	1	-1	1
a_0	0.980	3	0	0	1	ω_3 (1670)	1.670	3	0	0	0
ϕ	1.020	3	0	0	0	π_2 (1670)	1.670	9	0	0	1
Λ	1.116	2	1	-1	0	Ω^-	1.670	1	1	-1	0
h_1	1.170	3	0	0	1	N (1675)	1.675	4	1	0	1/2
Σ	1.189	6	1	-1	1	ϕ (1680)	1.680	3	0	0	0
a_1	1.230	9	0	0	1	K^* (1680)	1.680	6	0	1	1/2
b_1	1.230	9	0	0	1	\overline{K}^* (1680)	1.680	6	0	-1	1/2
Δ	1.232	16	1	0	3/2	N (1680)	1.680	4	1	0	1/2
f_2	1.270	5	0	0	0	ρ_3 (1690)	1.690	8	1	0	3/2
K_1	1.273	6	0	1	1/2	Λ (1690)	1.690	2	1	-1	0
\overline{K}_1	1.273	6	0	-1	1/2	Ξ (1690)	1.690	4	1	-1	1/2
f_1	1.285	3	0	0	1	ρ (1700)	1.700	9	0	0	1
η (1295)	1.295	1	0	0	0	N (1700)	1.700	4	1	0	1/2
π (1300)	1.300	3	0	0	1	Δ (1700)	1.700	16	1	0	3/2

Density of state increase exp. with m



Quantum Chromodynamics

Strong coupling constant

$$\alpha_s(Q^2) = \frac{g^2}{4\pi} \approx \log^{-1} \left(\frac{Q^2}{\Lambda_{QCD}^2} \right)$$

$$\Lambda_{QCD} \approx 200 \text{ MeV} \approx 1 \text{ fm}^{-1}$$

e.m. coupling

$$\alpha_{e.m.}(Q^2) = \frac{e^2}{4\pi} = \frac{1}{137}$$

$$V(Q) \approx \frac{\alpha(Q^2)}{r}$$

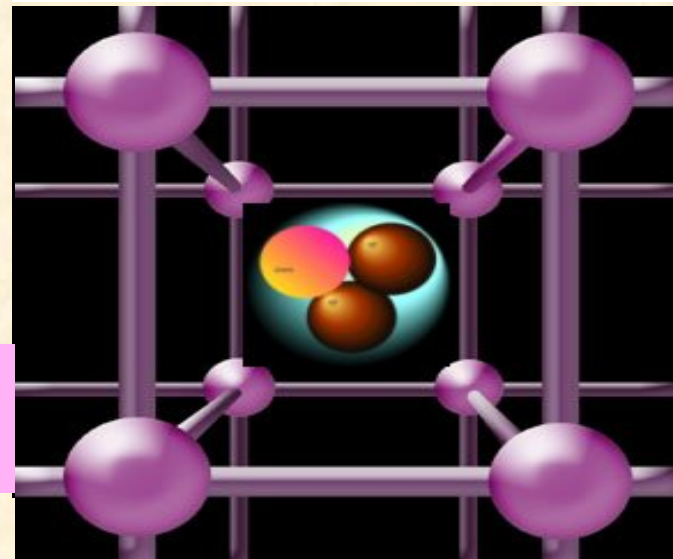
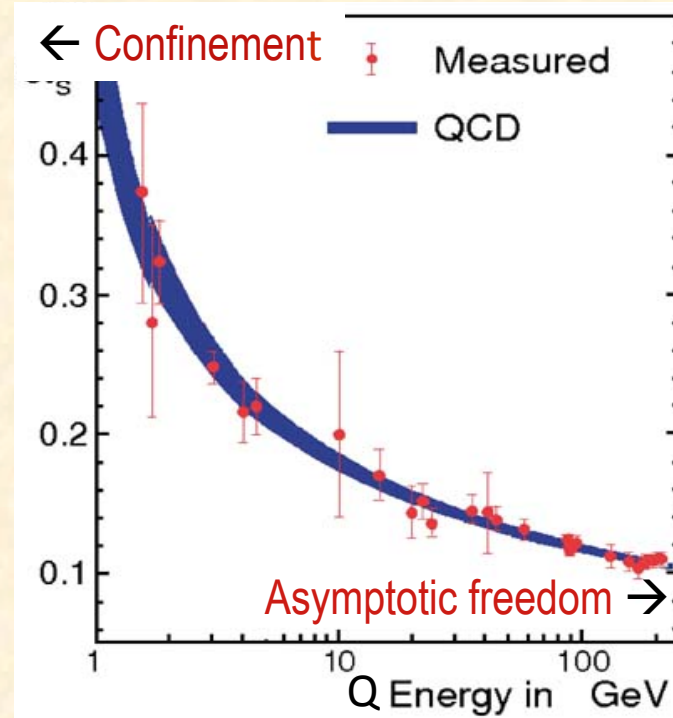
Two regimes:

➤ Perturbative: Asymptotic freedom ($Q \geq 20 \Lambda_{QCD}$)

- Interaction Increase with distance \neq other interaction
- precise results for Early Universe at energies we can reach on Earth!!!

➤ Non-Perturbative : Confinement

- solvable only on Lattice QCD
(i.e. integrating over about 10^7 variables...)



❖ Confinement means “No Ionization” → No colored plasma (“charged” gas) like for atoms!?

If you have to stay confined to white spots how can you move freely?



NI 10/02/2000

A skier (quark) is
Confined inside snow
patches (hadrons)

If you have to stay confined to white spots how can you move freely?

NI 10/02/2000



A skier (quark) is
Confined inside snow
patches (hadrons)

Temperature



The skier can move
further ... a new phase
develops

.. goes up



A skier (quark) can move
freely ... over long
distances

.. this way

Quark-Gluon Plasma (5th state of matter)

1975: J.C. Collins M.J. Perry, "Superdense Matter or **Asymptotically Free** Quarks?", Phys. Rev. Lett. 34, 1353: "*...matter at densities higher than nuclear consists of a quark soup. The **quarks become free** at sufficiently high density or temperature.*"

2000 – CERN Statement, Nature 403 : "evidence for the existence of a new state of quark-gluon matter in which quarks ... are liberated **to roam freely**... in which quarks and gluons are no longer confined but **free to move** around over a volume... quarks would then **freely roam**."

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1975: Cabibbo & Parisi, Phys.Lett.B 59, 67, "**Exponential hadronic spectrum** and quark liberation". An hadronic resonance gas has a **divergency in the partition function** at $T=T_0 \approx 160$ MeV \rightarrow phase transitions.

Note: Before "73 there was nothing to transit to. T_0 was limiting Temperature (Hagedorn)

Density of states $\rho(m)$ of hadronic matter wins over Boltmann suppression factor

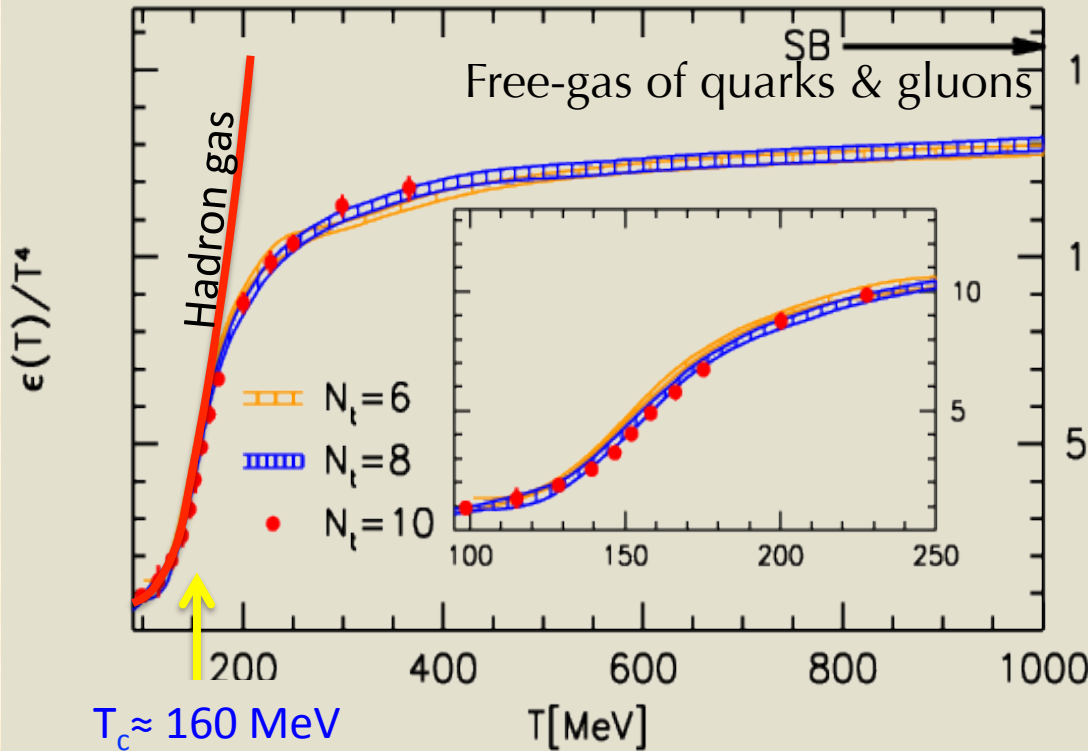
$$\log Z(T, V) \propto \int_{m_0}^{\infty} dm m^{3/2} \rho(m) e^{-\frac{m}{T}} \propto \int_{m_0}^{\infty} dm m^{\alpha+3/2} e^{-m\left(\frac{1}{T} - \frac{1}{T_0}\right)}$$

Integral diverges for $T \rightarrow T_0$:

Not related to Asymptotic Freedom!

Beyond naive argument: lattice QCD

Rescaled Energy Density



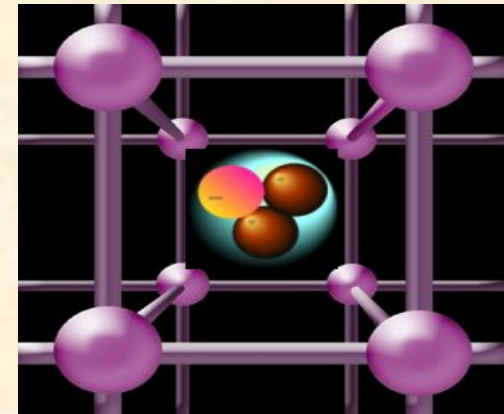
$$15 \frac{\epsilon_{SB}}{T^4} = \frac{\pi^2}{30} \left[\frac{7}{8} d_{q+\bar{q}} + d_g \right] \approx \frac{1}{3} \# d.o.f$$

Colored Matter
about 45 d.o.f.

$$d = 3_{fl} * 3_{col} * 2_s * 2_{anti} + 16_{gluon}$$

Wuppertal-Budapest Collab. (2010)

Stefan-Boltzmann limit not reached
by 15-20 % : QGP as a weak interacting gas?
But $\epsilon - 3p \gg 0$ strong interaction ...



Matter evolution in the Universe

BIG BANG

$T \sim 10^{32} \text{ }^\circ\text{K}$

10^{-43} seconds

Time after Big Bang

10^{-6} sec.

3 min.

380,000 years

1 billion years

13.7 billion years

Quark & Gluons
($T=10^{12} \text{ }^\circ\text{K}$)

Particles

Atomic Nuclei

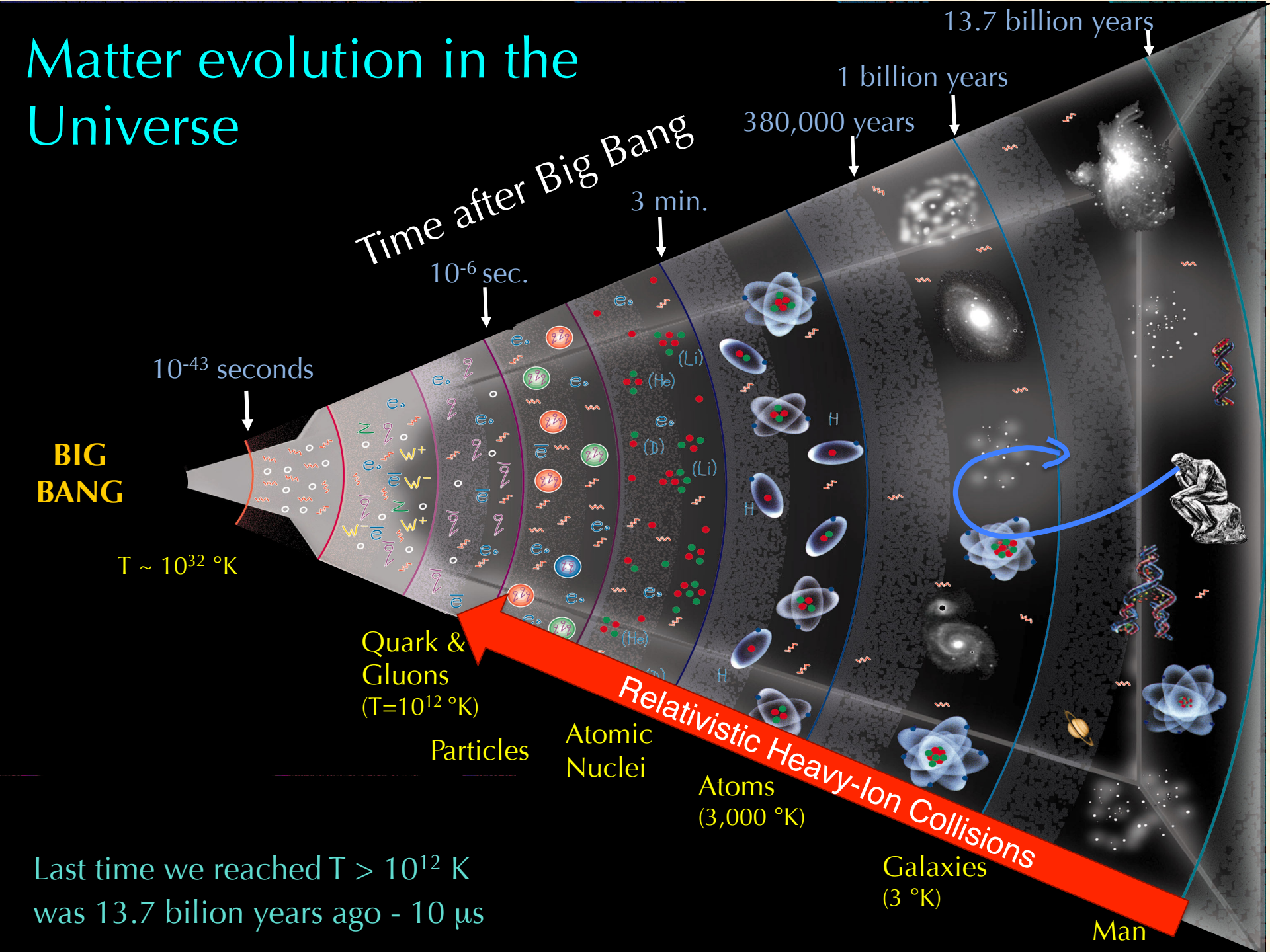
Atoms
($3,000 \text{ }^\circ\text{K}$)

Galaxies
($3 \text{ }^\circ\text{K}$)

Man

Relativistic Heavy-Ion Collisions

Last time we reached $T > 10^{12} \text{ K}$ was 13.7 billion years ago - $10 \text{ } \mu\text{s}$

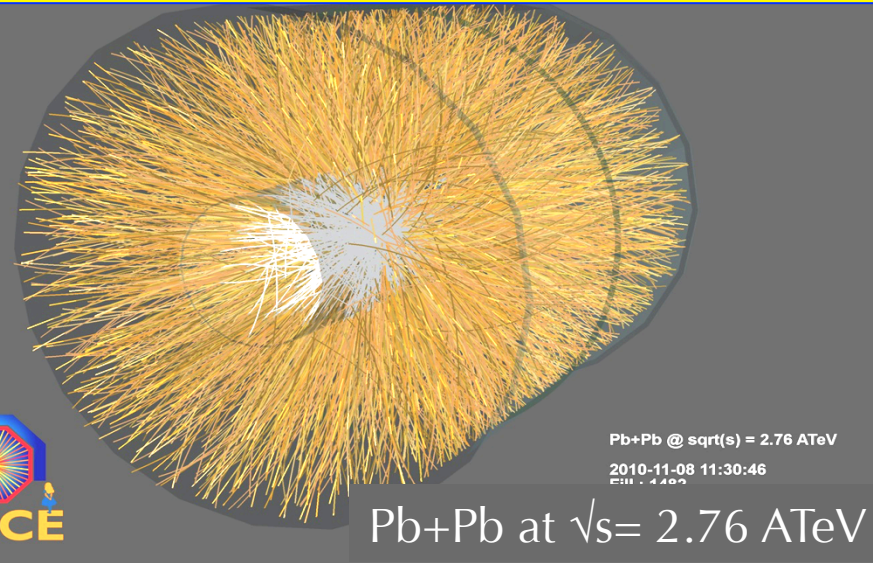
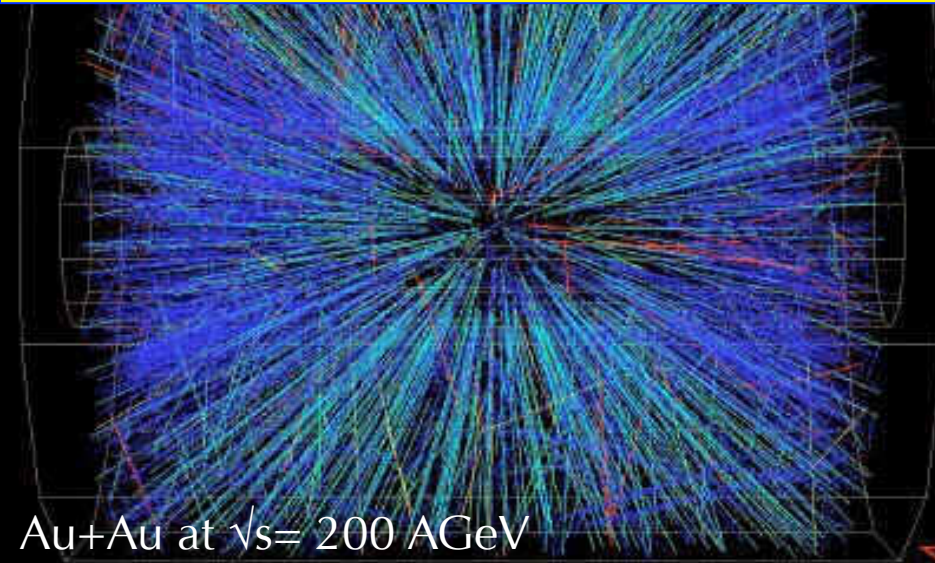


➤ Uninteresting question:

What happens when I crash two gold nuclei together?

RHIC-BNL

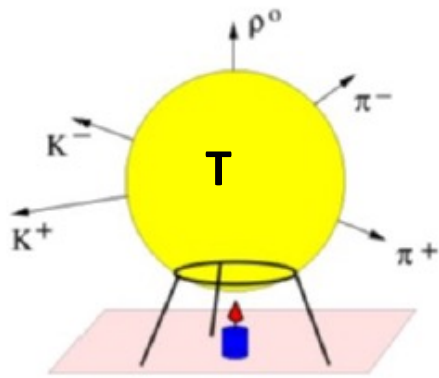
LHC-CERN



Do we create fireworks?

Or a plasma at some finite temperature?

Hadrons produced at $T < T_0$

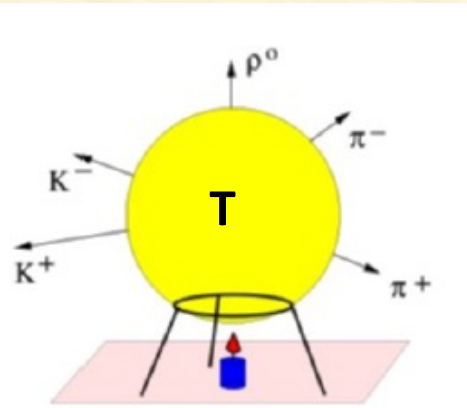


$E=mc^2$ (+) $E=KT$ energy used to produced new particles of mass m_j ($j= \pi, K, \rho, \Lambda, \Omega, \dots$)

Particle Abundancy

$$n_j \approx e^{-\frac{m_j}{T}}$$

Hadrons produced at $T < T_0$

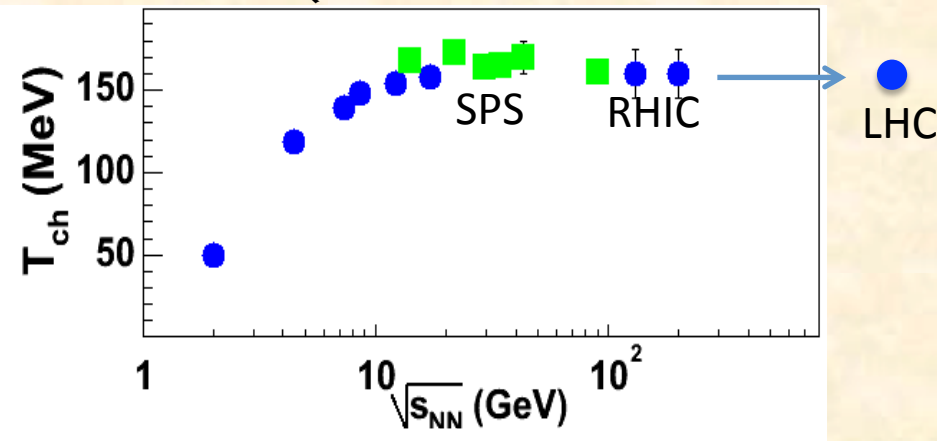


$E=mc^2$ (+) $E=KT$ energy used to produce new particles of mass m_j ($j = \pi, K, \rho, \Lambda, \Omega, \dots$)

Particle Abundance – Statistical Hadronization

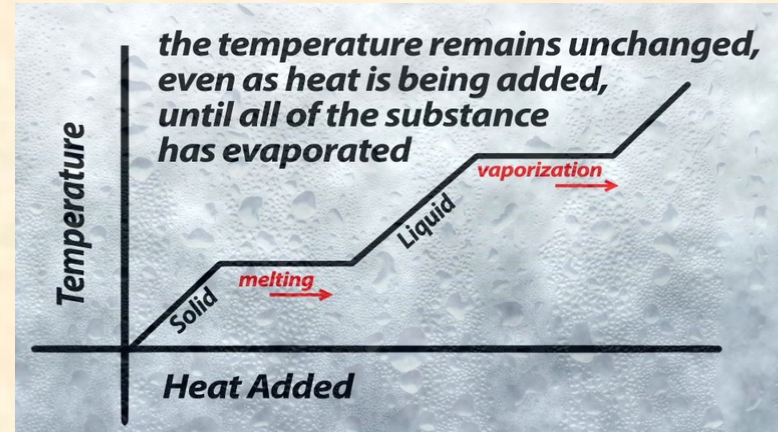
$$\langle n_j \rangle = \frac{(2J_j + 1)V}{(2\pi)^3} \int d^3p \left[e^{\sqrt{p^2 + m_j^2}/T + \mu \cdot \mathbf{q}_j/T} \pm 1 \right]^{-1}$$

Hot QCD matter from HIC



Energy – Heat \rightarrow

Water Phase transition



Does this mean it is a first order phase transition?

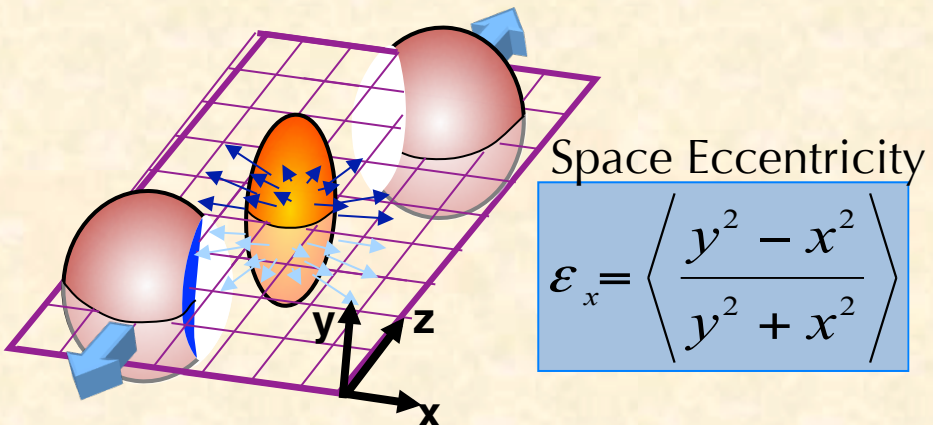
- No, lattice QCD says it is a cross-over.
- No, this behavior is due to confinement. This is a special matter!

How to study the properties of this strange QGP matter!

Having a sample of 10^{-14} m that last for 10^{-23} sec?

I will pick-up one example ...

Anisotropic Expansion in the transverse plane



$$\epsilon_x = \left\langle \frac{y^2 - x^2}{y^2 + x^2} \right\rangle$$

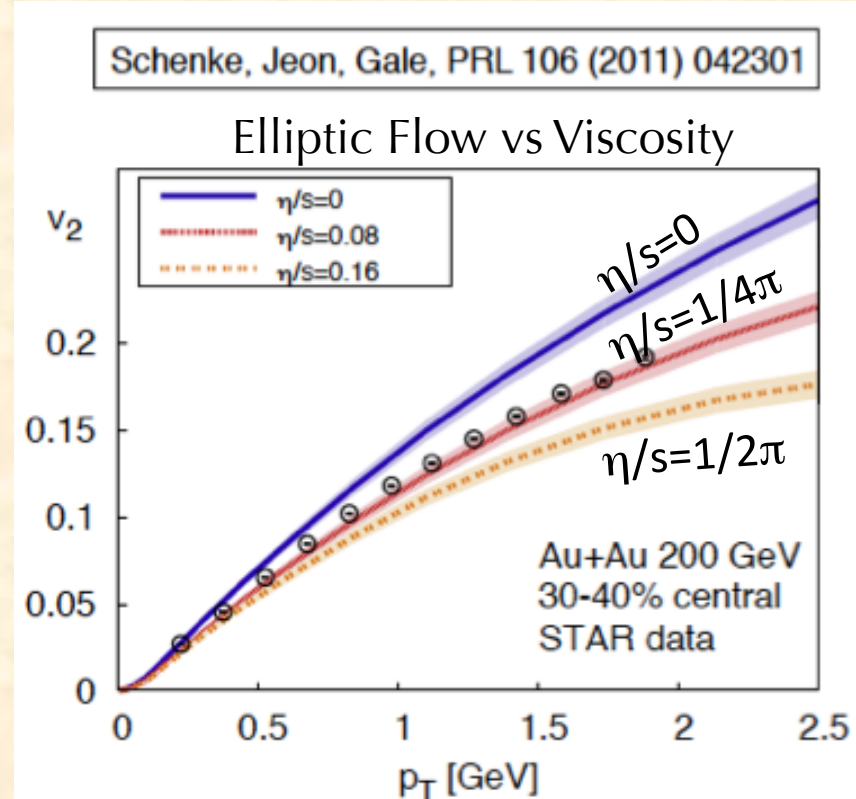
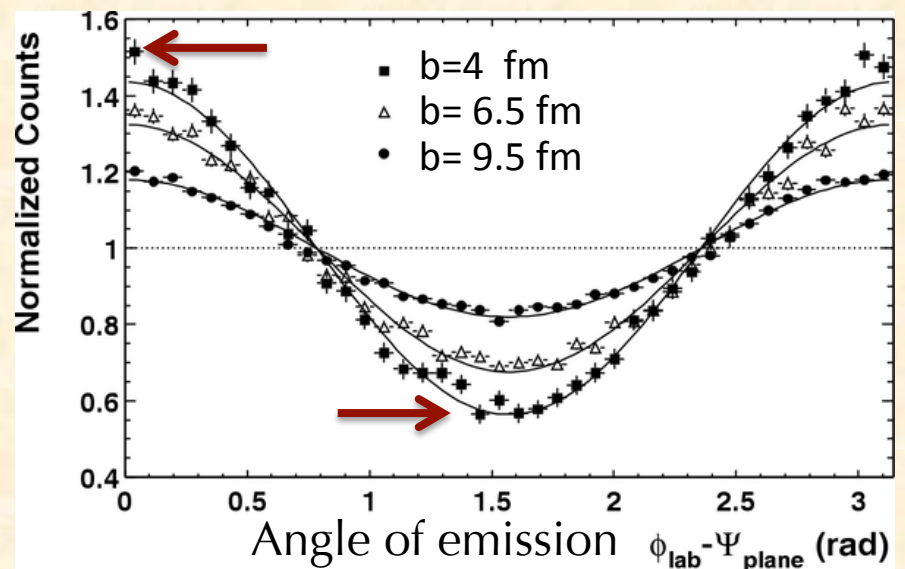
η/s viscosity
 \longleftrightarrow
 $c_s^2 = dP/d\varepsilon$ - EoS

Elliptic Flow

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle = \langle \cos(2\phi_p) \rangle$$

Coefficient Fourier expansion

$$\frac{dN}{dp_T d\phi} = \frac{dN}{dp_T} \left[1 + 2v_2 \cos(2\phi) + \dots \right]$$



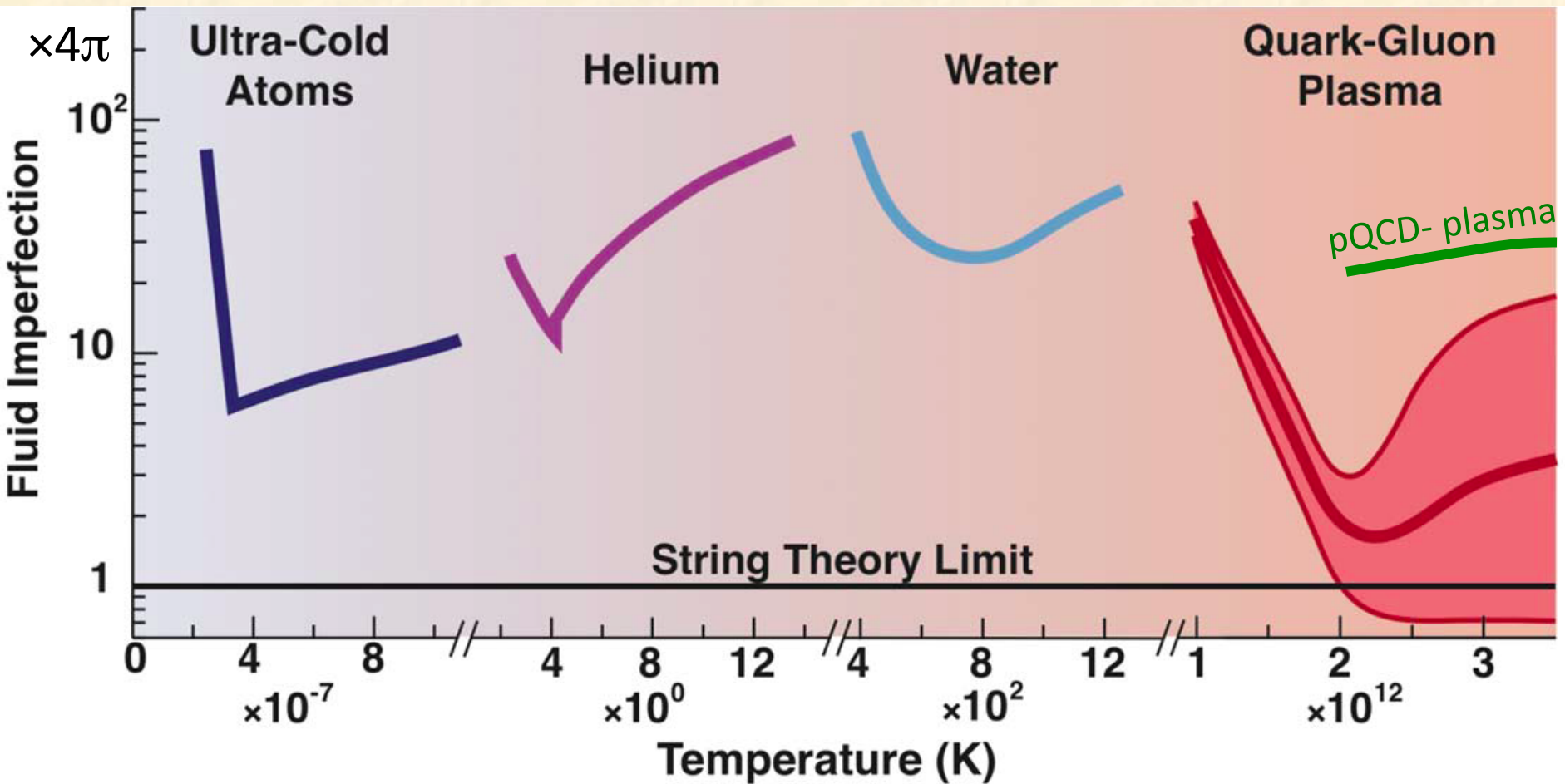
Just one Note ...

1) Trivial after solving Relativistic Viscous Hydrodynamics at Π° order

$$\begin{aligned}
 \tau_\Pi \dot{\Pi} + \Pi &= \Pi_{\text{NS}} + \tau_{\Pi q} q \cdot \dot{u} - \ell_{\Pi q} \partial \cdot q - \zeta \hat{\delta}_0 \Pi \theta \\
 &\quad + \lambda_{\Pi q} q \cdot \nabla \alpha + \lambda_{\Pi \pi} \pi^{\mu\nu} \sigma_{\mu\nu} \\
 \tau_q \Delta^{\mu\nu} \dot{q}_\nu + q^\mu &= q_{\text{NS}}^\mu - \tau_{q\Pi} \Pi \dot{u}^\mu - \tau_{q\pi} \pi^{\mu\nu} \dot{u}_\nu \\
 &\quad + \ell_{q\Pi} \nabla^\mu \Pi - \ell_{q\pi} \Delta^{\mu\nu} \partial^\lambda \pi_{\nu\lambda} + \tau_q \omega^{\mu\nu} q_\nu - \frac{\kappa}{\beta} \hat{\delta}_1 q^\mu \theta \\
 &\quad - \lambda_{qq} \sigma^{\mu\nu} q_\nu + \lambda_{q\Pi} \Pi \nabla^\mu \alpha + \lambda_{q\pi} \pi^{\mu\nu} \nabla_\nu \alpha \\
 \tau_\pi \dot{\pi}^{\langle\mu\nu\rangle} + \pi^{\mu\nu} &= \pi_{\text{NS}}^{\mu\nu} + 2 \tau_{\pi q} q^{\langle\mu} \dot{u}^{\nu\rangle} \\
 &\quad + 2 \ell_{\pi q} \nabla^{\langle\mu} q^{\nu\rangle} + 2 \tau_\pi \pi_\lambda^{\langle\mu} \omega^{\nu\rangle\lambda} - 2 \eta \hat{\delta}_2 \pi^{\mu\nu} \theta \\
 &\quad - 2 \tau_\pi \pi_\lambda^{\langle\mu} \sigma^{\nu\rangle\lambda} - 2 \lambda_{\pi q} q^{\langle\mu} \nabla^{\nu\rangle} \alpha + 2 \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu}
 \end{aligned}$$

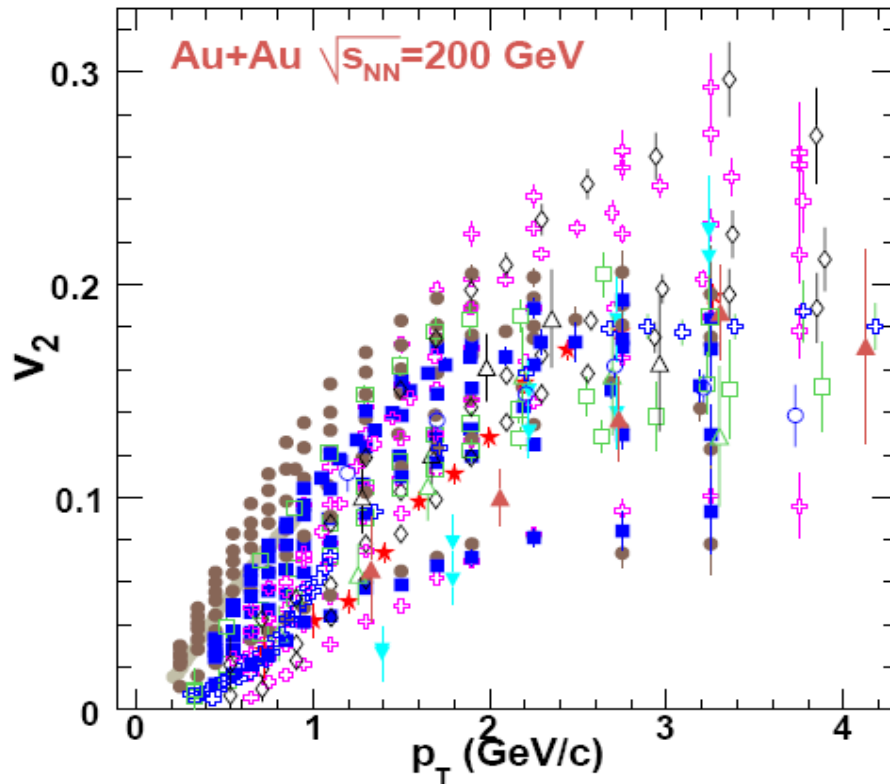
All is done assuming that matter created is thermal at $\tau \approx O(1\text{fm}/c)$

Shear Viscosity for systems in 20 order of T magnitudes!



Report to the Nuclear Science Advisory Committee in 2013

One more thing about elliptic flow



V_2 baryons and mesons

PHENIX (Phys.Rev.Lett.91, Preliminary: QM05, GRC 06)

- - $\pi^+\pi^-$: min.bias, 0-10%, 10-20%, 20-30%, 30-40%, 40-50%, 20-60%
- - π^0 : min.bias
- - K^+K^- : min.bias, 0-10%, 10-20%, 20-30%, 30-40%, 40-50%, 20-60%
- ⊕ - $p+\bar{p}$: min.bias, 0-10%, 10-20%, 20-30%, 30-40%, 40-50%, 20-60%
- ▼ - d : min.bias, 10-50%
- △ - ϕ : 20-60%

STAR (Phys.Rev.Lett. 92, Phys.Rev.C72(2005), Preliminary QM05, SQM06)

- - $\pi^+\pi^-$: min.bias
- - K_S^0 : min.bias, 5-30%, 30-70%
- ⊕ - $p+\bar{p}$: min.bias
- ◇ - $\Lambda+\bar{\Lambda}$: min.bias, 5-30%, 30-70%
- ★ - $\Xi+\bar{\Xi}$: min.bias
- ▲ - $\Omega+\bar{\Omega}$: min.bias

Always one question bounces back!

Can we see how and if quarks are flowing?

Confinement: we can see only hadrons flowing

My first Proceedings on QGP...

BUDAPEST 2002 WORKSHOP ON
**QUARK AND HADRON
DYNAMICS**

IN HONOR OF
**JUDIT NÉMETH,
ISTVÁN LOVAS AND
JÓZSEF ZIMÁNYI**



Lévai

Budapest 2002 Workshop on
Quark and Hadron Dynamics


SYSTEMA

Texas A&M, October 2002 – gift from Peter Levai

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JÓZSEF ZIMÁNYI



Texas A&M, October 2012 – gift from Peter Levai

Discussing at lunch with **Peter Levai**
(Director of MTA Wigner-Budapest...)

P. Levai



fat Burger

V. Greco



My first Proceedings on QGP...

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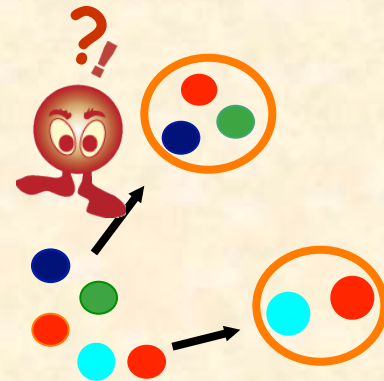
SYSTEMA

Texas A&M, October 2012 – gift from Peter Levai

“In **ALgebraic COalescenceRecombination** model we assume that just before the hadronization the dense matter can be described as a mixture of dressed up, **massive quarks and antiquarks ...**”

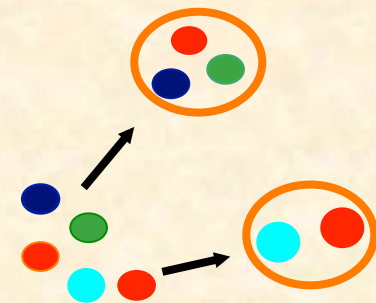
By J. Zimanyi and the Budapest group

If you have a medium of quarks
Why you need the vacuum to
hadronize?



In Texas we moved to
observables in momentum space

Recombination enhances Anisotropies



Meson recombination(qq)

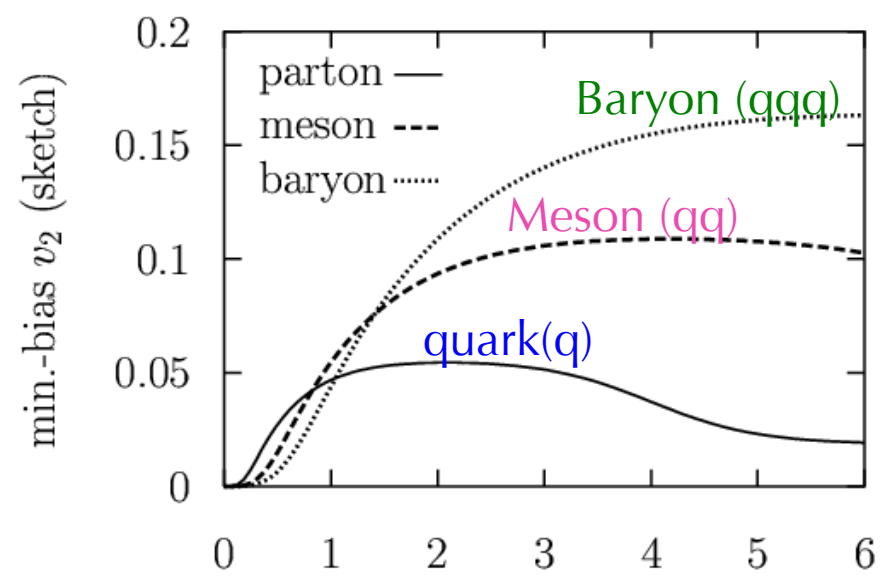
$$f_H(\mathbf{P}_H = 2\mathbf{p}_T) \approx f_q(\mathbf{p}_T) \otimes f_{\bar{q}}(\mathbf{p}_T)$$

Baryon recombination(qqq)

$$f_H(\mathbf{P}_H = 3\mathbf{p}_T) \approx f_q(\mathbf{p}_T) \otimes f_q(\mathbf{p}_T) \otimes f_q(\mathbf{p}_T)$$

$$\approx [1 + v_{2q}(p_T) \cos(2\varphi_p) + \dots]^2 \approx 1 + 2v_{2q}(2p_T) \cos(2\varphi_p) + \dots$$

$$\approx [1 + v_{2q}(p_T) \cos(2\varphi_p) + \dots]^3 \approx 1 + 3v_{2q}(3p_T) \cos(2\varphi_p) + \dots$$



Two branches

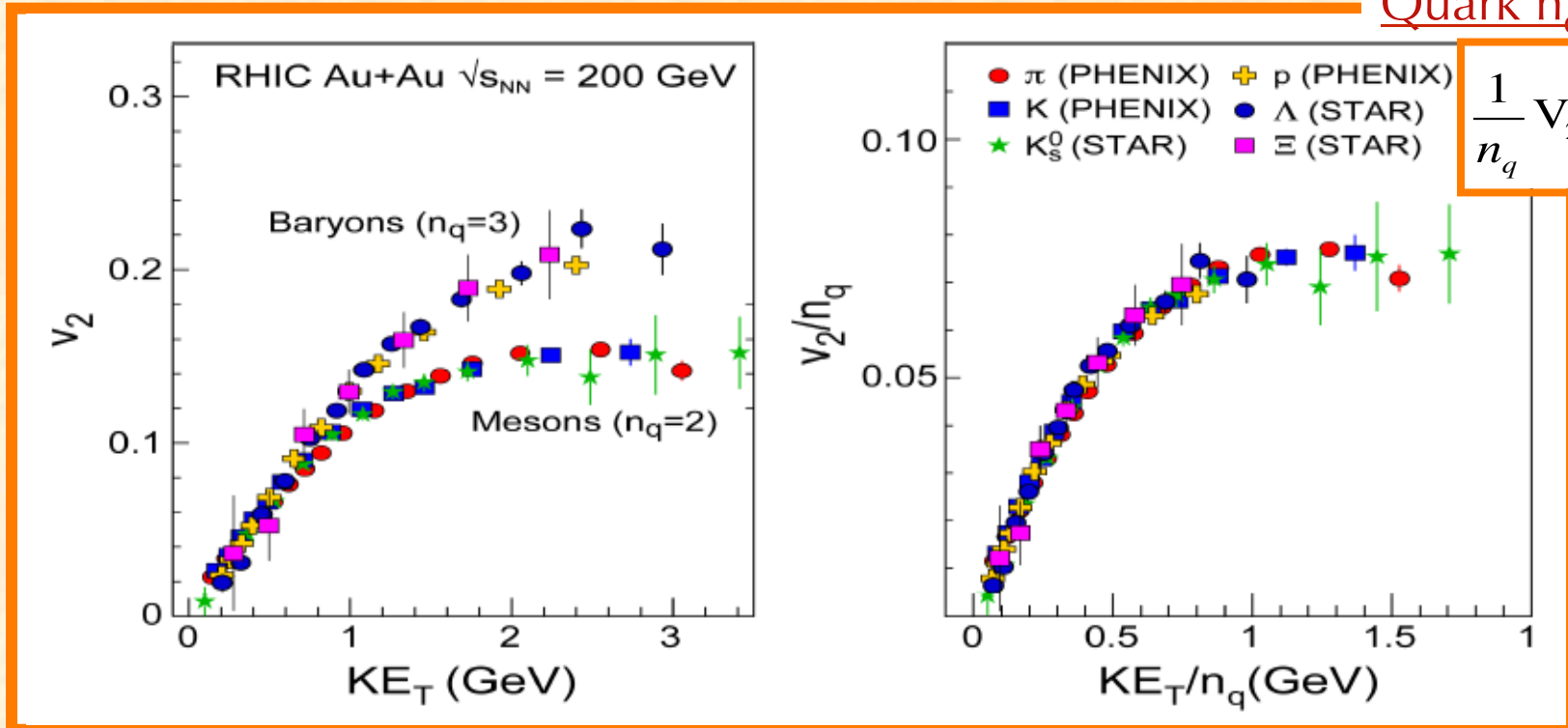
$$v_{2,M}(p_T) \approx 2v_{2,q}(p_T/2)$$

$$v_{2,B}(p_T) \approx 3v_{2,q}(p_T/3)$$

Discarding space-momentum correlation, hadron wave function width, event-by-event fluctuations, Resonance decays, ...

Too beautiful to be true? ...

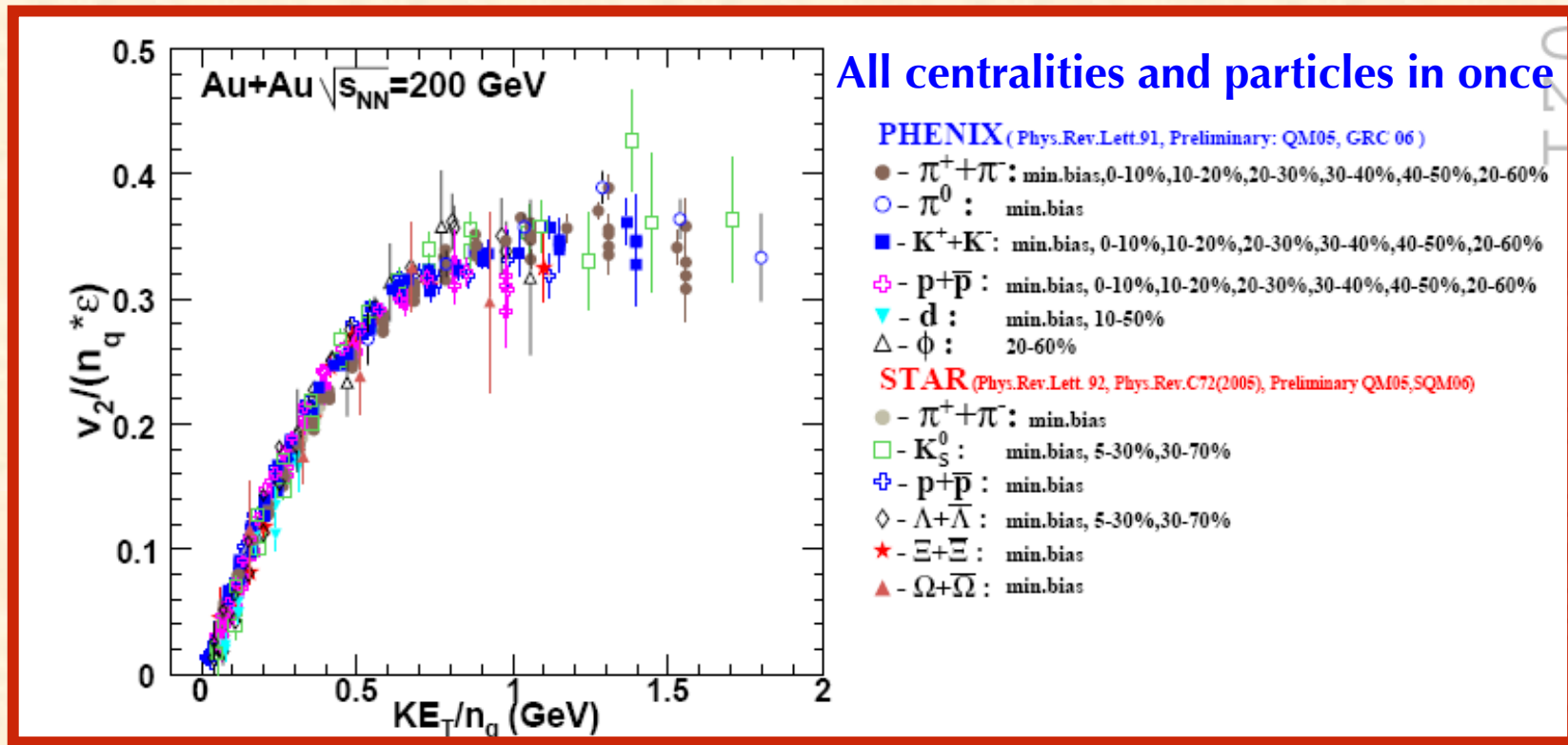
Quark n_q scaling



PHENIX, PRL 98(2007)

Anisotropic Flow formed at partonic level, one common QGP flow
Flow depends on quark content \rightarrow two branches; Meson and Baryon

Too beautiful to be true ...



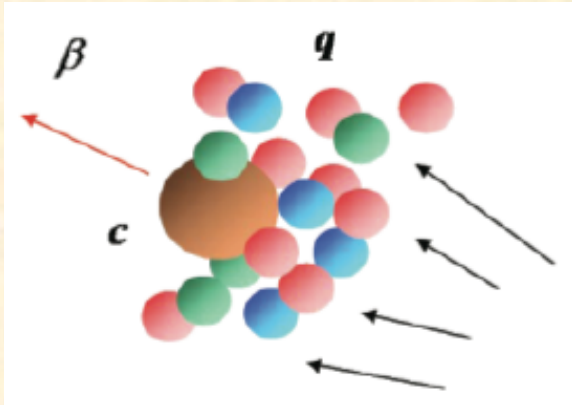
Everything rescales in one common flow!

We “see” the underlying quark flow.. with some distortion

an elephant in the liquid



An elephant in the liquid: Heavy Charm Quark



Brownian motion

$$\frac{\partial f_{c,b}}{\partial t} = \gamma \frac{\partial (p f_{c,b})}{\partial p} + D \frac{\partial^2 f_{c,b}}{\partial p^2}$$

Drag

Diffusion

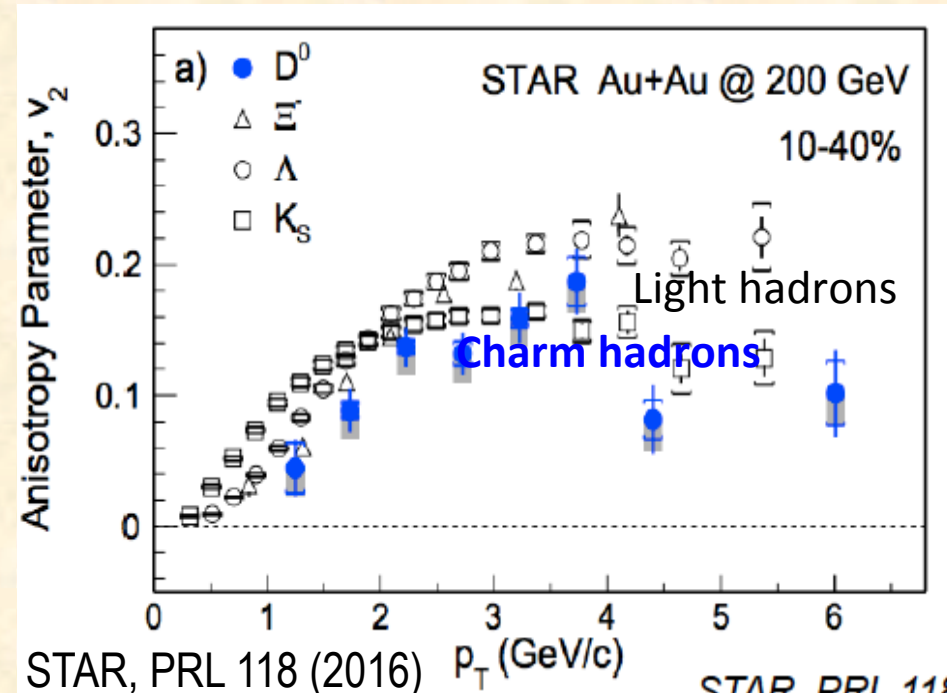
QGP created is made by 99% of $q=u,d,s$, $m_q \approx 10 \text{ MeV}$
 + few Heavy Charm Quarks: $M_c \approx 1500 \text{ MeV}$

Standard Kinetic theory:

Poorly dragged & long thermalization time

$$\tau_{C,therm} \approx O(10^2) \gg \tau_{QGP} \gg \tau_{q,therm} \approx O(1) \text{ fm/c}$$

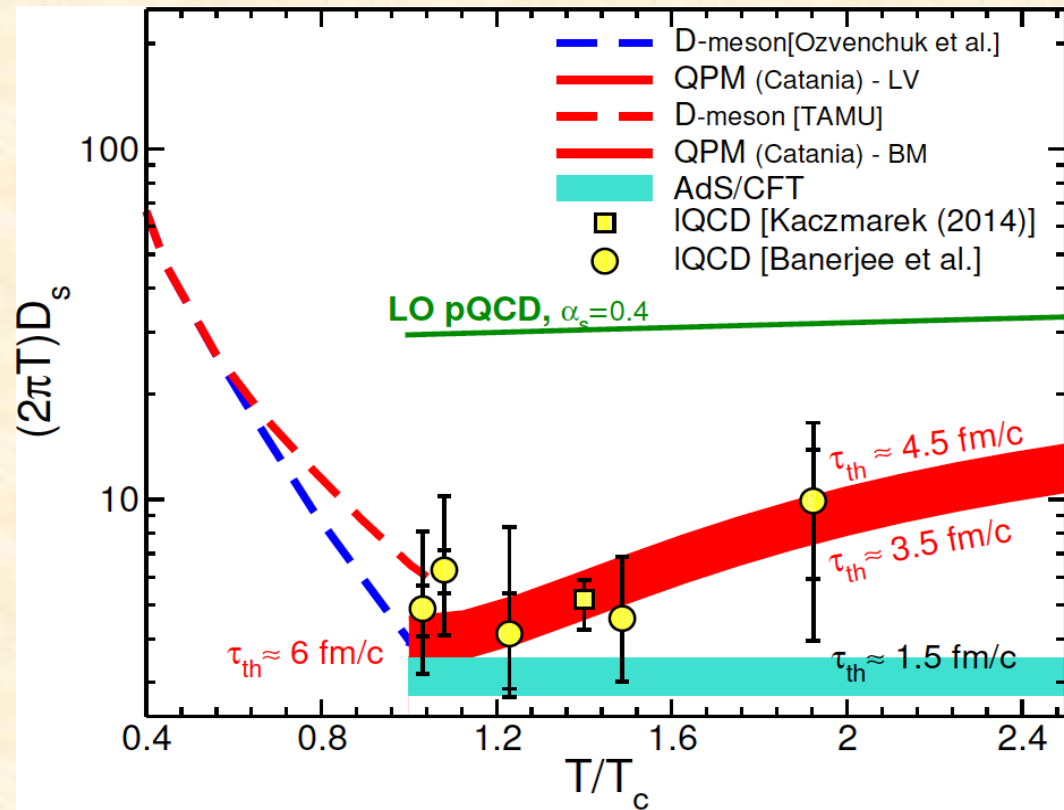
How they flow



1992: B. Muller, NATO Advanced Study Institute

“For plasma conditions realistically obtainable in the nuclear collisions ($T \sim 250 \text{ MeV}$, $g = 2$) the **effective quark & gluon mass $m^* \sim 400 \text{ MeV}$** . We must conclude, therefore, that the notion of almost **free gluons and quarks in the high T phase of QCD is quite far from the truth.**”

Diffusion Coefficient of Charm Quark



$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

Asymptotic free regime

Not a model fit to IQCD data!
Phenomenology \approx lattice QCD

Infinite Strong Coupling (AdS/CFT)

- Created matter is the **Hot QCD matter in non perturbative regime!**
- Likely a U shape typical of matter undergoing a phase transition
- $T \rightarrow T_c$ gets close to the AdS/CFT limit

Perspectives...

- **Characterizing viscosity η/s , bulk ξ/σ , conductivity σ_{el} , diffusion D_s :**
 - Important to understand QCD at high T up to pert. QCD regime
 - Provide a precise background for cosmology (Ex. WIMP relic density...)
- **Study Matter behavior under Huge Magnetic fields (10^{18} Gauss)**
 - Charge-Parity violation in Strong Interaction?
- **At TeV scale new view on pp collisions is emerging**
 - relevance for High-Energy Astrophysics at PeV scale and above

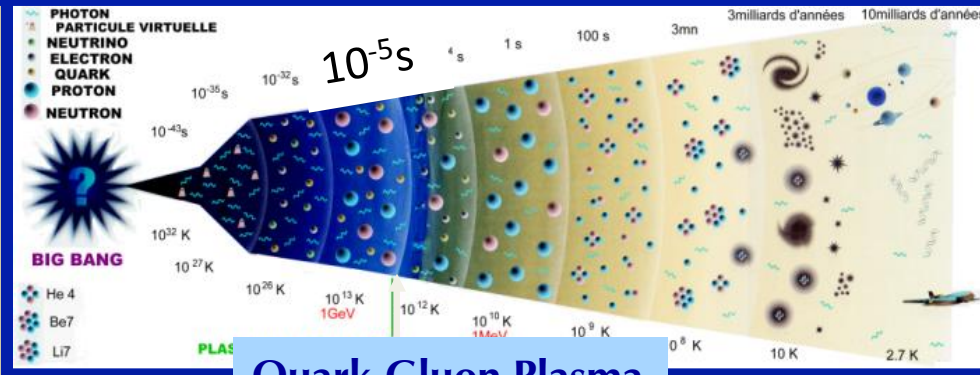
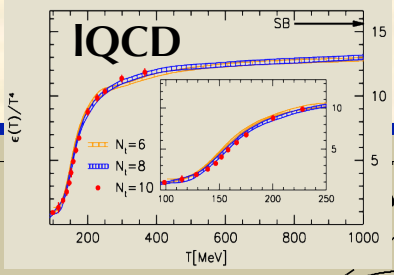
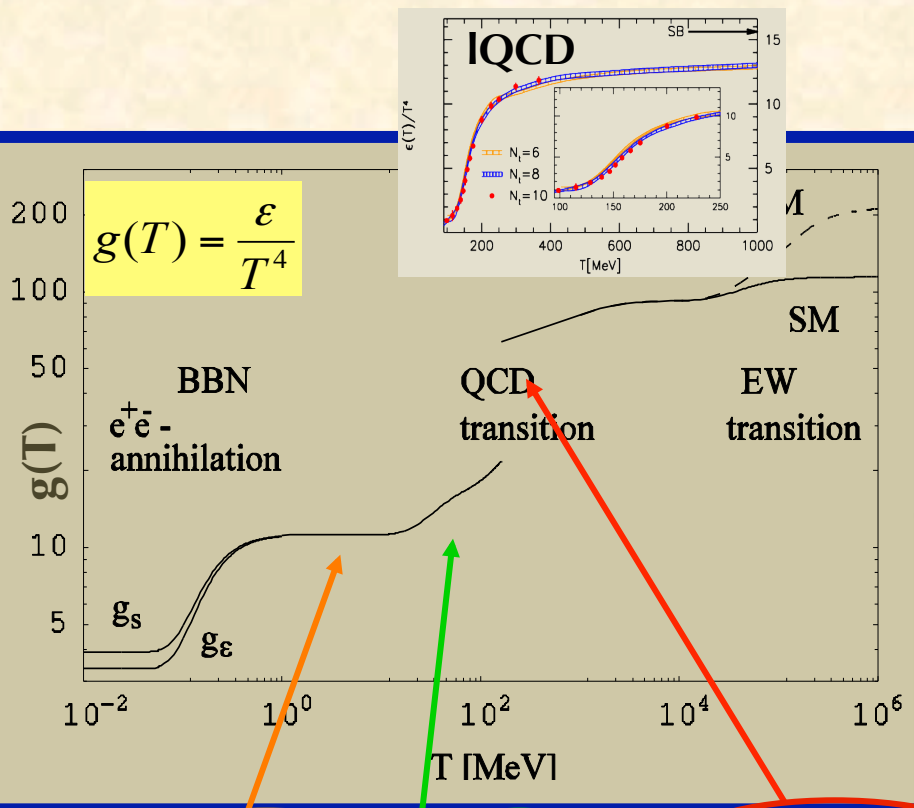


A Great Honor to be a member of this Academia!

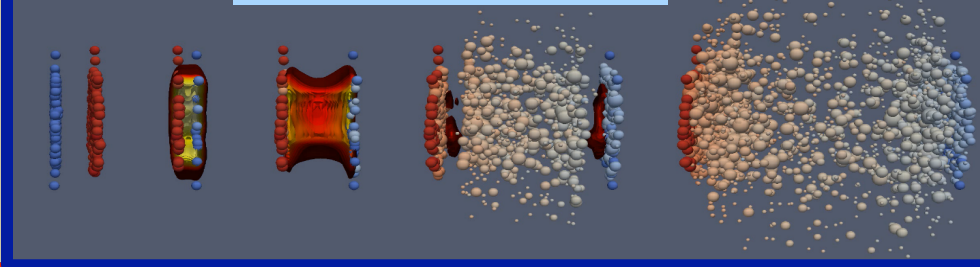
A very pleasant feeling to see the benevolent
view of elder Colleagues!

An emotional coincidence to enter AE in Budapest!

Degrees of freedom in the Universe



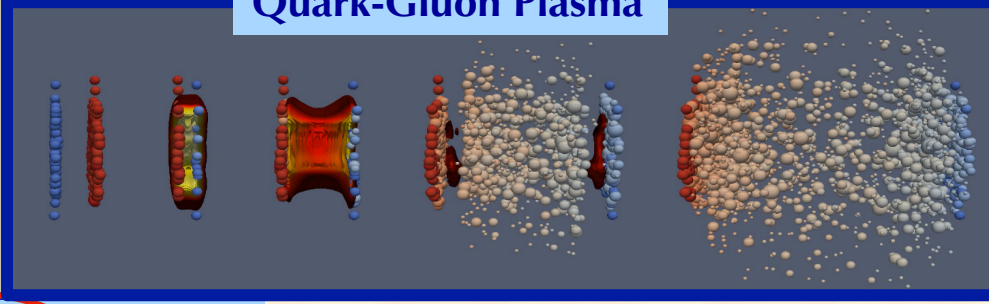
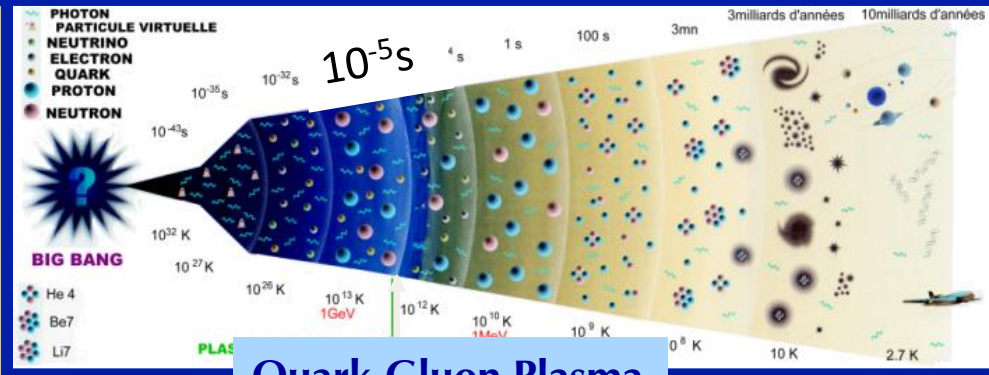
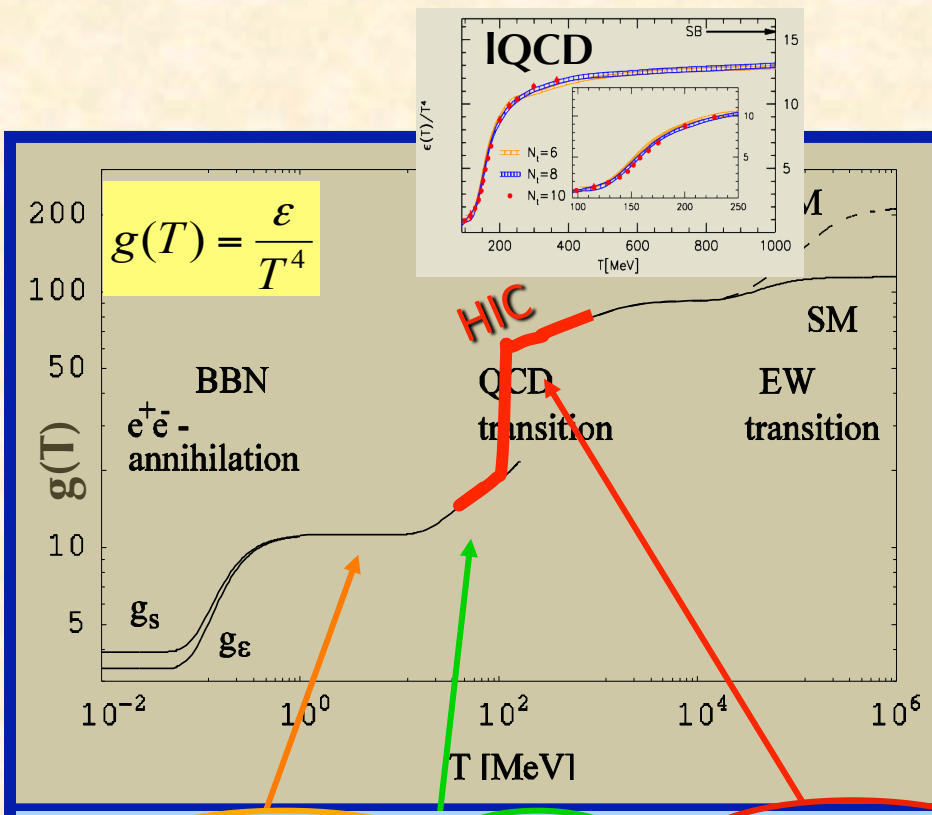
Quark-Gluon Plasma



$$g(T) = 2_\gamma + 4_e + 4_\nu + 3_\mu + 3_\pi + \dots + 16_g + 31.5_{uds} + 21_{cb} + \dots$$

Disappearance of colored matter the most drastic event

Degrees of freedom in the Universe

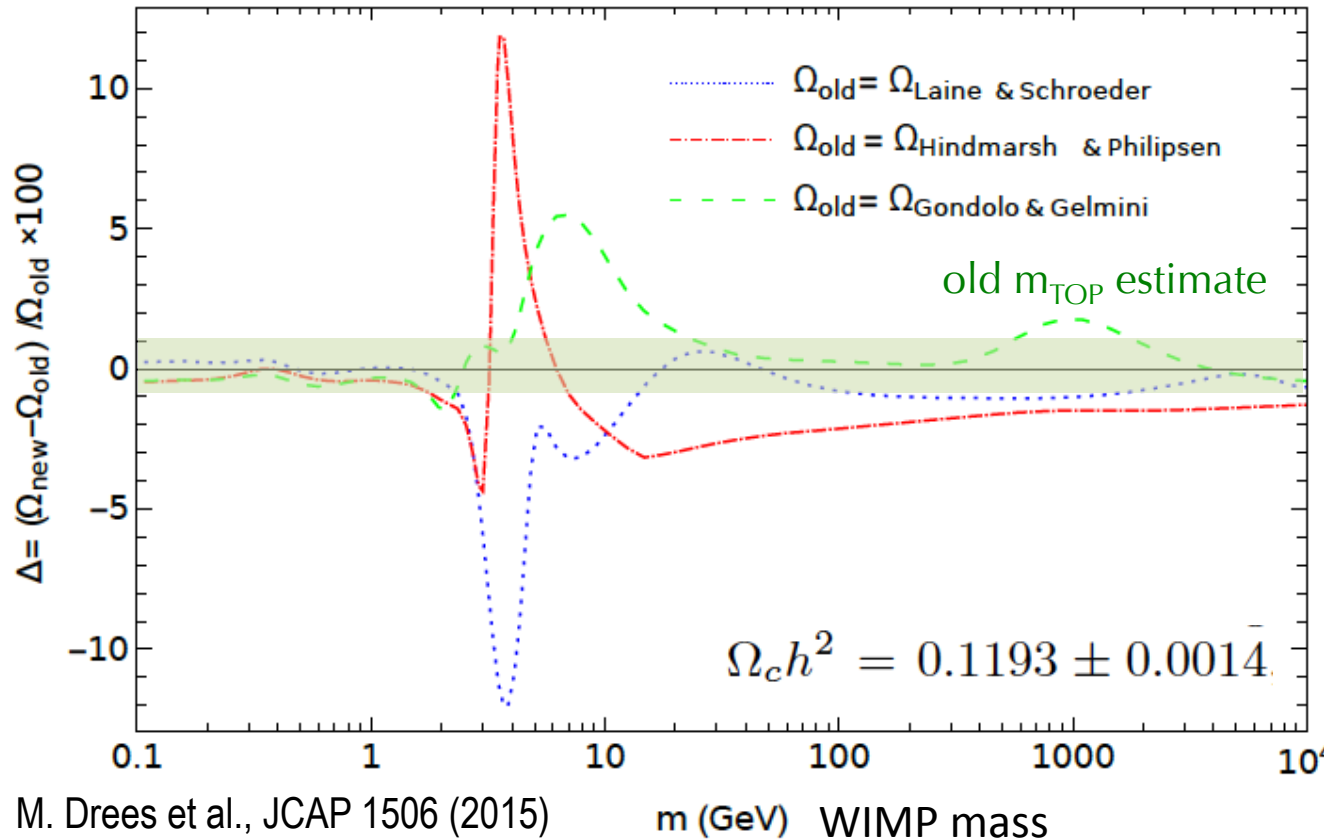


$$g(T) = 2_\gamma + 4_e + 4_\nu + 3_\mu + 3_\pi + \dots + 16_g + 31.5_{uds} + 21_{cb} + \dots$$

Disappearance of colored matter the most drastic event

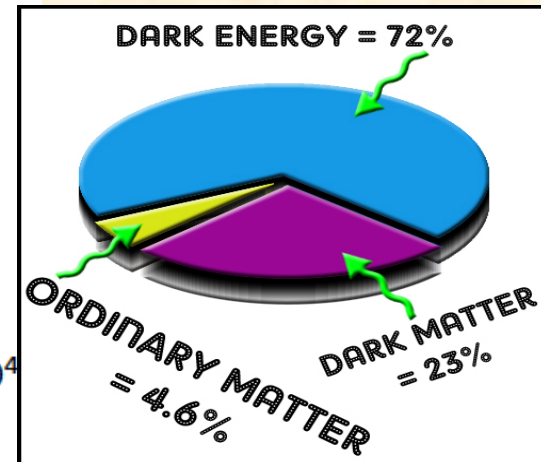
QCD EoS and the Relic WIMP Dark Matter

% variation of Ω due to different QCD EoS



PLANCK estimate to determine Ω with 1% precisions

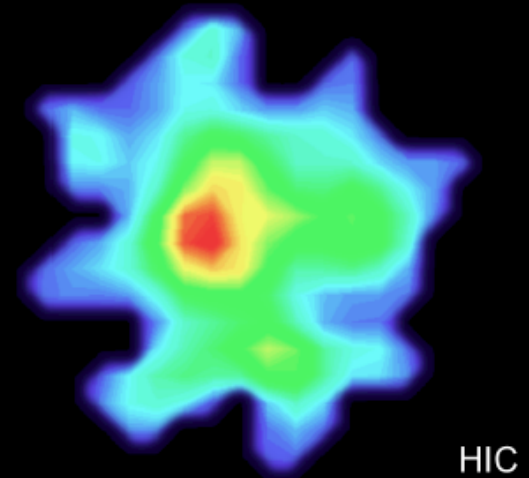
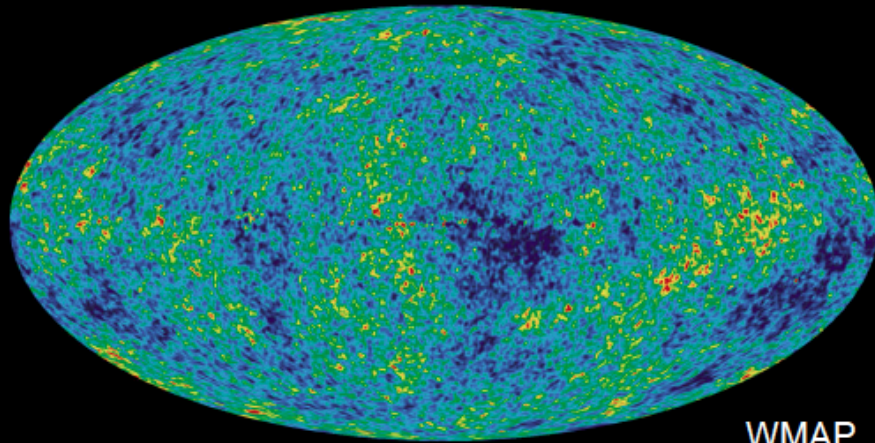
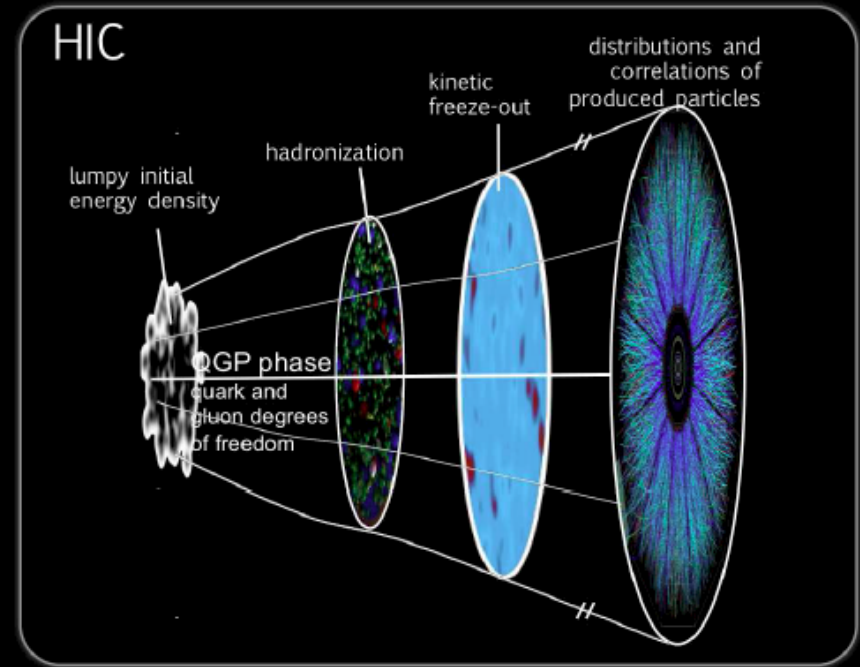
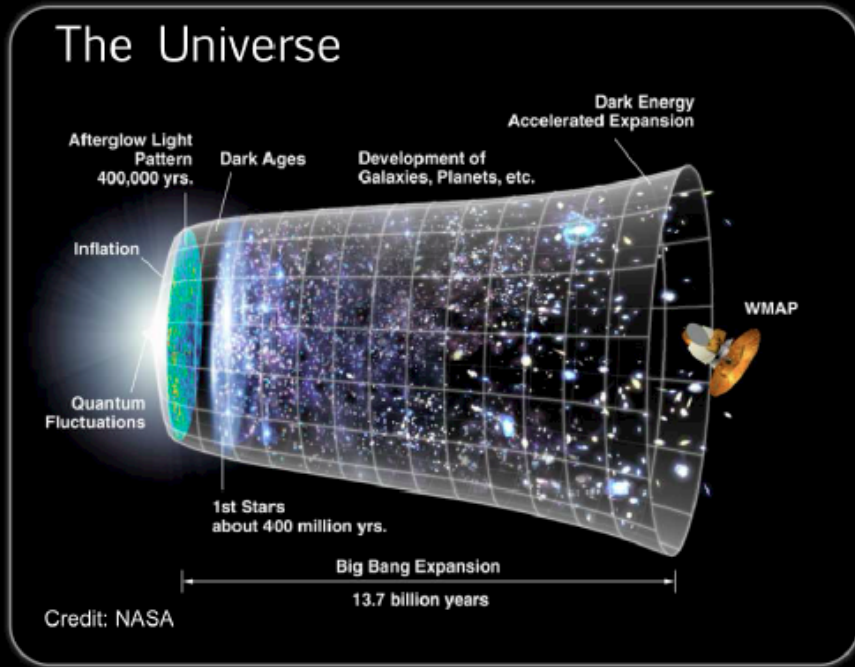
$$\Omega_c = \frac{\rho_{DM}}{\rho_c}$$



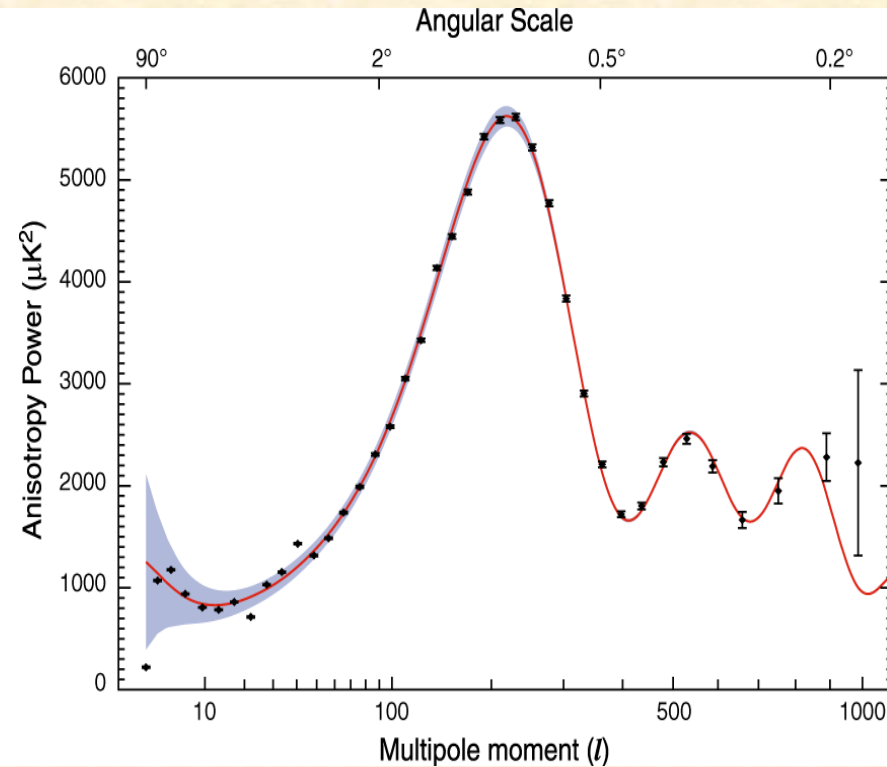
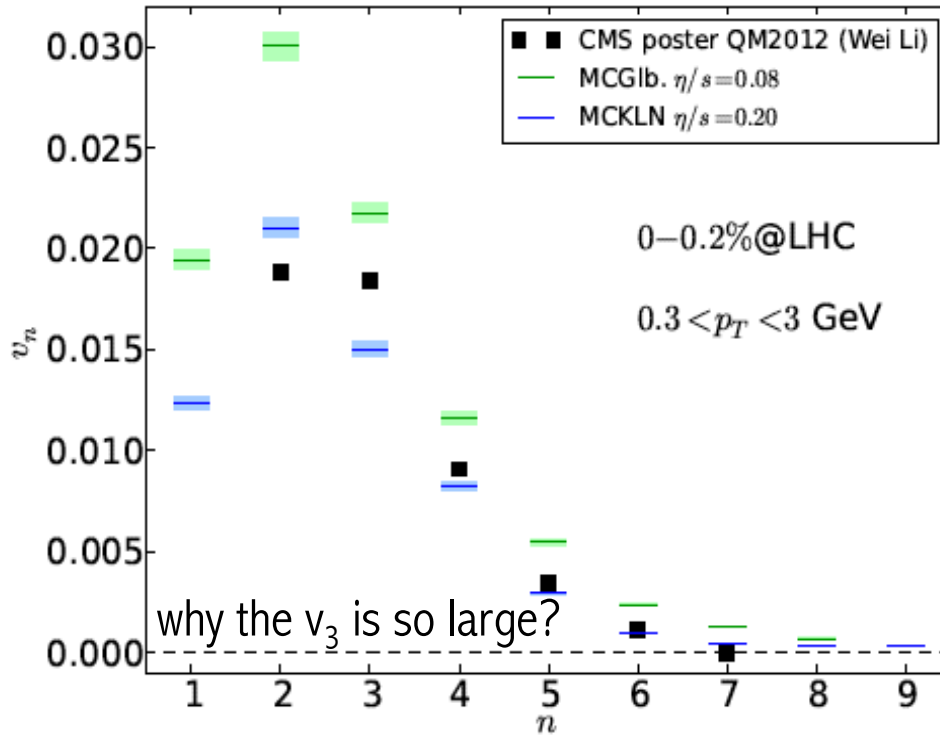
Under the assumption of isentropic Early Universe expansion

- We are now determining viscosities $\eta/s(T)$, $\zeta/s(T) \rightarrow$ entropy production
- We will see in the future the impact of the knowledge of Hot QCD

Another analogy with Early Universe expansion



Going deeply into Hot QCD matter



- Initial QCD quantum fluctuations
- T dependence of η/s
- Equation of State
- Freeze-out dynamics

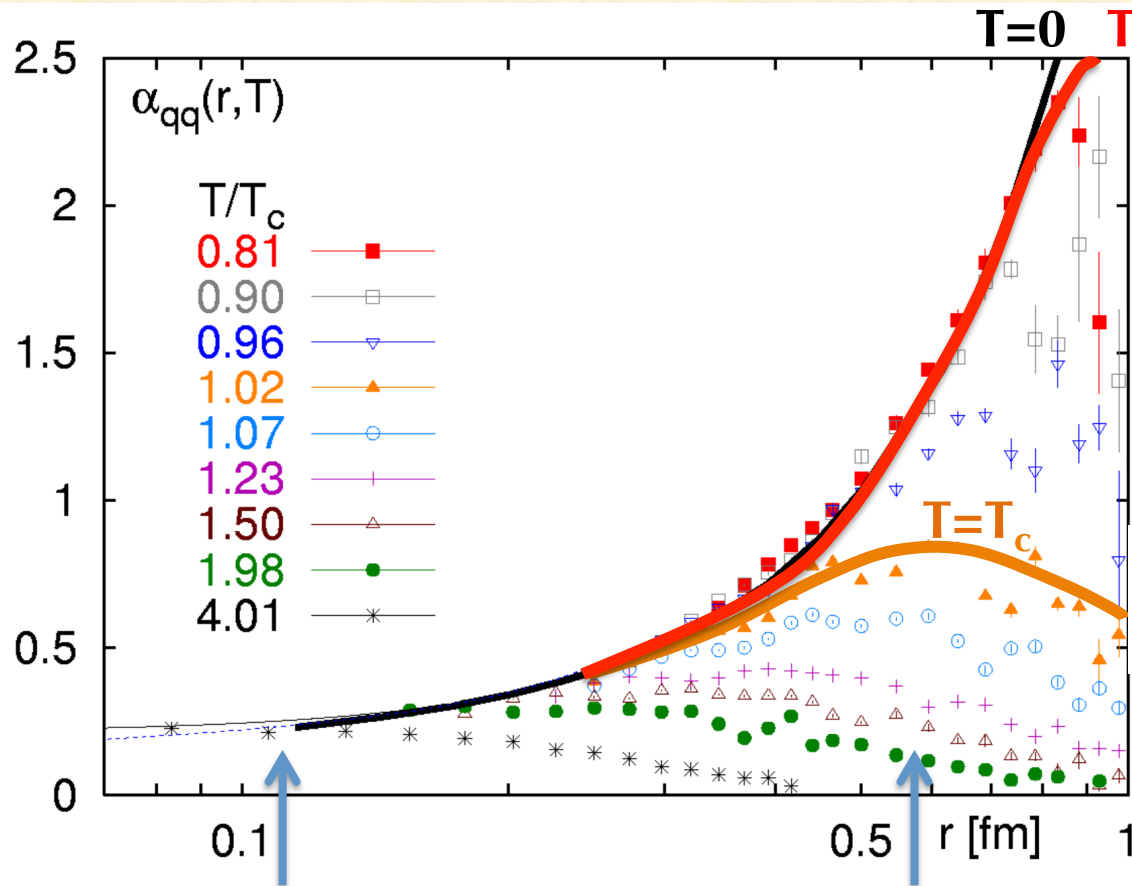
Keeping size and life-time of QGP

- Standard Model Matter
- Cold Dark Matter
- Dark Energy
- Hubble Constant

Keeping Age and Flatness of the Universe

Possible because at LHC one starts to create about than 10,000 particle per event

Beyond naive argument: lattice QCD



$$V(r, T) = \frac{4}{3} \frac{\alpha(r, T)}{r}$$

$$\alpha \approx r^2 \rightarrow V \approx Kr$$

$$\alpha(r, T > T_c) = \alpha_{\text{eff}}(T) e^{-m_D(T)r}$$

High-Temperature medium screens the Confinement

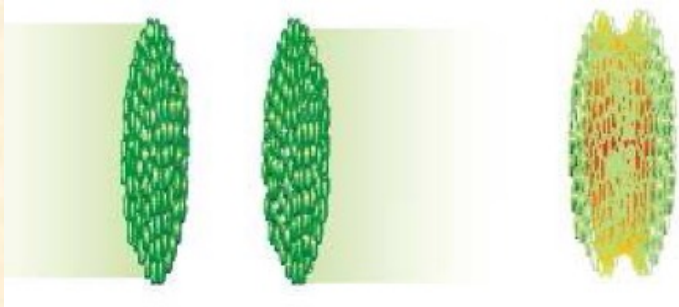
QCD vacuum is diamagnetic: repels fields lines

Perturbative regime
 $\alpha \approx \log(r/r_0) \leq 0.25$

Average distance
 at ρ_c

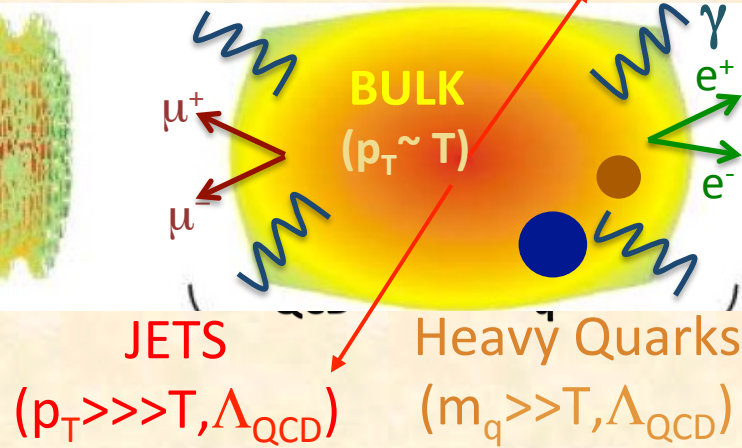
Multifacets Physics

Initial Conditions



Color Glass Cond.
Gluon saturation

Quark-Gluon Plasma

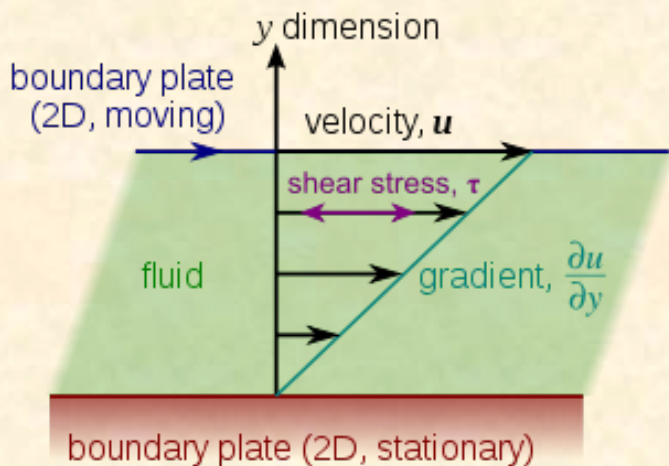


Hadronization

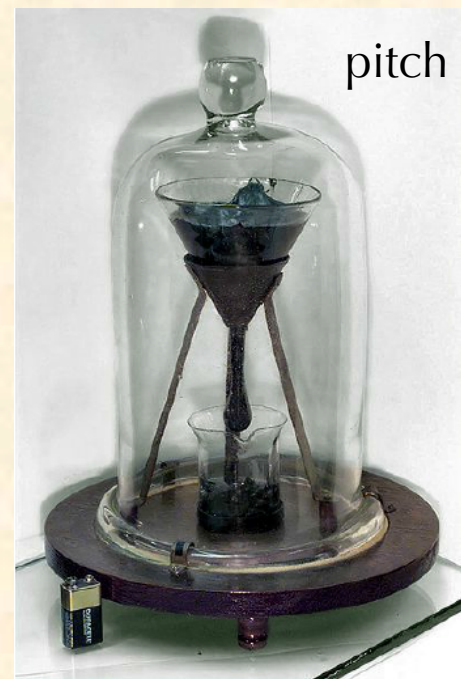


Microscopic
Mechanism
Matters!

Why is Shear Viscosity is relevant



$$\frac{F_x}{A_{yz}} = -\eta \frac{\partial v_x}{\partial y}$$



$\eta = (2.3 \pm 0.5) \cdot 10^8 \text{ Pa} \cdot \text{s}$
8 drops 1932-2013

Text book kinetic theory

$$\frac{\eta}{s} \approx \frac{1}{15} \langle p \rangle \cdot \lambda$$

Small $\eta/s \rightarrow$ small mean free path λ
 \rightarrow strongly coupled system

At limits of Quantum mechanism ($\langle p \rangle \approx \Delta E$, $\lambda \approx c\Delta t$)

$$\Delta E \cdot \Delta t \geq 1 \rightarrow \eta/s > 1/15 \quad \text{which for QGP mean } \eta > 10^{11} \text{ Pa} \cdot \text{s}$$

AdS/CFT, based on the conjecture that a Gauge theory in 4D (in the infinite coupling limit) is dual to a gravitational calculation in 5D gives $\eta/s > 1/4\pi$

Shear viscosity of some substances



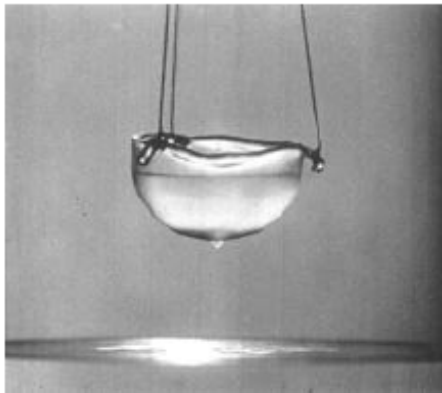
honey:

$$\eta \sim (2 - 10) Pa \cdot s$$



water:

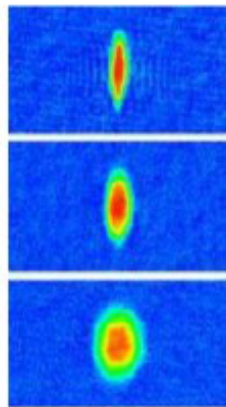
$$\eta \sim (10^{-3} - 10^{-4}) Pa \cdot s$$



liquid ^4He :

$$T = 5.1 \text{ K}$$

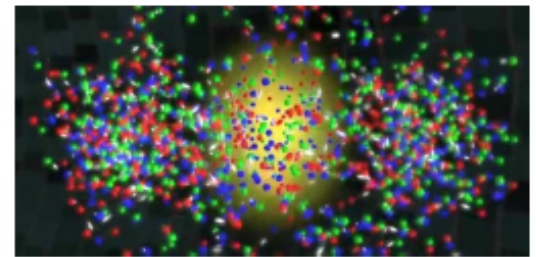
$$\eta = 1.7 \cdot 10^{-6} Pa \cdot s$$



trapped ^6Li :

$$T = 23 \cdot 10^{-6} \text{ K}$$

$$\eta \leq 1.7 \cdot 10^{-15} Pa \cdot s$$



QGP:

$$T = 2 \cdot 10^{12} \text{ K}$$

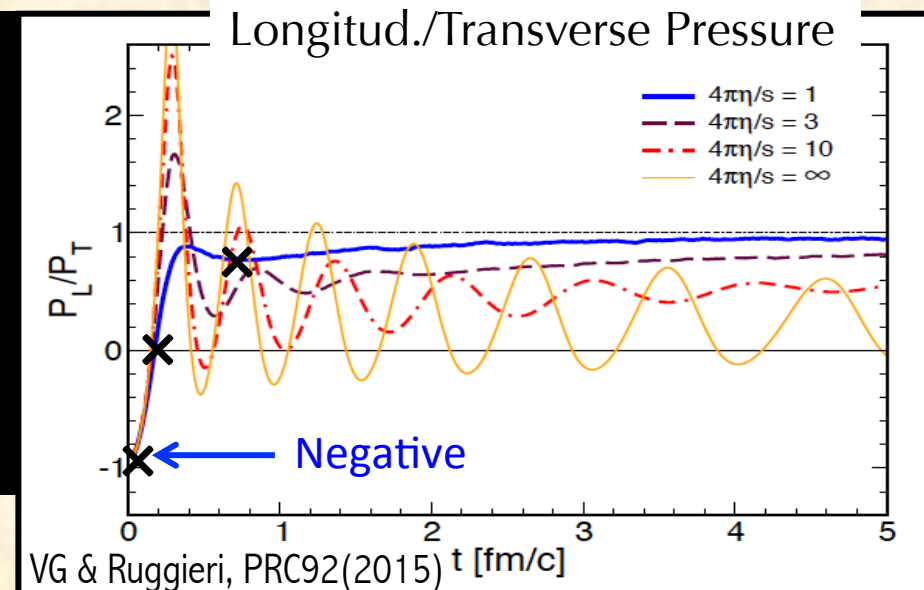
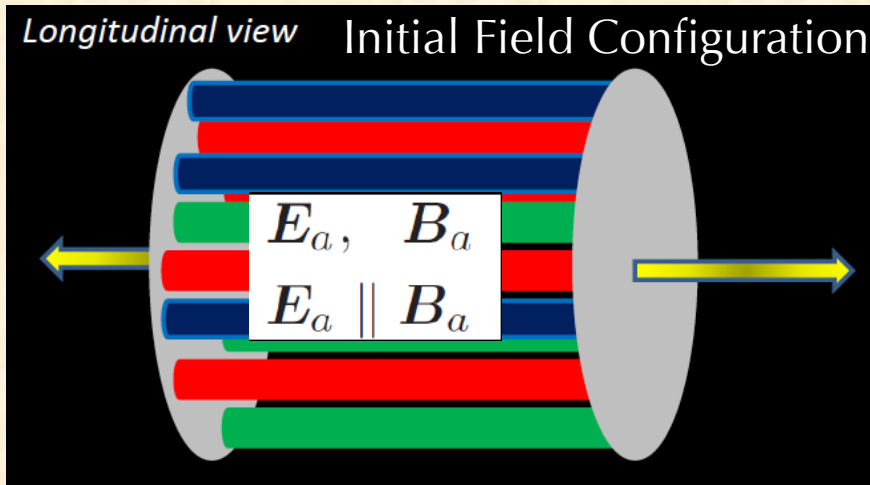
$$\eta \leq 5 \cdot 10^{11} Pa \cdot s$$

Two Notes ...

1) Trivial after solving Relativistic Viscous Hydrodynamics at Π° order

$$\begin{aligned}
 \tau_\Pi \dot{\Pi} + \Pi &= \Pi_{\text{NS}} + \tau_{\Pi q} q \cdot \dot{u} - \ell_{\Pi q} \partial \cdot q - \zeta \hat{\delta}_0 \Pi \theta \\
 &\quad + \lambda_{\Pi q} q \cdot \nabla \alpha + \lambda_{\Pi \pi} \pi^{\mu\nu} \sigma_{\mu\nu} \\
 \tau_q \Delta^{\mu\nu} \dot{q}_\nu + q^\mu &= q_{\text{NS}}^\mu - \tau_{q\Pi} \Pi \dot{u}^\mu - \tau_{q\pi} \pi^{\mu\nu} \dot{u}_\nu \\
 &\quad + \ell_{q\Pi} \nabla^\mu \Pi - \ell_{q\pi} \Delta^{\mu\nu} \partial^\lambda \pi_{\nu\lambda} + \tau_q \omega^{\mu\nu} q_\nu - \frac{\kappa}{\beta} \hat{\delta}_1 q^\mu \theta \\
 &\quad - \lambda_{qq} \sigma^{\mu\nu} q_\nu + \lambda_{q\Pi} \Pi \nabla^\mu \alpha + \lambda_{q\pi} \pi^{\mu\nu} \nabla_\nu \alpha \\
 \tau_\pi \dot{\pi}^{\langle\mu\nu\rangle} + \pi^{\mu\nu} &= \pi_{\text{NS}}^{\mu\nu} + 2 \tau_{\pi q} q^{\langle\mu} \dot{u}^{\nu\rangle} \\
 &\quad + 2 \ell_{\pi q} \nabla^{\langle\mu} q^{\nu\rangle} + 2 \tau_\pi \pi_\lambda^{\langle\mu} \omega^{\nu\rangle\lambda} - 2 \eta \hat{\delta}_2 \pi^{\mu\nu} \theta \\
 &\quad - 2 \tau_\pi \pi_\lambda^{\langle\mu} \sigma^{\nu\rangle\lambda} - 2 \lambda_{\pi q} q^{\langle\mu} \nabla^{\nu\rangle} \alpha + 2 \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu}
 \end{aligned}$$

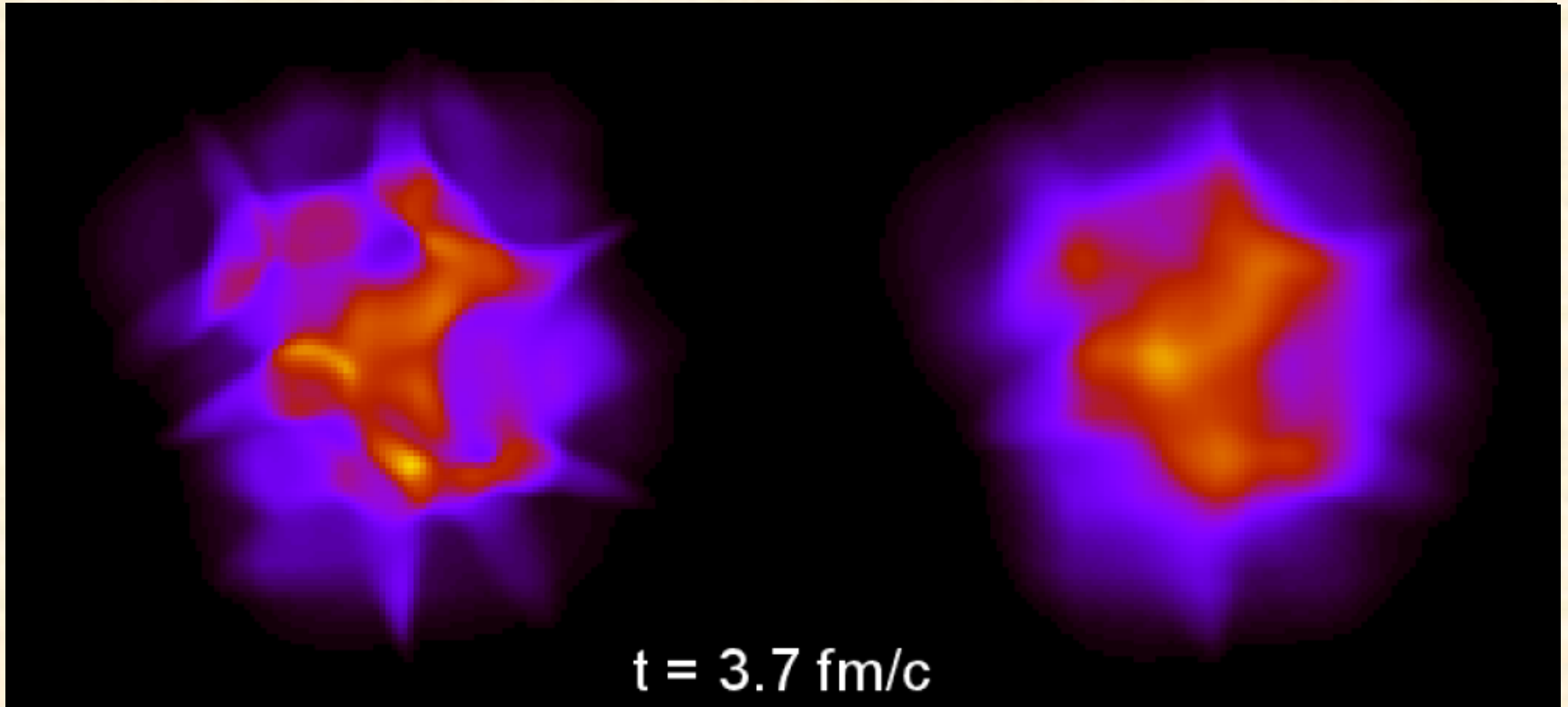
2) All is done assuming that matter created is thermal at $\tau \approx \mathcal{O}(1 \text{ fm}/c)$



η/s smoothen fluctuations and affect more higher harmonics

Ideal

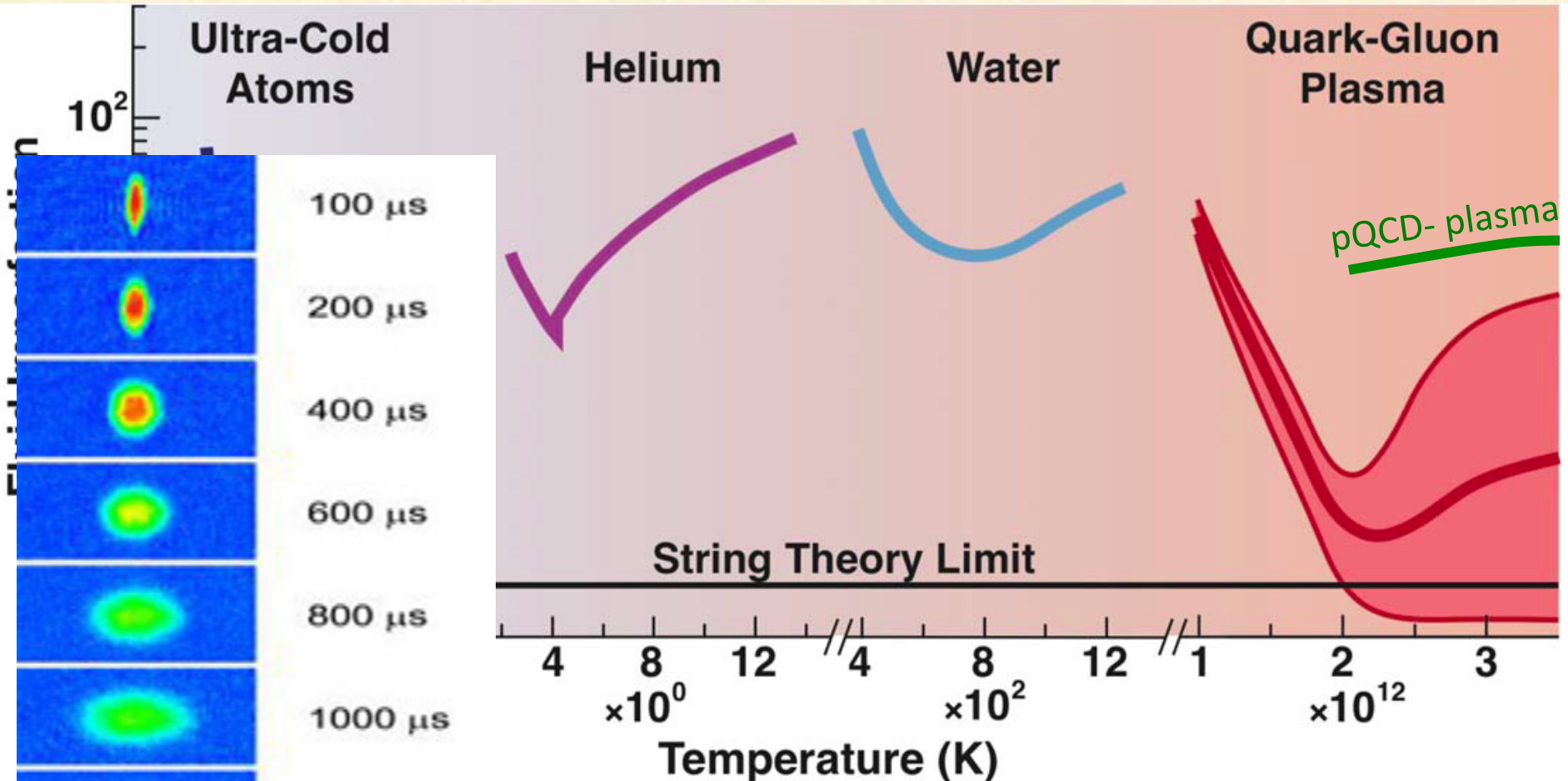
Viscous



$\eta/s=0$

$\eta/s=0.16$

Shear Viscosity for systems in 20 order of T magnitudes!

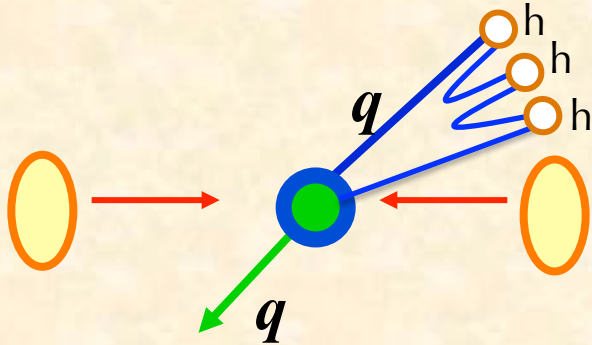


O'Hara et al., Science 298(2002)

Modified Hadronization in AA w.r.t. to ee, ep, pp

Fragmentation: e^+e^- , ep, pp

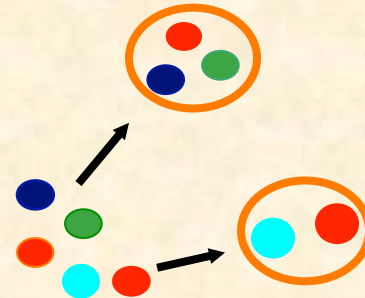
$$f_H(P_H = zp_T) = f_{q,g}(p_T) \otimes D_{q,g \rightarrow H}(z), \quad z < 1$$



Forced by Confinement

Quark recombination

$$f_H(P_H = 2p_T) \approx f_q(p_T) \otimes f_{\bar{q}}(p_T)$$



Favored by DeConfinement

Meson recombination (qq)

$$f_H(P_H = 2\mathbf{p}_T) \approx f_q(\mathbf{p}_T) \otimes f_{\bar{q}}(\mathbf{p}_T)$$

$$\approx [1 + v_{2q}(p_T) \cos(2\varphi_p) + \dots]^2 \approx 1 + \underbrace{2v_{2q}(2p_T)}_{\text{enhancement}} \cos(2\varphi_p) + \dots$$

Ideal Hydrodynamics: a perfect fluid?

$$\begin{cases} \partial_\mu T^{\mu\nu}(x) = 0 \\ \partial_\mu j_B^\mu(x) = 0 \end{cases}$$

$$T^{\mu\nu}(x) = [\varepsilon + p]u^\mu u^\nu - pg^{\mu\nu}$$

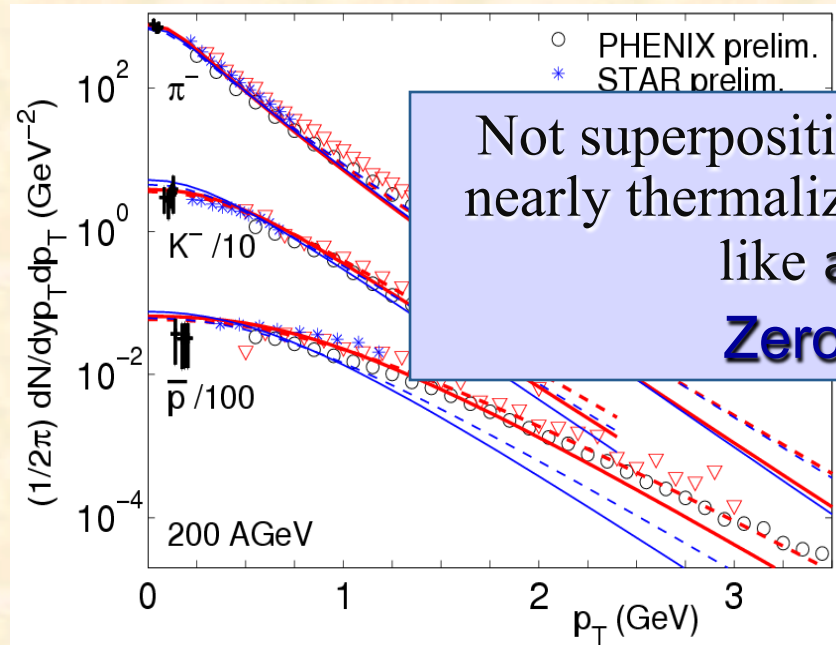
$$T^* \approx T_f + \frac{1}{2}m\langle\beta_T^2\rangle$$

$$\begin{aligned} T_f &\sim 120 \text{ MeV} \\ \langle\beta_T\rangle &\sim 0.5 \end{aligned}$$

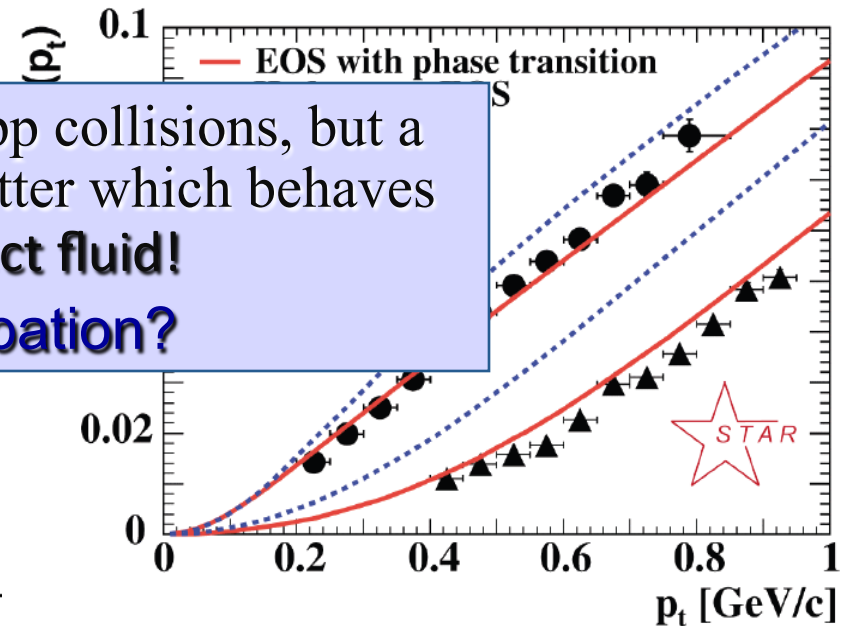
No microscopic description ($\lambda \rightarrow 0$), no dissipation,...only conservation laws!

- Blue shift of dN/dp_T hadron spectra
- Large v_2/ε
- Mass ordering of $v_2(p_T)$

For the first time very close to ideal Hydrodynamics

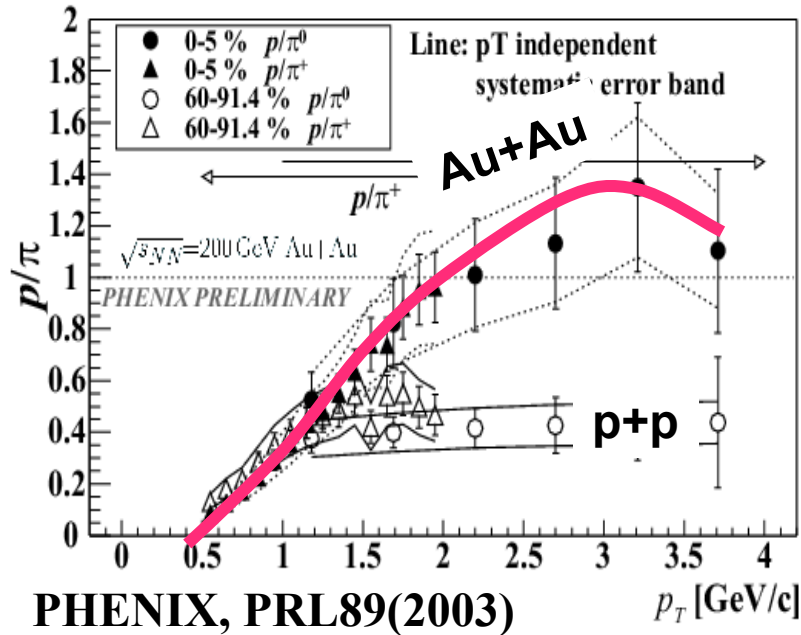


Not superposition of pp collisions, but a nearly thermalized matter which behaves like a perfect fluid!
Zero dissipation?

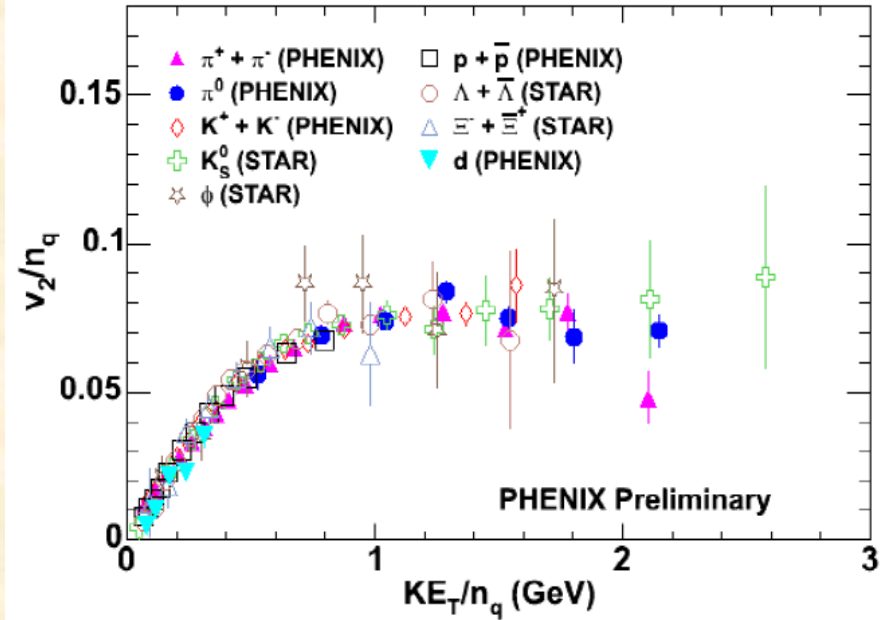


Hadronization Modified

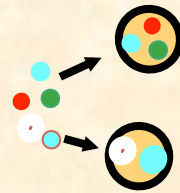
Baryon/Mesons



Quark number scaling



Use medium and not vacuum
 -> Quark coalescence
 More easy to produce baryons!



$$V_{2,M} \left(\frac{1}{n} V^2 \left(\frac{p_T}{n} \right) (p_T/2) \right)$$

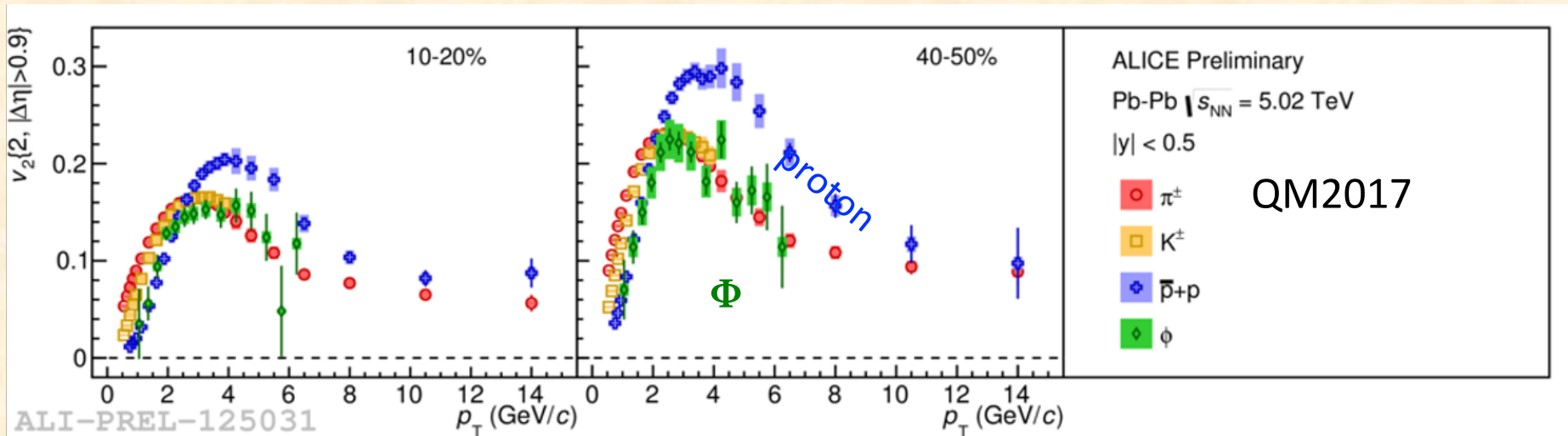
$$V_{2,B} \left(\frac{1}{n} V^2 \left(\frac{p_T}{n} \right) (p_T/3) \right)$$

Hadronization is modified
Dynamical quarks are visible

Last Result from LHC: ϕ flows also with n_q

P (qqq), ϕ (qq) with $M_p \approx M_\phi$

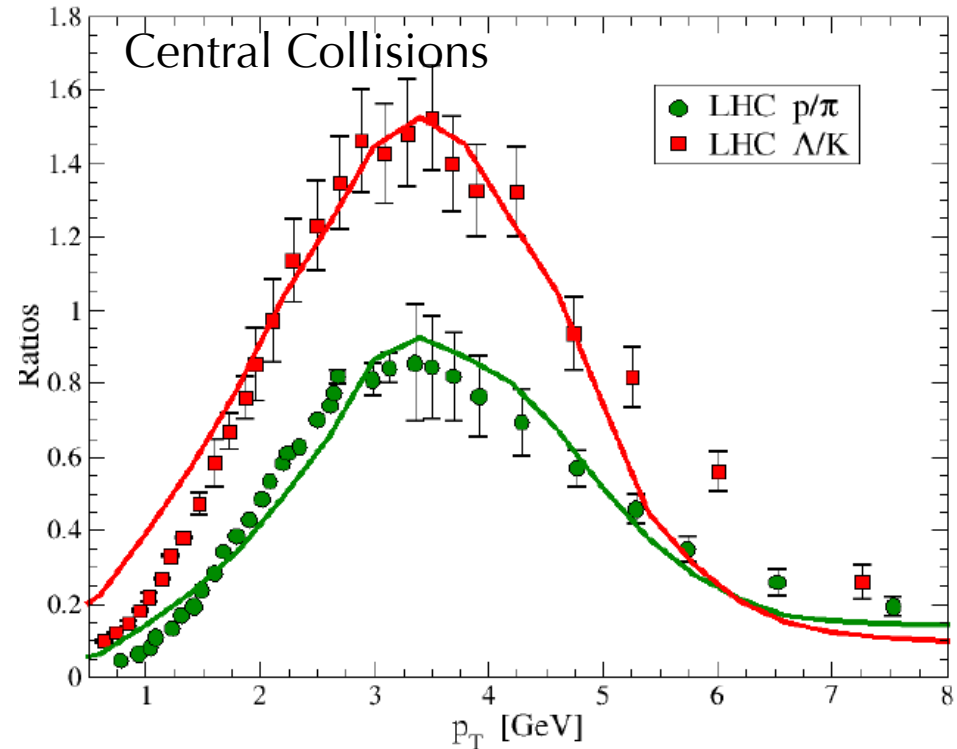
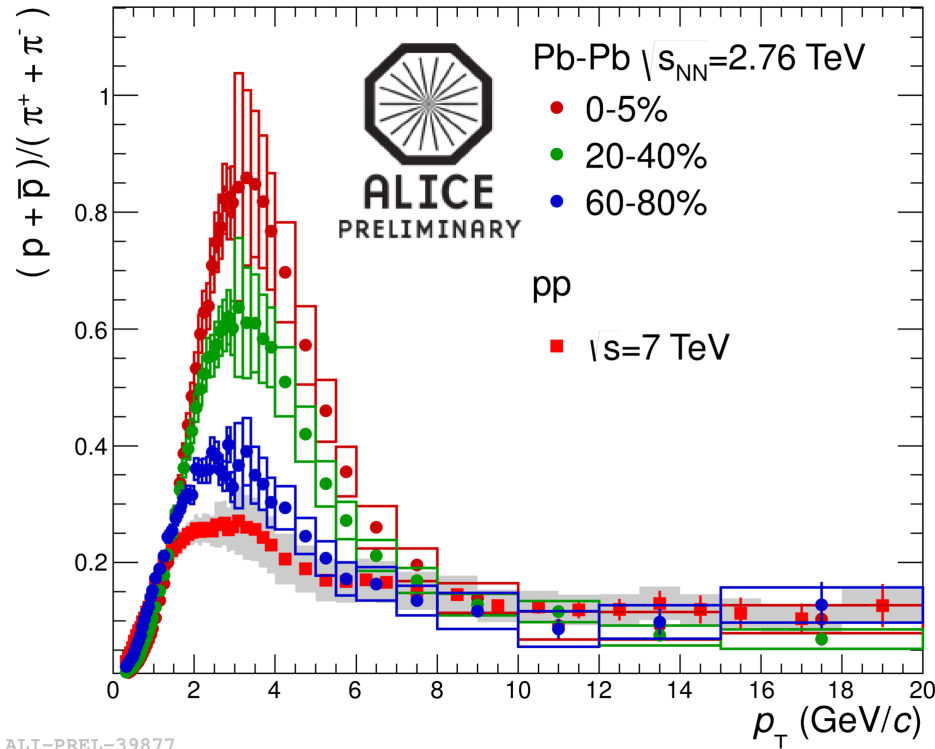
So do they flow at the same way: hydrodynamic flow?



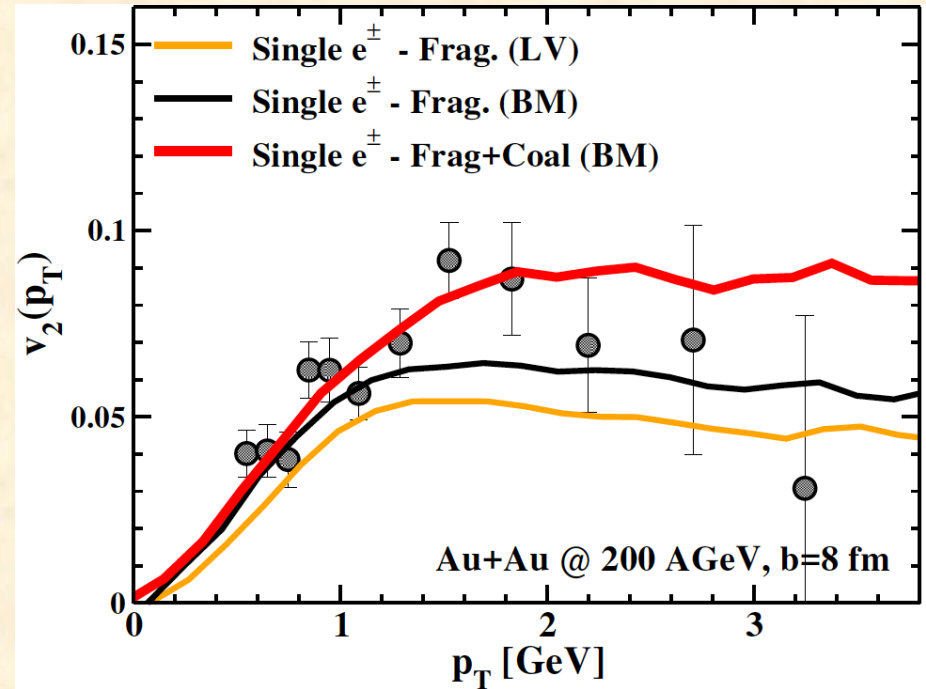
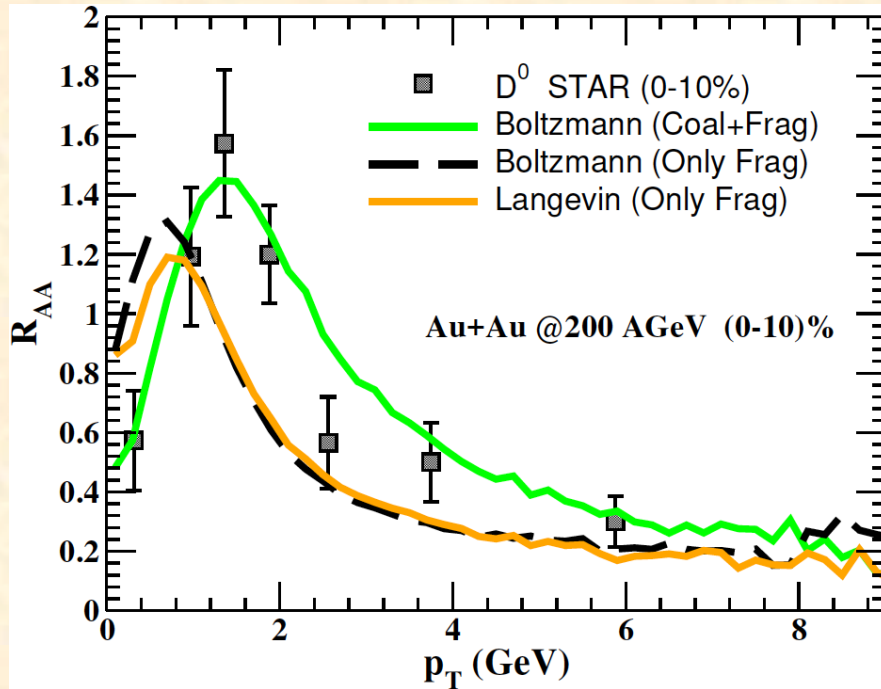
Φ flow with its constituent quark number!!!

Hadronization Modified: B/M Ratios

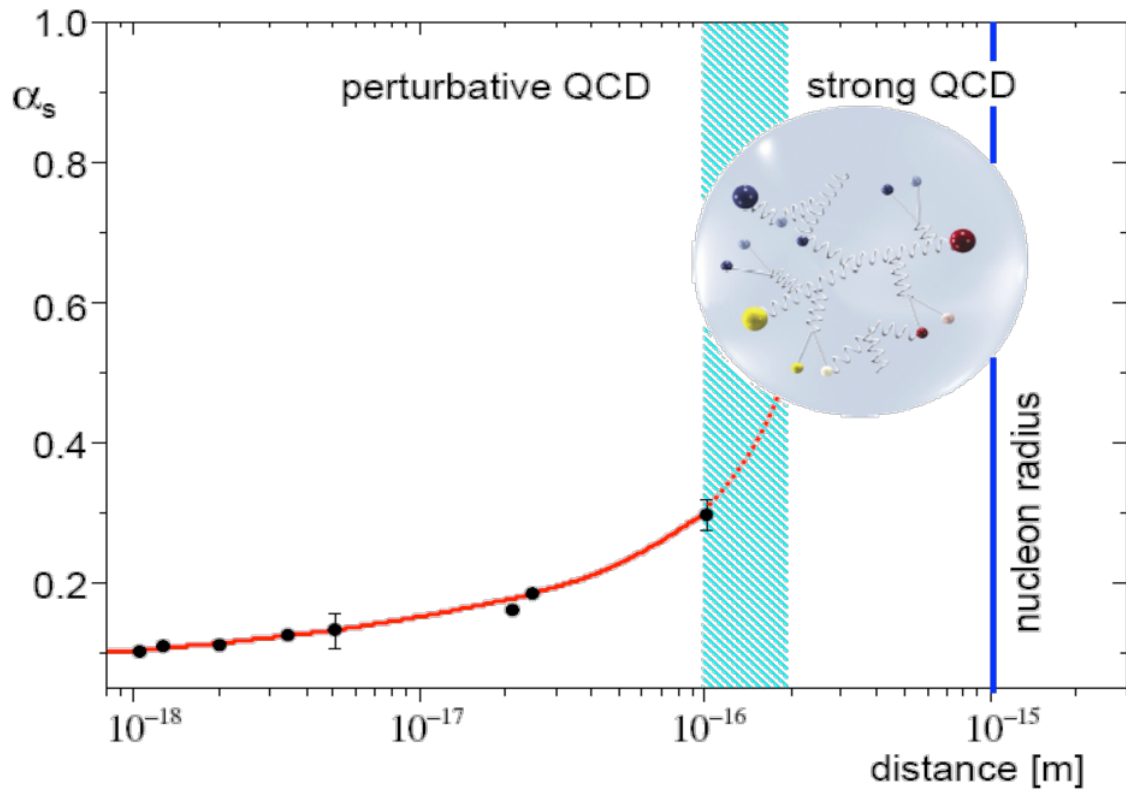
Ratio in Hadronization by Coalescence



What is the impact of coalescence?

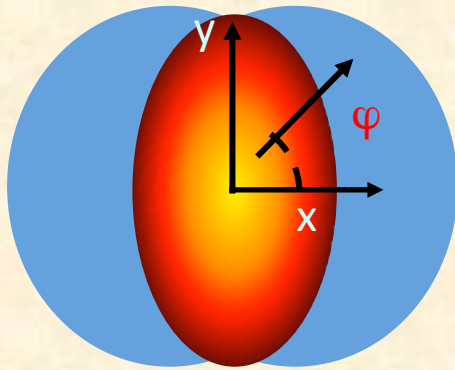


- $R_{AA}(p_T)$ significant reshaped \rightarrow exp. data
- *Opposite to energy loss Coalescence brings up both R_{AA} and v_2*



Relativistic Heavy-Ion Collision when I was Young

Transverse view of HIC



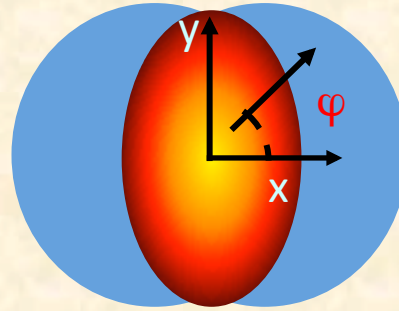
Longitudinal View



With years we have been able to look inside the created matter deeper than expected ...

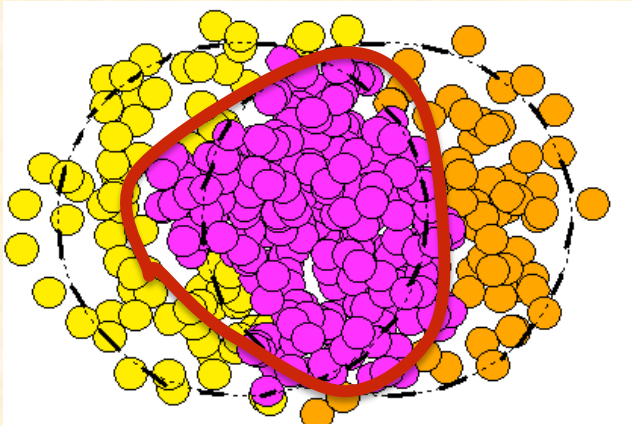
Upgrading the view on the matter created in HIC

Transverse view of HIC



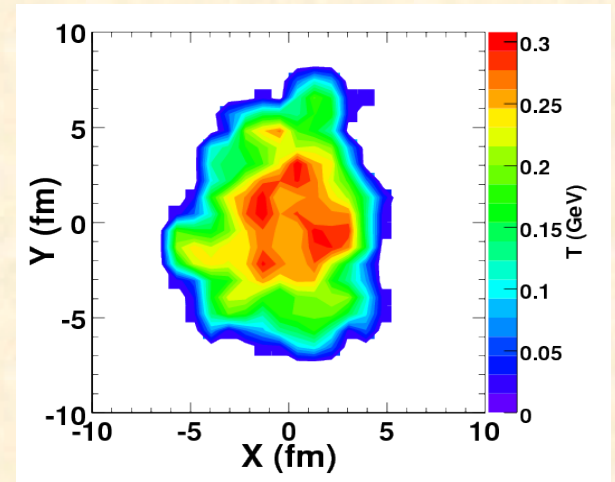
Relativistic HIC
in '90s, '00 till about 2005

Anisotropies $v_n = \langle \cos(n\phi_p) \rangle$ only
with **even** parity due to symmetry



Jacak & Muller, Science 337 (2012)

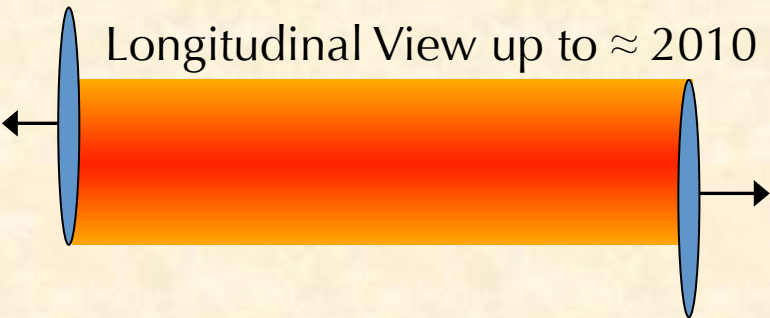
Due to fluctuations
we can have odd v_3 harmonic!



All harmonics appearing
with different weights.

Thanks to the great endeavor of experimentalist to measure even-by-event
[Prof. R. Snelling at 17.50]

Upgrading Longitudinal View



Vorticity \rightarrow Polarization

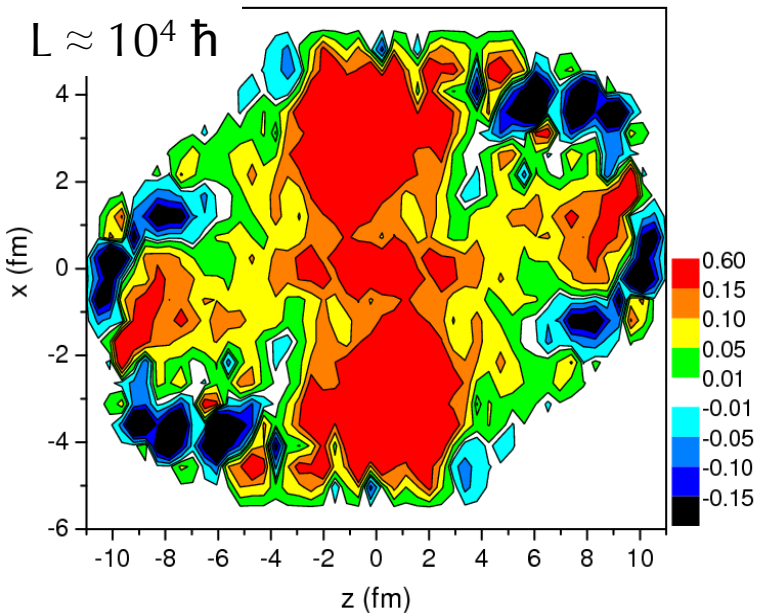
$$S^\mu(p) \approx \frac{1}{m} \epsilon^{\mu\nu\rho\sigma} p_\sigma \frac{\int_\Sigma d\Sigma_\tau p^\tau n_F (1 - n_F) \partial_\nu (u^\mu / T)}{\int_\Sigma d\Sigma_\tau p^\tau n_F}$$

Quantum-Relativistic effect

F. Becattini et al., Ann. Phys. 338 (2013)32



Theory from Becattini & Csernai (MAE)



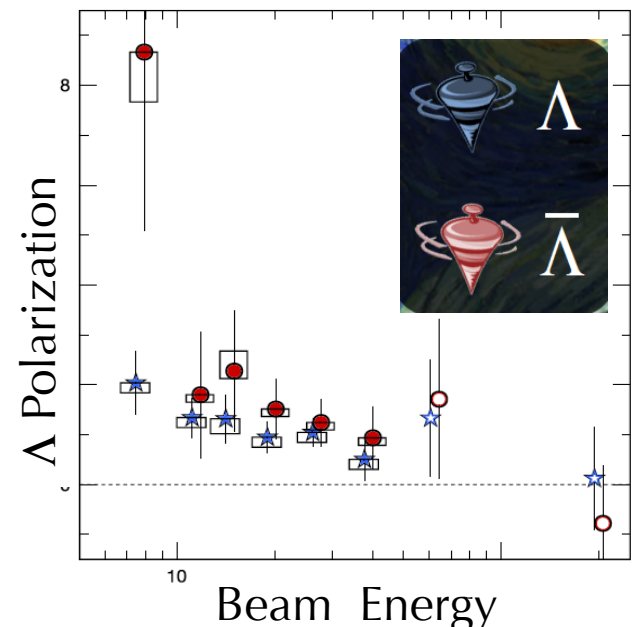
In Hydrodynamics

$$\hbar\omega \approx K_B T \mathcal{P}_\Lambda$$

$$\omega \approx 10^{22} \text{ s}^{-1}$$

Superfluid nanodroplets

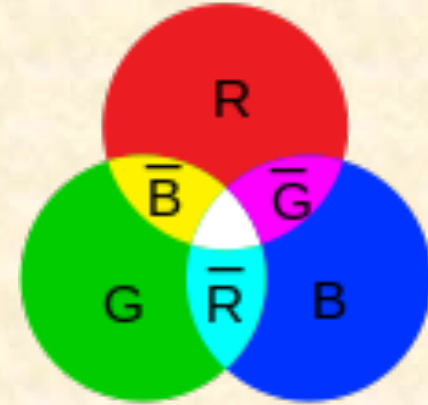
$$\omega \approx 10^7 \text{ s}^{-1}$$



Quantum Chromodynamics

$$\mathcal{L}_{QCD} = \bar{\Psi}(i\gamma_{\mu}\partial_{\mu} - m_i)\Psi - gA_a^{\mu}\bar{\Psi}\gamma_{\mu}t_a\Psi - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}$$

$$F_a^{\mu\nu} = \partial^{\mu}A_a^{\nu} - \partial^{\nu}A_a^{\mu} + if_{abc}A_b^{\mu}A_c^{\nu}$$

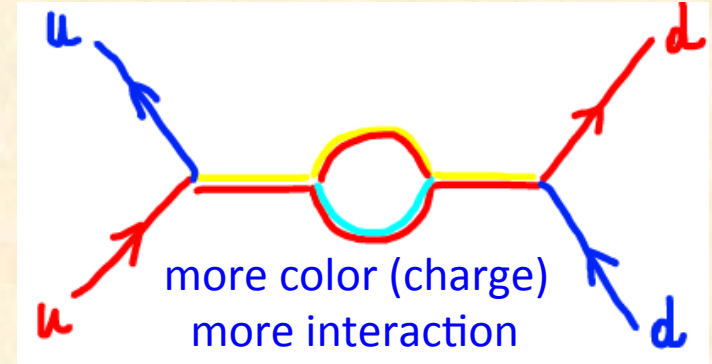
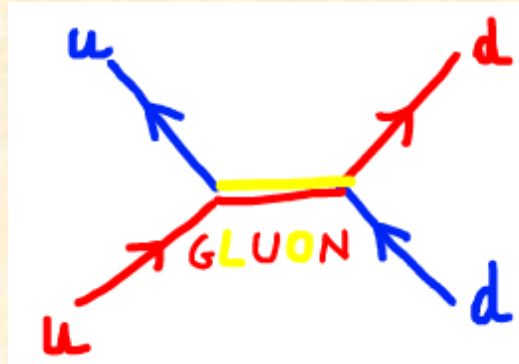
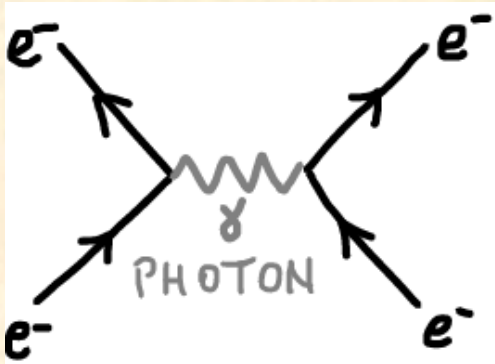


Similar to QED but 3 charges!!!

Because they are “3” they are named “color charges”:

With more than 1 charge → carrier of the interaction

→ must also be colored “charged”

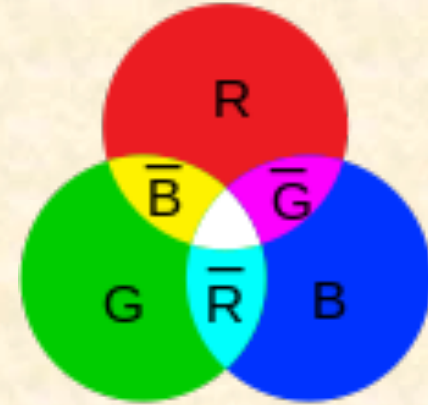


Quantum Flutuatiions

Quantum Chromodynamics

$$L_{QCD} = \bar{\Psi} \left(i \gamma_{\mu} \partial_{\mu} - m_i \right) \Psi - g A_a^{\mu} \bar{\Psi} \gamma_{\mu} t_a \Psi - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$

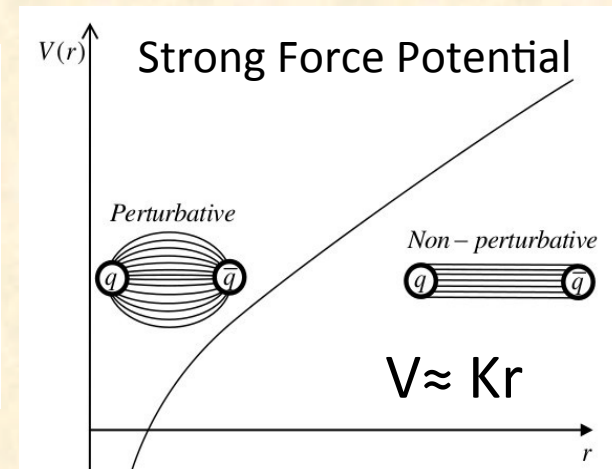
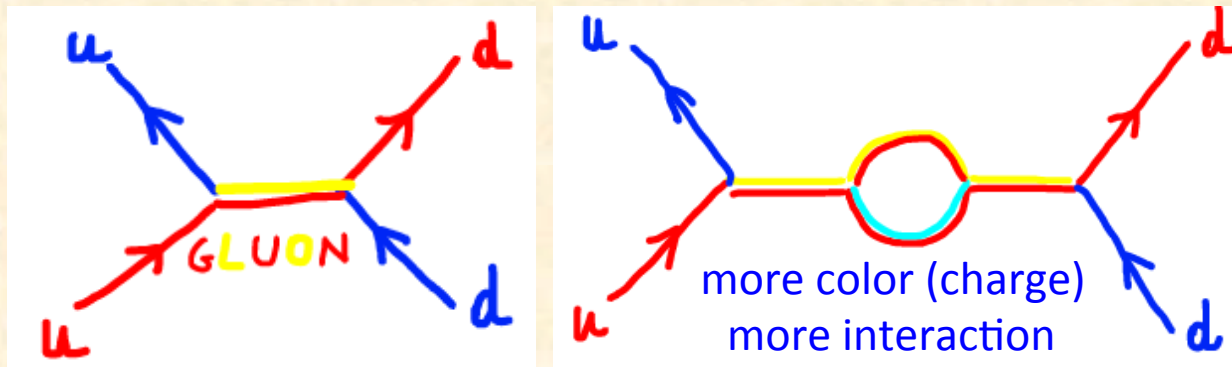
$$F_a^{\mu\nu} = \partial^{\mu} A_a^{\nu} - \partial^{\nu} A_a^{\mu} + i f_{abc} A_b^{\mu} A_c^{\nu}$$



Similar to QED but 3 charges!!!

Because they are “3” they are named “color charges”

→ With more than 1 charge → carrier of the interaction has to be colored → **completely different from QED!**



Difference #1: At small distance quarks interact less, this is a different World!

Asymptotic freedom (Nobel 2004)